

1 **Three-dimensional repositioning of jaw in the orthognathic surgery using the**  
2 **binocular stereo vision**

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10 **Abstract**

11 In recent years, the binocular stereo vision has become more popular in many  
12 different areas because of the latest developments in three-dimensional (3-D) image  
13 processing technology that ensures rich information in comparison with other sensor  
14 types. This study presents a novel method based on the binocular stereo vision system to  
15 reduce the measurement error encountered frequently in the orthognathic surgery. The  
16 main aim is to enhance the level of the accuracy of this sensitive operation. The  
17 developed system is not only useful for the preoperative assessment or the postoperative  
18 process but also can be utilized during the real-time operation. Additionally, this system  
19 provides a broader working field, more practical and healthier environment and less  
20 expensive setup. Therefore, the developed binocular stereo vision system may be  
21 acceptable for most surgeons. Experimental results show that the average error rate for  
22 all of X, Y and Z coordinates in the Cartesian system is 0.25 mm which is clinically  
23 acceptable (< 1.00 mm). The binocular stereo vision system would be a helpful

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1 throughout the orthognathic surgery to improve precision of the measurement and  
2 satisfy the healthy surgical operating environment.

3 **Key Words:** Measurement error, 3-D coordinate measurement, three-dimensional (3-D)  
4 image processing, stereo vision, stereo imaging, 3-D image-guided orthognathic  
5 surgery, real-time surgical navigation.

## 6 **1. Introduction**

7 The orthodontics is one of the oldest divisions of the dentistry. The orthognathic  
8 surgery is the surgical correction of skeletal anomalies or malformations including the  
9 maxilla or the mandible [1]. The success of the surgery depends on the correct  
10 diagnosis, and the special preoperative plan [2]. The orthognathic surgical planning  
11 should be performed correctly before the operation. According to this planning, it is  
12 necessary to reposition the jaws accurately with the desired direction and displacement,  
13 since it is crucial to re-establish physiological functions and esthetic anatomy after the  
14 surgical operation [3]. However, the orthognathic surgery studies show that there are  
15 some significant differences between the preoperative surgical planning and  
16 postoperative results [4]. These differences result from inability to transfer the  
17 numerical data, which is derived from the surgical planning to the operation accurately.  
18 This situation affects the achievement of the orthognathic surgery negatively. The major  
19 errors can be classified as application error, human error, registration error, technical  
20 error, and imaging error [5]. The mistakes that are made during the operation affect the  
21 surgery result negatively because the surgeons who are aware of these disadvantages  
22 have no intention to use the technical devices routinely. At present, the typical method  
23 for repositioning jaws in the correct location is based on the utilizing the surgical  
24 splints.

1       The three-dimensional (3-D) measurement of the jaw and teeth is an important task  
2 for the computerized vision systems. The stereo vision has become more popular in  
3 many different areas because of the latest development in three-dimensional technology  
4 and also vision sensors ensure rich information in comparison with other sensor types  
5 [6, 7]. Recent advances in computer vision make it possible to acquire high-resolution  
6 3-D models of scenes and objects [8]. The advantage of 3-D model construction from  
7 two-dimensional (2-D) images is that it does not require specialized equipment; only a  
8 simple digital camera can fulfill the requirement. Specialized equipment like laser  
9 scanners can lead to a very accurate construction of 3-D models. However, this  
10 equipment is generally very expensive, and it may not be safe using in applications like  
11 human body modeling [9]. The traditional methods of preoperative preparation are  
12 based on the lateral and the frontal radiographic images and computer-based  
13 tomography devices [10–12]. Nevertheless, these devices have some significant  
14 disadvantages such as radiation, high cost, impracticality and low precision level.  
15 Therefore, numerous approaches presented in the literature in order to mitigate side  
16 effects of using such devices [13].

17       In this paper, a novel method is developed with 3-D image-guided surgery  
18 navigation by applying the stereo vision, in order to realize the real-time tracking the  
19 position and the rotation of the patient with the instruments. The proposed method  
20 guides the surgeon during the surgical operation whether the actual 3-D position of the  
21 jaw matches with the preoperative measurements by getting real-time, more accurate  
22 information of repositioning of the irregular jaw sections.

