

Supplementary Materials

**An Integrated Quay Crane Assignment and Scheduling Problem with Several Contractors in Container Terminals**

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**Table S.1**

Parameters of random instances in small size.

No.	Problem Information												
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
1	3	(4 3 4)	5	(3 2 3 2 3)	(15 14 13 15 16)	(5 7 6)	(5 6 6)	(4 3 5)	7	4	(12 14 11)	11 11 5 7 5 4 8 7 11 7 6 9 5 9 4	22 35 18 20 30 25 17 15 25 14 23 30
2	3	(3 3 3)	4	(3 2 3 3)	(11 12 12 13)	(3 3 4)	(8 8 5)	(3 4 3)	5	3	(12 8 15)	3 7 5 7 3 4 7 5 11 8 6 10	32 5 28 17 31 15 22 25 45
3	4	(2 3 2 3)	5	(2 2 4 3 4)	(10 11 11 14 9)	(2 3 4 3)	(5 6 6 5)	(3 3 4 3)	6	4	(17 20 10 15)	4 9 7 7 9 5 6 6 5 6 8 11 6 4 9 9 5 9 4 8	12 25 18 22 20 30 25 17 17 15 25 35
4	2	(4 5)	3	(4 3 4)	(15 14 12)	(3 3)	(6 5)	(4 3)	5	3	(20 10)	1 9 4 3 7 4	12 21 20 25 17 15 18 22 25 22
5	3	(4 3 3)	5	(3 2 2 3 3)	(12 16 17 15 15)	(2 2 4)	(6 5 6)	(4 3 4)	5	4	(21 12 15)	7 9 6 5 7 8 11 9 11 8 5 9 9 7 10	16 13 15 22 28 26 16 15 21 25 9 27
6	3	(2 3 3)	5	(2 3 4 3 4)	(12 11 13 11 9)	(2 4 3)	(5 5 6)	(4 3 4)	6	1	(16 16 12)	7 9 8 7 7 8 7 9 6 8 5 9 9 7 6	30 33 22 12 28 16 24 11 31

**Table S.1**

Continued

No.	Problem Information												
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
7	3	(3 3 3)	3	(2 4 3)	(11 8 9)	(3 3 2)	(5 5 6)	(2 3 3)	4	3	(12 13 11)	7 9 8 7 7 8 7 9 7	36 43 35 42 38 46 46 45 31
8	3	(4 4 4)	3	(3 3 4)	(8 10 9)	(3 2 3)	(5 5 6)	(4 3 3)	6	2	(20 10 30)	7 9 8 7 9 11 9 11 10	32 28 46 26 49 39 45 35 31 23 31 41
9	3	(3 3 3)	4	(3 3 4 4)	(11 16 14 12)	(3 3 2)	(5 5 6)	(4 3 4)	5	1	(16 11 23)	7 9 8 7 7 8 7 9 11 8 5 9	32 28 16 16 25 11 15 15 27
10	3	(4 4 3)	4	(4 3 2 4)	(11 12 13 12)	(3 3 3)	(5 5 5)	(4 3 4)	6	2	(16 13 15)	7 9 8 7 7 8 7 9 11 9 11 10	20 23 25 32 28 36 16 25 11 25 15 27
11	3	(4 4 3)	4	(3 5 2 5)	(14 16 15 14)	(3 4 2)	(5 6 6)	(2 3 3)	6	3	(15 16 11)	7 5 8 7 7 7 8 5 8 9 6 10	9 5 35 32 8 16 16 35 9 25 15 21
12	4	(3 5 4 2)	5	(5 3 4 5 4)	(12 14 11 10 11)	(4 3 3 2)	(6 6 7 5)	(3 3 4 2)	7	3	(19 16 14 17)	8 6 7 5 7 9 4 6 7 8 5 6 3 6 4 8 6 5 8 4	23 17 9 11 12 20 19 18 8 24 22 10 17 30 28 16 15 19 22 12
13	3	(4 5 4)	6	(4 5 3 4 4 5)	(10 11 12 10 12 12)	(2 3 4)	(3 5 4)	(2 3 4)	4	4	(15 14 11)	5 9 8 6 7 7 7 9 12 8 8 11 6 7 10 9 8 9	24 8 15 12 14 24 9 21 11 17 15 17 18 19 22