1 The rest of paper starts with introducing stereo processing in Section 2. The  
2 experimental setup and measurements are given in Section 3. Section 4 discusses and  
3 analyzes the experimental results. Section 5 concludes the paper.

## 4 **2. Stereo Processing**

5 The system consists of pre-calibrated binocular stereo camera operating in the  
6 visible spectrum and software. Algorithms have been developed in order to register 3-D  
7 depth information for the stereoscopic images and estimate some reposition values from  
8 them. A user graphical interface is developed as a practical tool to select the desired  
9 points and to display the results.

10 The stereo processing is implemented by three main steps [14]:

- 11 i. Identify correlation between image features in different views of the scene,
- 12 ii. Compute the relative changes between pointed coordinates in each image,
- 13 iii. By applying the camera geometry, specify the 3-D position of the points relative to  
14 the camera.

### 15 **2.1. Image Acquisition**

16 The image acquisition, defined as retrieving an image from a hardware-based source  
17 such as camera, is always the first step in the image processing. The pre-calibrated  
18 binocular camera (BumbleBee2 - Point Grey Research, Inc.) is used which is aligned in  
19 parallel (with a fixed position) with the baseline of 120 mm and  $1032 \times 776$  maximum  
20 pixels. It has a 6-pin IEEE-1394a OHCI PCI Host Adapter for camera control and video  
21 data transmission. In order to process the acquired images, a specialized software is  
22 developed using Birchfield and Tomasi's pixel by pixel stereo matching algorithm [15].

## 1    **2.2. Disparity Maps**

2        The two image-sensors (cameras) of the binocular stereo vision system reside on the  
3    different horizontal coordinates along the same line. Thus, any point in the 3-D  
4    projection maps to the two different locations on the image-sensors. The difference  
5    between the coordinates of the same features on the left and right image (Figure 1) will  
6    define the disparity for the any point of the image  $d(P)$ . The computation is done by  
7    the following steps:

8        Disparity for the feature  $A$  is defined as  $d(A) = X(A_{left}) - X(A_{right})$  and the  
9    disparity of point  $B$  will be derived as  $d(B) = X(B_{left}) - X(B_{right})$  where  $X(A_{left})$  is  
10   the  $X$  coordinate of the point  $A_{left}$  [14].

11       The images captured from the two horizontally displaced camera positions produce  
12   different perspectives of the same scene, which helps in calculating the difference in  
13   relative displacement of the objects in the scene. This relative displacement is referred  
14   to as disparity [16]. The computation of the disparity map as shown in Figure 2a is a  
15   key step to obtain the depth information in the form of a 3-D depth map as shown in  
16   Figure 2b. The Sum of Absolute Differences Correlation method of stereo vision is used  
17   to calculate disparity (1).

18       The approach is led by following processes:

- 19        i. Fetch a pixel from the right image,
- 20        ii. From the left image find a neighborhood of the given right image,
- 21        iii. Compare this neighborhood to a number of neighborhoods along the same row,
- 22        iv. Choose the best match for disparity map.

1 According to the following (1) the comparisons of neighborhoods or masks are  
 2 computed [14]:

$$3 \min_{d=d_{min}}^{d_{max}} \left( \sum_{i=-\frac{m}{2}}^{\frac{m}{2}} \left( \sum_{j=-\frac{m}{2}}^{\frac{m}{2}} \left( |I_{right}[x+i][y+j] - I_{left}[x+i+d][y+j]| \right) \right) \right) \quad (1)$$

4 where  $d_{min}$  and  $d_{max}$  are the minimum and the maximum disparities of  $d$ ,  $m$  is the  
 5 mask size,  $I_{right}$  and  $I_{left}$  are the right and left images,  $x$  and  $y$  are the points'  
 6 coordinates in images [15].

### 7 **2.3. The Computation of the 3-D Coordinates**

8 In this study, the 3-D depth information about the object is constructed via the stereo  
 9 triangulation principle which is based on the difference of an object's location in two  
 10 images because of the changed view of the perspective. One of the key elements in 3-D  
 11 algorithms is to convert image values (in the pixel space) into the real world Cartesian  
 12 coordinates, accurately (Figure 3) [6].

13 The triangulation formulation is based on the similarity between the triangles as  
 14 seen from (2), for which all the ratios

$$15 \frac{B}{Z} = \frac{B - (X^l - X^r)}{Z - f} = \frac{X^l - X^r}{f} = \frac{d}{f} \quad (2)$$

16 are equal.

17 This leads to the following formulation to calculate the distance  $Z$ , where  $d$  (  
 18  $d = X^l - X^r$ ) is the disparity,  $f$  is the focal length,  $B$  is the baseline,  $X^l$  is the  
 19 column position information on the left image of the measured object  $P$  as shown in  
 20 Figure 3a. Similarly,  $X^r$  is the column position information on the right image of the

1 measured object  $P$ . Once the image of the 3-D depth map is obtained, the depth  
2 measurements are carried out as seen from the following (3);

$$3 \quad \frac{B}{Z} = \frac{d}{f} \rightarrow Z = f \frac{B}{d} \quad (3)$$

4 The baseline  $B$  is defined as the distance between the two camera centers. The focal  
5 length  $f$  is predefined by the employed camera. The accuracy of the system increases  
6 with increasing the baseline ( $B$ ) due to the limitations on the camera resolution for a  
7 fixed distance [17]. Figure 3b shows the relationship between the distance and the  
8 disparity.

9 After  $Z$  is determined,  $X$  and  $Y$  can be calculated using the usual projective camera  
10 by the (4) and (5):

$$11 \quad X = u \frac{Z}{f} \quad (4)$$

$$12 \quad Y = v \frac{Z}{f} \quad (5)$$

13 where  $u$  and  $v$  are the pixel location in the 2-D image.  $X$ ,  $Y$  and  $Z$  values are the real  
14 3-D positions.

15 Finally, a complete image of real 3-D depth map (Figure 2b) can be constructed  
16 from image of the disparity map (Figure 2a).  $X$ ,  $Y$  and  $Z$  movement information of final  
17 locations of upper and lower jaws is reported to the surgeon through a developed user  
18 interface software.

### 19 **3. Experimental Setup and Measurements**

20 This part, first, explains the preparation of the dental plaster model and continues  
21 with the image rotation, segmentation and ends with the distance calculation. Figure 4  
22 shows the articulator (SAM 3 made by SAM Präzisionstechnik GmbH) used in this

1 study that has similar functionality to caliper and is utilized to calculate the movement  
2 by transferring the position of the patient's jaw, teeth and the face in a 3-D space.

### 3 **3.1. The Dental Plaster Model**

4 In the orthognathic surgery, preliminary surgical plans are designed through  
5 building the jaw models from the molded dental plasters of the upper and the lower  
6 teeth. The performance of the developed binocular stereo vision system in this study,  
7 will be compared to the conventional dental plaster models to prove the new concept.

8 As shown in Figure 5a, first of all, the patients` lower and upper jaw plaster models  
9 are manufactured by using a device called articulator. Before the operation, the position  
10 of upper and lower-jaw-teeth of the patient is closed. Then, the positioning of teeth of  
11 the closed jaws are marked in red ink by the dental surgeon. Similarly, the expected  
12 closed teeth positions after the correction operation are marked. Finally, the difference  
13 between the positions is determined in mm. These positions are shown in Figure 5b and  
14 Figure 5c. To improve the results, measurements are realized three times for each closed  
15 positions of the teeth before and after operation. Eventually, the final value that will be  
16 considered in the operation is based on the average of three independent measurements.

17 The X, Y, Z positions of all the marked teeth (Figure 6) of the patient`s upper and  
18 lower jaws are measured manually with a mechanical compass by the dental surgeon  
19 (Figure 7a). For this particular patient, there are 14 teeth at lower jaw and 12 at the  
20 upper jaw. All of these 26 teeth`s Cartesian coordinate values are measured and  
21 recorded with respect to a reference point. Similarly, the same measurements are carried  
22 out by the developed binocular stereo vision system (Figure 7b).

23 The measurement results are obtained by using the difference between the initial and  
24 the final positions of the jaws for the calculation of the displacements of the jaws in the



1 Cartesian coordinates. Finally, the measurement error is calculated by comparing the  
2 conventional manual system with the developed binocular stereo vision system.