**Table S.1**

Continued

No.	Problem Information												
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
14	6	(4 5 3 5 3 4)	6	(4 4 5 3 5 4)	(11 14 12 13 13 12)	(4 5 4 4 3 2)	(6 6 5 6 4 5)	(3 2 2 3 3 2)	7	3	(10 21 23 14 12 17)	5 9 9 8 6 7 6 6 9 5 6 4 8 9 8 7 8 5 7 8 6 5 7 4 6 8 5 7 4 7 5 7 6 5 6 6	20 33 35 36 25 14 32 18 16 18 34 32 16 25 8 32 18 23 15 11 27 28 17 21 9 24 14 11 21 16
15	4	(4 5 5 3)	6	(5 5 4 5 3 4)	(12 11 10 11 10 11)	(3 3 2 4)	(6 7 5 6)	(3 4 3 3)	3	4	(11 9 14 10)	9 9 5 8 7 6 4 6 7 6 7 5 6 7 5 6 8 6 7 5 6 4 5 7	20 23 24 27 18 16 28 26 26 21 26 29 25 24 24 28 19 26 25 27
16	6	(5 3 4 5 5 4)	6	(5 4 5 3 3 5)	(10 12 11 13 13 11)	(4 4 5 3 4 5)	(7 8 6 7 6 6)	(4 4 3 4 3 3)	6	4	(12 16 15 10 9 13)	8 5 6 7 4 7 5 6 7 6 4 6 9 7 8 9 8 7 9 9 8 7 8 9 5 9 8 6 7 8 8 4 6 5 7 6	33 23 18 32 16 29 23 37 16 24 32 18 19 16 32 17 27 31 22 28 36 19 10 21 20 16 23 19 11 22
17	4	(3 3 5 2)	5	(4 4 5 3 4)	(15 13 14 12 14)	(3 3 4 3)	(7 8 6 8)	(4 4 3 4)	8	5	(11 16 14 18)	9 5 7 6 7 4 6 5 8 3 6 4 7 4 9 5 5 6 4 8	12 24 14 22 24 12 9 23 26 20 25 26 15 19 20 10 19 27 21 16
18	2	(4 5)	4	(5 3 4 4)	(10 9 11 9)	(5 4)	(6 5)	(3 3)	3	5	(14 10)	7 5 6 6 8 7 8 7	22 19 11 29 35 42 24 31 36 13
19	4	(4 3 4 2)	4	(4 5 4 5)	(10 9 10 8)	(3 5 4 2)	(8 8 7 5)	(4 5 4 3)	5	5	(19 11 13 15)	9 12 9 8 8 7 9 11 7 9 9 7 6 5 9 8	20 33 39 33 32 28 36 42 26 25 31 23 35 35 17 11