### 3 **3.2. Image Rotation**

4 During the experimental studies, it has been noticed that the apparatus and the  
5 camera could not be kept the original angular position of their locations. For this reason,  
6 some rotations are observed in the X-Y directions. To prevent the error due to the post-  
7 operation image is rotated in the theta ( $\theta$ ) amount and it is matched with the pre-  
8 operation image (Figure 8).

9 In order to compute a rotation by using matrices, the point ( $x, y$ ) in two dimensions,  
10 (orientation from positive  $x$  to  $y$ ) is written as a vector and then multiplied by a  
11 rotation matrix from the angle  $\theta$  (theta) (6) and (7):

$$12 \quad R(\theta) = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} \quad (6)$$

$$13 \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix} \quad (7)$$

14 where ( $x', y'$ ) are the coordinates of the point after the rotation. The formulation for  $x'$   
15 and  $y'$  can be seen in (8) and (9) [18];

$$16 \quad x' = x.\cos\theta - y.\sin\theta \quad (8)$$

$$17 \quad y' = x.\sin\theta + y.\cos\theta \quad (9)$$

### 18 **3.3. Segmentation**

19 A fundamental operation in digital image processing is color image segmentation  
20 with many variants presented in the literature [19]. In this section, prior to  
21 segmentation, surgeon marks a point on the image. To confirm the stereo vision  
22 system's results, the average value of three manual measurements of the marked points

1 on the teeth are used. The X, Y, Z positions of the marked points are manually  
2 measured with a mechanical compass (caliper) with respect to a reference point. This  
3 operation is repeated three times to minimize measurement errors. In question selected  
4 points are approximately marked on the image as well. There may be some shifts on the  
5 image due to the manual selection of these points in the image which has a low  
6 resolution due to zoom effect.

7 First of all, to eliminate these errors and to identify these points accurately, the  
8 marked area is segmented using a threshold value and the R-G-B (Red- Green- Blue)  
9 values of the neighboring points in the  $9 \times 9$  matrix. If the any one of the R-G-B values  
10 of the examining point is out of range then this point is eliminated and it is not included  
11 in the segmented area. Secondly, after the area segmentation, the geometric center of  
12 this shape is assigned as the marked point for each one of XY, XZ and YZ-plane. In this  
13 way, it is determined with a high precision (Figure 9).

#### 14 **3.4. Distance Calculation**

15 The distances of the new position of the jaws are calculated by obtaining pre-  
16 assigned measurement points (Figure 6) on the pre-operation and the post-operation  
17 images. The positional changes in (X, Y, Z) coordinate values of the marked point can  
18 be formulated in the following (10) – (12):

$$19 \quad \text{Movement}(X) = |PostOperation(X) - PreOperation(X)| \quad (10)$$

$$20 \quad \text{Movement}(Y) = |PostOperation(Y) - PreOperation(Y)| \quad (11)$$

$$21 \quad \text{Movement}(Z) = |PostOperation(Z) - PreOperation(Z)| \quad (12)$$

22 The next section will provide experimental and statistical results.

#### 1    **4. Experimental Results and Analysis**

2        The application does not regard solely the scanning of plaster models, but also for  
3    the real time navigation of the patient. The purpose of using plaster models in this study  
4    is to verify the effectiveness of the proposed method. Thus once it is verified, the model  
5    will also be used in applications like human body. In this study, the stereo camera is  
6    used to take “one single shot” (one stereo pair) of part of teeth and to convert it to 3-D  
7    image. As the image from this viewpoint provides sufficient information to make the  
8    necessary measurements to locate the teeth, a fully 3-D reconstruction process is not  
9    needed. In addition, quality inspection process is sufficient to measure and locate the  
10    teeth from a partly constructed 3-D image.

11        To calculate the approximation error along the (X, Y, Z) coordinates in millimeters  
12    (mm), a movable lower and upper plaster models of jaw of the patient for experiments  
13    are built as shown in Figure 5. The error values are calculated as absolute difference of  
14    accurate measurement values of caliper (manual) and stereo vision system reposition  
15    values ( $|Manual - Stereo Vision|$ ).