**Table S.1**

Continued

No.	Problem Information												
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
20	4	(4 4 3 4)	4	(3 3 2 4)	(9 9 10 9)	(3 4 3 2)	(3 3 5 4)	(2 2 3 2)	7	5	(12 17 23 16)	8 11 8 11 5 9 8 9 8 9 10 5 6 5 7 9	25 33 35 24 36 28 36 37 29 38 36 38 30 35 37 31
21	2	(3 5)	3	(5 3 4)	(10 11 12)	(2 2)	(7 6)	(3 3)	3	4	(14 12)	8 9 9 11 9 7	24 33 29 22 32 28 21 25 25 19
22	4	(4 4 5 3)	6	(4 3 4 5 4 5)	(14 13 12 13 12 13)	(2 3 4 4)	(5 5 6 5)	(3 2 3 3)	2	3	(15 12 10 13)	8 7 7 6 9 5 6 5 8 6 7 5 7 8 5 6 6 5 7 8 5 7 6 4	20 33 34 27 38 16 28 36 26 21 26 29 25 29 24 28 19 26 28 27
23	5	(4 5 4 5 3)	6	(4 5 3 4 5 4)	(12 13 12 13 13 11)	(4 3 3 2 3)	(5 6 6 6 4)	(4 3 3 3 2)	4	6	(13 11 12 13 11)	11 8 9 10 11 9 7 8 9 9 8 8 7 6 8 7 8 6 8 5 7 6 9 8 7 9 5 7 6 8	20 13 34 23 30 22 28 11 27 16 12 15 27 26 32 15 13 32 29 19 15 26 11 16 24
24	5	(3 5 2 3 4)	6	(4 5 5 4 4 5)	(12 14 15 16 14 14)	(4 3 3 2 3)	(6 7 6 6 7)	(3 4 3 3 4)	3	8	(13 11 12 13 11)	9 6 7 5 8 6 4 7 5 6 6 7 4 6 7 4 8 6 7 4 5 7 4 7 5 5 6 4 7 7	11 10 27 31 22 21 22 21 14 13 26 10 12 11 19 28 29 14 19 27 16 21 9 20 12
25	5	(3 4 3 3 4)	6	(4 5 4 4 5 4)	(15 17 16 15 16 15)	(2 3 3 4 3)	(8 6 7 7 8)	(4 3 4 4 4)	7	11	(21 17 16 16 19)	8 6 7 5 8 9 6 8 5 7 6 4 5 7 7 6 6 8 7 6 7 6 5 5 9 4 8 6 7 6	21 17 19 24 22 14 18 15 22 28 11 16 19 26 12 17 20 28 12 18

**Table S.1**

Continued

No.	Problem Information												
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
26	2	(4 5)	4	(5 4 3 4)	(8 11 13 9)	(4 3)	(7 6)	(4 4)	2	4	(13 12)	6 8 5 4 7 5 6 4	33 15 12 36 25 21 15 27 15 26
27	3	(4 3 4)	5	(2 4 4 3 4)	(14 17 13 15 15)	(2 3 3)	(6 5 6)	(4 3 5)	2	2	(12 14 13)	11 9 8 9 6 8 6 8 11 9 8 5 6 6 7	10 33 15 32 22 6 16 15 31 21 5 17
28	3	(3 3 3)	4	(3 5 4 3)	18 16 17 15	(3 2 3)	(8 7 6)	(3 3 2)	3	2	(7 18 9)	13 6 8 9 5 4 8 6 9 7 8 7	17 7 18 35 34 15 15 21 41
29	4	(3 3 3 2)	6	(4 3 5 4 4 5)	(10 9 7 11 8 9)	(2 3 3 4)	(6 6 7 5)	(3 4 4 3)	7	1	(12 12 14 11)	7 9 7 6 11 5 6 5 6 9 11 7 7 7 8 6 9 8 8 5 10 8 9 6	40 33 30 22 32 18 16 34 36 25 31 24
30	3	(3 3 3)	5	(3 5 3 2 5)	15 15 16 14 15	(3 3 3)	(4 8 5)	(2 4 3)	8	4	(13 16 13)	5 8 5 7 5 11 8 7 9 5 8 7 7 6 7	22 35 18 30 10 35 17 15 5

**Table S.2**

The first part of parameters of random instances in large size.

No.	Problem Information						
	$M$	$J_m$	$Q$	$I_q$	$\mu_q$	$D_m$	$R_m$
1	4	(5 4 5 5)	7	(4 5 4 4 5 3 4)	(43 65 37 54 30 44 51)	(8 11 7 9)	(190 230 205 310)
2	5	(4 4 5 5 4)	7	(5 3 5 5 4 4 5)	(47 35 54 45 60 49 39)	(17 14 20 15 12)	(55 52 49 47 60)
3	6	(4 5 5 4 5 5)	7	(4 4 5 4 5 4 4)	(55 43 47 39 48 55 49)	(11 15 17 12 18 14)	(179 237 369 360 290 340)
4	7	(5 5 4 4 5 5 5)	7	(5 4 5 3 4 5 5)	(46 53 42 39 46 44 56)	(16 11 17 15 10 18 15)	(157 284 257 163 158 284 356)
5	3	(5 4 3)	7	(3 5 4 5 3 3 4)	(56 73 45 27 35 52 39)	(16 14 15)	(286 352 175)
6	3	(4 3 4)	5	(3 3 3 2 3)	(47 36 53 40 29)	(12 16 17)	(248 165 249)
7	4	(3 2 3 3)	5	(4 4 2 3 4)	(46 53 44 58 39)	(16 18 12 15)	(275 196 186 230)
8	4	(5 3 5 5)	6	(5 5 4 3 4 3)	(45 64 73 40 55 64)	(16 18 13 11)	(239 264 258 248)
9	5	(3 5 4 5 5)	6	(4 4 5 4 5 3)	(44 57 63 48 39 69)	(16 13 15 17 12)	(164 286 256 198 223)
10	6	(3 4 4 5 4 5)	6	(4 5 5 4 3 4)	(56 47 63 45 37 51)	(14 16 14 17 15 12)	(376 254 256 176 265 256)

**Table S.3**

The second part of parameters of random instances in large size.

No.	Problem Information					
	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
1	(80 125 120 170)	15	90	(45 66 49 70)	45 38 65 56	
					47 29 76 45	188 360 295 340
					65 48 54 38	350 275 390 280
					45 54 27 54	405 370 400 190
					54 55 46 48	355 540 370 450
					67 54 56 68	440 380 530 290
					55 48 65 39	
					38 43 55 67 69	
					46 64 55 63 49	270 485 380 430 345
					47 55 64 57 50	386 295 485 453 395
2	(28 25 24 30 35)	12	35	(46 38 53 55 46)	64 57 64 38 49	370 564 485 290 468
					44 63 58 48 50	196 348 548 374 279
					56 74 56 49 59	439 463 473 480 310
					65 78 56 64 49	
					49 53 69 53 53 39	
					48 63 49 72 36 48	389 478 386 148 379 296
					48 63 54 73 48 36	467 535 289 376 438 539
					58 63 47 56 38 64	427 377 455 297 486 290
					47 63 38 72 47 55	347 538 463 286 464 386
					38 74 56 75 48 64	537 475 386 576 465 576
3	(80 120 160 180 130 170)	16	49	(37 62 54 57 37 63)	58 47 64 58 36 85	
					78 46 73 48 67 38 64	
					74 56 93 57 64 54 38	367 537 647 257 386 486 463
					46 56 73 64 55 87 48	536 573 453 296 463 465 365
					84 57 65 52 58 67 25	587 565 276 379 586 386 358
					58 63 63 84 74 58 92	456 456 365 475 265 387 465
					74 56 75 62 46 82 49	573 298 465 480 276 586 496
					46 57 28 64 52 57 63	
4	(90 140 170 85 75 125 190)	19	54	(84 63 57 62 85 66 73)		