16        The coordinate changes of the selected points and the error rates for X, Y and Z axes  
17    are given in Table 1, Table 2 and Table 3, respectively. The measurement errors for the  
18    upper and the lower jaws are provided separately in the given tables. The tooth numbers  
19    are given for the right and the left side of each jaw. The layout of teeth in a jaw is given  
20    in Figure 6. As the acceptable error should be lower than 1 mm, the measurements  
21    clearly suggests the success of the proposed method.

22        The mean error rates for X, Y and Z coordinates are 0.25 mm, 0.26 mm and 0.25  
23    mm, respectively. The standard deviation rates for X, Y and Z coordinates are 0.18, 0.19  
24    and 0.17, respectively. The experimental measurements for X, Y and Z statistically lead

1 to results of  $0.25 \pm 0.18$  mm,  $0.26 \pm 0.19$  mm and  $0.25 \pm 0.17$  mm, respectively. As it is  
2 clearly seen, they are clinically acceptable values ( $< 1.00$  mm) [20].

3 As the acceptable error should be lower than 1.00 mm and dispersion of the  
4 measurement errors do not exceed the target value, the measurements clearly suggest  
5 the success of the stereo vision system. The reasons for the inhomogeneous distribution  
6 of errors may be accumulating from improper lux level of the illumination [14] on the  
7 object and the camera or the user`s carelessness on the activation operation or the  
8 miscalculation distances of 3-D images.

9 In order to further explain the results, the comparisons between the manual  
10 measurements and the stereo vision measurements are illustrated in Figure 10. The  
11 correlation diagrams show the measurement differences with respect to the  $45^\circ$  diagonal  
12 for each axis. The measurement points along the  $45^\circ$  diagonal show the correct  
13 measurements. The divergence in the line is caused by the measurement error between  
14 the manual and the stereo vision measurement values.

15 In this research study, the Statistical Package for Social Sciences (SPSS) version  
16 21.0 is used for the Cronbach`s alpha reliability analysis of the measurements. The  
17 Cronbach`s alpha ( $\alpha$ ) reliability analysis [21] is used to measure the consistency level  
18 statistically. Table 4 shows the consistency level of a measurement. Higher alpha values  
19 indicate that measurements are acceptable whereas lower alpha values indicate that  
20 measurements are unacceptable ( $\alpha < 0.5$ ). The results of analysis are summarized in  
21 Table 5. As observed from Table 4 and Table 5; all alpha values are greater than 0.9  
22 with highest level of consistency.

## 1 **5. Conclusion**

2 This paper focuses on the reduction of measurement errors of the orthognathic  
3 surgery based on the binocular stereo vision. As a case study, the proposed method  
4 applied to be used by dental surgeons. The proposed method improves the precision by  
5 using the binocular stereo vision technology and satisfies the surgical operation  
6 environment in the range of 600 – 750 mm. The results show a high positioning  
7 accuracy of measurements between the post-operation and the pre-operation  
8 measurement points. Cronbach’s alpha reliability results are all favorable. Finally, the  
9 results in 3-D depth measurements show that binocular stereo vision can be reliably  
10 used to reduce measurements error as an alternative method in the orthognathic surgery.  
11 As a future study, 3-D printed and coordinate measurement machine (CMM) models  
12 would be applied to verify the correctness and efficiency of the proposed method.  
13 Furthermore, as the accuracy is the main concern of this case study, recently developed  
14 stereo vision algorithms would be applied in order to obtain better measurements. The  
15 ultimate purpose of this study is in-vivo binocular stereo vision measurement to be used  
16 in surgical operational environment. Nevertheless, there are some difficulties to be  
17 addressed such as the proper determination of measurement location points including  
18 reference point on real jaws and positioning of binocular stereo cameras across patient’s  
19 face to measure the precise displacement of jaw(s). In addition, the artificial intelligence  
20 methods has great potential to improve the accuracy of measurements and the capability  
21 of instrumentation in many application areas [22]. It is considered that the proposed  
22 approach can be enhanced with artificial intelligence techniques.