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No.	Problem Information					
	$R'_m$	$C$	$C'$	$I_m$	$C''_{qm}$	$\omega_{jm}$
5	(145 175 85)	22	42	(46 58 73)	53 64 57	374 583 496
					74 56 36	465 397 476
					46 73 45	487 286 186
					49 55 38	386 497 276
					47 63 48	475 309 197
					48 63 58	386 466 276
					66 48 53	199 286 539
6	(145 85 150)	20	35	(35 63 44)	46 57 53	375 485 298
					53 47 41	638 584 538
					55 61 48	573 273 387
					32 47 52	297 427 364
					63 46 51	
7	(139 110 104 125)	35	45	(48 64 58 66)	47 36 53 29	
					47 58 73 46	387 539 599 334
					55 39 74 68	476 599 370 453
					44 63 48 57	298 196 630 520
					55 48 64 39	
8	(130 145 150 125)	45	40	(48 65 49 29)	46 74 58 66	487 563 287 573
					46 74 65 48	537 276 375 453
					77 56 38 54	186 352 532 275
					55 64 58 36	264 536 186 573
					64 75 46 53	354 450 455 376
					55 47 39 64	
9	(86 142 125 105 110)	22	30	(57 38 72 47 58)	43 74 57 64 55	463 475 286 374 463
					47 63 58 69 83	645 354 563 465 466
					59 73 68 73 57	487 367 367 647 386
					58 73 52 68 98	732 386 486 574 646
					47 84 92 40 37	476 365 365 677 455
					57 38 75 93 63	
10	(180 120 130 140 130 225)	25	45	(39 84 56 74 36 46)	47 63 47 58 84 55	365 465 254 587 465 376
					46 73 68 57 63 50	176 367 467 376 267 638
					54 57 63 49 73 87	476 537 645 653 578 387
					58 74 63 59 68 72	567 376 678 387 268 198
					58 63 59 67 54 83	367 532 467 527 398 467
					65 73 56 45 59 46	

**Table S.4**

Computational results of random instances in small and large sizes

No:	B&B						TLBO						Gap (%)
	$T_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	$T_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	
1	(3,3,3)	(2,4,3)	(0,0,0)	q1:m1 ; q3:m2 q5:m3	2140	22	(3,3,3)	(2,4,3)	(0,0,0)	q1:m1 ; q3:m2 q5:m3	2150	6	0.4
2	(3,3,4)	(0,0,0)	(0,0,0)	q1:m1 ; q3:m2 q4:m3	1406	36	(3,3,4)	(0,0,0)	(0,0,0)	q1:m1 ; q3:m2 q4:m3	1430	7	1.7
3	(3,3,2,4)	(0,0,2,0)	(1,0,0,1)	q1:m1 ; q3:m2 q4:m3 ; q5:m4	1228	94	(3,3,2,4)	(0,0,2,0)	(1,0,0,1)	q1:m1 ; q3:m2 q4:m3 ; q5:m4	1228	8	0
4	(2,3)	(1,0)	(0,0)	q1:m1 ; q3:m2	1049	19	(2,3)	(1,0)	(0,0)	q1:m1 ; q3:m2	1057	5	0.7
5	(3,2,2)	(0,0,2)	(1,0,0)	q1:m1 ; q4:m2 q5:m3	1032	23	(3,2,2)	(0,0,2)	(1,0,0)	q1:m1 ; q4:m2 q5:m3	1032	6	0
6	(3,3,4)	(0,1,0)	(1,0,1)	q3:m1 ; q4:m2 q5:m3	999	445	(3,3,3)	(0,1,0)	(1,0,0)	q1:m1 ; q2:m2 q3:m3	1009	6	1
7	(7,6,6)	(0,0,0)	(4,3,4)	q1:m1 ; q2:m2 q3:m3	2011	494	(7,6,6)	(0,0,0)	(4,3,4)	q1:m1 ; q2:m2 q3:m3	2083	10	3.5
8	(6,6,6)	(0,0,0)	(3,4,3)	q1:m1 ; q2:m2 q3:m3	5343	27	(6,6,6)	(0,0,0)	(3,4,3)	q1:m1 ; q2:m2 q3:m3	5959	10	11
9	(2,3,3)	(1,0,0)	(0,0,1)	q2:m1 ; q3:m2 q4:m3	492	14	(2,3,3)	(1,0,0)	(0,0,1)	q2:m1 ; q3:m2 q4:m3	492	6	0
10	(3,4,4)	(0,0,0)	(0,1,1)	q1:m1 ; q2:m2 q4:m3	1918	344	(3,4,4)	(0,0,0)	(0,1,1)	q1:m1 ; q2:m2 q4:m3	1918	7	0
11	(2,3,3)	(1,1,0)	(0,0,1)	q2:m1 ; q3:m2 q4:m3	2030	11	(3,3,3)	(0,1,0)	(0,0,1)	q1:m1 ; q2:m2 q4:m3	2166	6	6