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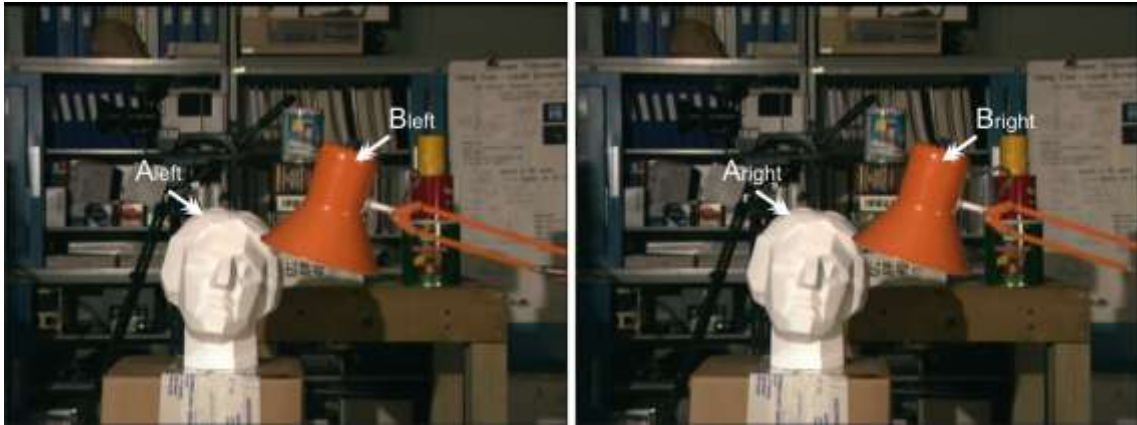
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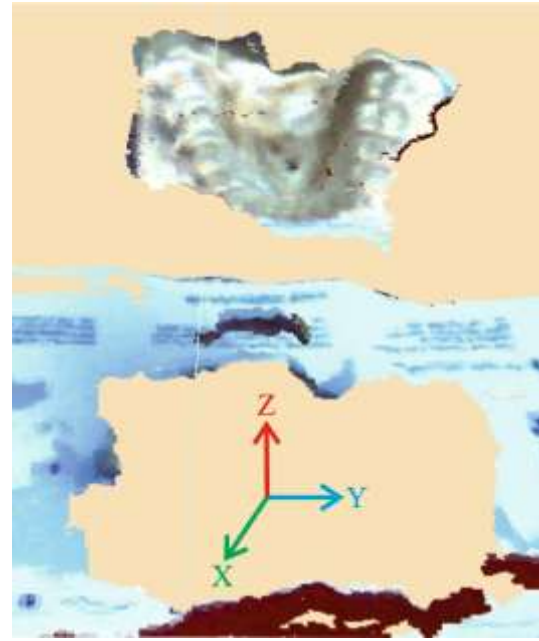
1

2 **Figure 1.** Example of matching points between stereo vision images. The Tsukuba  
3 image is taken from Middlebury Stereo Evaluation (<http://vision.middlebury.edu/stereo>)

4



(a)



(b)

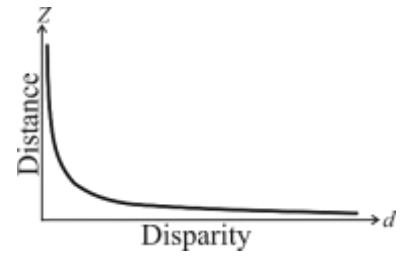
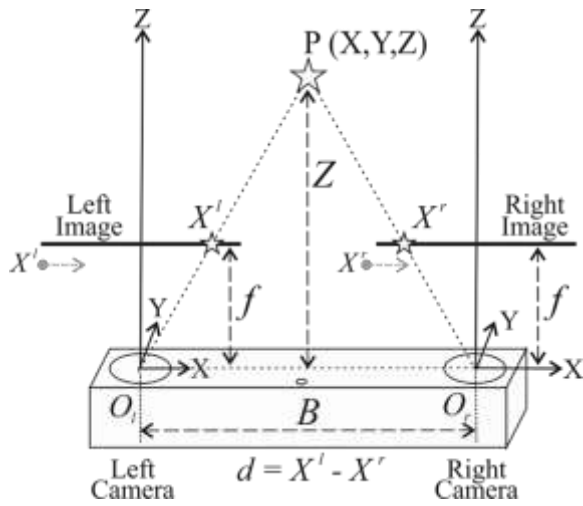
1

2

3 **Figure 2.** Main stages for the depth measurement process: (a) image of disparity map

4 (b) image of 3-D depth map.