**Table S.4**

Continued

No:	B&B						TLBO						
	$T'_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	$T'_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	Gap (%)
12	(2,3,3,2)	(2,0,0,0)	(0,0,0,0)	q2:m1 ; q3:m2 q4:m3 ; q5:m4	2703	72	(2,3,3,2)	(2,0,0,0)	(0,0,0,0)	q2:m1 ; q3:m2 q4:m3 ; q5:m4	2746	10	1.5
13	(3,2,2)	(0,1,2)	(1,0,0)	q1:m1 ; q2:m2 q6:m3	1048	799	(3,2,2)	(0,1,2)	(1,0,0)	q1:m1 ; q2:m2 q6:m3	1061	8	1.2
14	(3,3,4,4,3,4)	(1,2,0,0,0,0)	(0,0,0,0,0,2)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6	6379	45	(3,3,3,4,3,3)	(1,2,1,0,0,0)	(0,0,0,0,0,1)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6	6963	14	9.1
15	(3,3,3,3)	(0,0,0,1)	(0,0,1,0)	q1:m1 ; q2:m2 q4:m3 ; q5:m4	1391	41	(3,3,3,3)	(0,0,0,1)	(0,0,1,0)	q1:m1 ; q2:m2 q4:m3 ; q5:m4	1392	10	0
16	(4,4,4,4,4,3)	(0,0,1,0,0,2)	(0,0,0,1,0,0)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6	6133	34	(4,4,4,4,4,3)	(0,0,1,0,0,2)	(0,0,0,1,0,0)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6	6969	15	13.6
17	(2,2,2,2)	(1,1,2,1)	(0,0,0,0)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	1211	960	(2,2,2,2)	(1,1,2,1)	(0,0,0,0)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	1211	7	0
18	(4,4)	(1,0)	(0,0)	q1:m1 ; q3:m2	2005	111	(4,4)	(1,0)	(0,0)	q1:m1 ; q3:m2	2010	7	0.2
19	(4,5,5,6)	(0,0,0,0)	(1,0,1,4)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	2814	199	(4,5,5,6)	(0,0,0,0)	(1,0,1,4)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	2862	14	1.7
20	(5,6,6,5)	(0,0,0,0)	(2,2,3,3)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	6096	832	(6,6,6,5)	(0,0,0,0)	(3,2,3,3)	q1:m1 ; q2:m2 q3:m3 ; q4:m4	6726	11	10.3
21	(3,4)	(0,0)	(1,2)	q2:m1 ; q3:m2	1143	900	(3,4)	(0,0)	(1,2)	q2:m1 ; q3:m2	1153	7	0.8
22	(3,3,3,3)	(0,0,1,1)	(1,0,0,0)	q1:m1 ; q3:m2 q4:m3 ; q6:m4	1195	48	(3,3,3,3)	(0,0,1,1)	(1,0,0,0)	q1:m1 ; q3:m2 q4:m3 ; q6:m4	1196	9	0

**Table S.4**

Continued

No:	B&B						TLBO						Gap (%)
	$T_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	$T_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	
23	(2,3,3,3,3)	(2,0,0,0,0)	(0,0,0,1,0)	q1:m1 ; q2:m2 q4:m3 ; q5:m4 q6:m5	2219	23	(2,3,3,3,3)	(2,0,0,0,0)	(0,0,0,1,0)	q1:m1 ; q2:m2 q4:m3 ; q5:m4 q6:m5	2239	10	23
24	(2,2,2,3,2)	(2,1,1,0,1)	(0,0,0,1,0)	q2:m1 ; q3:m2 q4:m3 ; q5:m4 q6:m5	1145	164	(2,2,2,3,2)	(2,1,1,0,1)	(0,0,0,1,0)	q2:m1 ; q3:m2 q4:m3 ; q5:m4 q6:m5	1169	11	24
25	(2,2,2,2,2)	(0,1,1,2,1)	(0,0,0,0,0)	q1:m1 ; q2:m2 q3:m3 ; q5:m4 q6:m5	1623	4	(2,2,2,2,2)	(0,1,1,2,1)	(0,0,0,0,0)	q1:m1 ; q2:m2 q3:m3 ; q5:m4 q6:m5	1623	7	25
26	(3,4)	(1,0)	(0,1)	q2:m1 ; q3:m2	1156	237	(3,4)	(1,0)	(0,1)	q2:m1 ; q3:m2	1195	7	26
27	(2,3,3)	(0,0,0)	(0,0,0)	q2:m1 ; q4:m2 q5:m3	641	84	(2,3,3)	(0,0,0)	(0,0,0)	q2:m1 ; q4:m2 q5:m3	641	6	27
28	(2,3,3)	(1,0,0)	(0,1,0)	q1:m1 ; q2:m2 q3:m3	584	21	(2,3,3)	(1,0,0)	(0,1,0)	q1:m1 ; q2:m2 q3:m3	584	6	28
29	(4,4,3,4)	(0,0,0,0)	(2,1,0,0)	q1:m1 ; q2:m2 q4:m3 ; q6:m4	1704	30	(4,4,3,4)	(0,0,0,0)	(2,1,0,0)	q1:m1 ; q2:m2 q4:m3 ; q6:m4	1704	9	29
30	(3,3,3)	(0,0,0)	(0,0,0)	q1:m1 ; q3:m2 q5:m3	1597	24	(3,3,3)	(0,0,0)	(0,0,0)	q1:m1 ; q3:m2 q5:m3	1597	6	30
31	-	-	-	-	-	more than one hour	(13 9 12 11)	(0 2 0 0)	(5 0 5 2)	q1:m1 ; q2:m2 q4:m3 ; q7:m4	600942	34	31
32	-	-	-	-	-	more than one hour	(10 12 14 10 12)	(7 2 6 5 0)	(0 0 0 0 0)	q1:m1 ; q3:m2 q4:m3 ; q5:m4 q6:m5	372812	42	32

**Table S.4**

Continued

No:	B&B						TLBO						Gap (%)
	$T'_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	$T'_m$	$E_m$	$F_m$	Assignment	OFV	CPU Time (s)	
33	-	-	-	-	-	more than one hour	(11 15 14 10 12 15)	(0 0 3 2 6 0)	(0 0 0 0 0 1)	q1:m1 ; q3:m2 q4:m3 ; q5:m4 q6:m5 ; q7:m6	927570	47	-
34	-	-	-	-	-	more than one hour	(16 15 16 17 15 15 12)	(0 0 1 0 0 3 3)	(0 4 0 2 5 0 0)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6 q7:m7	1957922	65	-
35	-	-	-	-	-	more than one hour	(7 14 10)	(9 0 5)	(0 0 0)	q2:m1 ; q3:m2 q6:m3	303408	27	-
36	-	-	-	-	-	more than one hour	(16 18 13)	(0 0 4)	(4 2 0)	q1:m1 ; q2:m2 q3:m3	495681	26	-
37	-	-	-	-	-	more than one hour	(12 12 11 14)	(4 6 1 1)	(0 0 0 0)	q1:m1 ; q2:m2 q4:m3 ; q5:m4	278545	29	-
38	-	-	-	-	-	more than one hour	(9 8 11 13)	(7 10 2 0)	(0 0 0 2)	q2:m1 ; q3:m2 q5:m3 ; q6:m4	1814196	31	-
39	-	-	-	-	-	more than one hour	(15 13 12 15 13)	(1 0 3 2 0)	(0 0 0 0 1)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q6:m5	1396838	37	-
40	-	-	-	-	-	more than one hour	(11 13 13 18 16 14)	(3 3 1 0 0 0)	(0 0 0 1 1 2)	q1:m1 ; q2:m2 q3:m3 ; q4:m4 q5:m5 ; q6:m6	1987959	51	-