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(a)

(b)

**Figure 3.** (a) Basic diagram of a binocular stereo vision system (b) distance versus disparity relationship [6, 7].

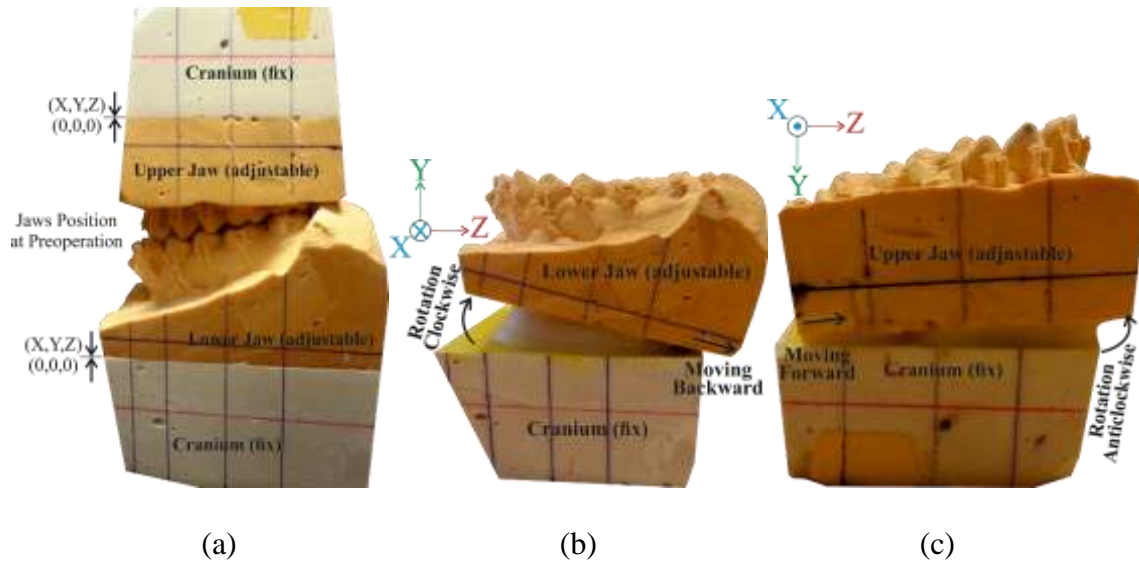


1

2 **Figure 4.** A 3-D dental plaster jaw model installed into an articulator for surgical

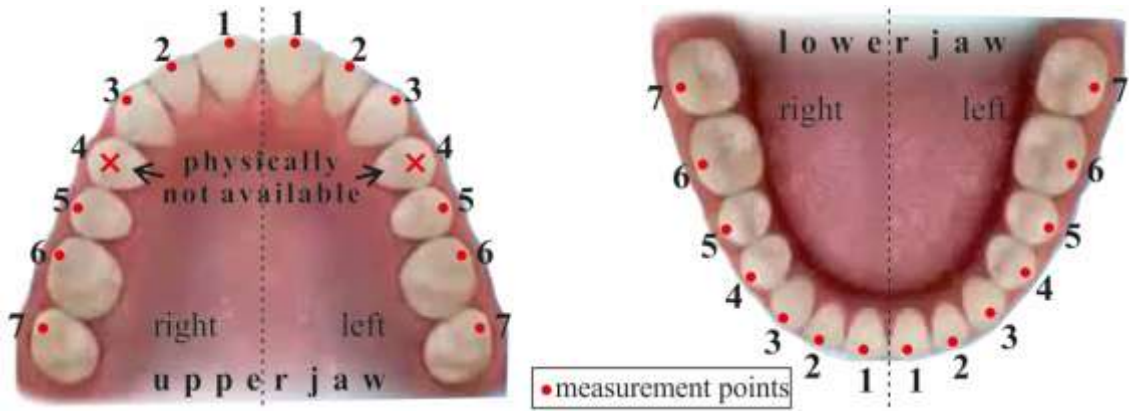
3 planning and simulation.

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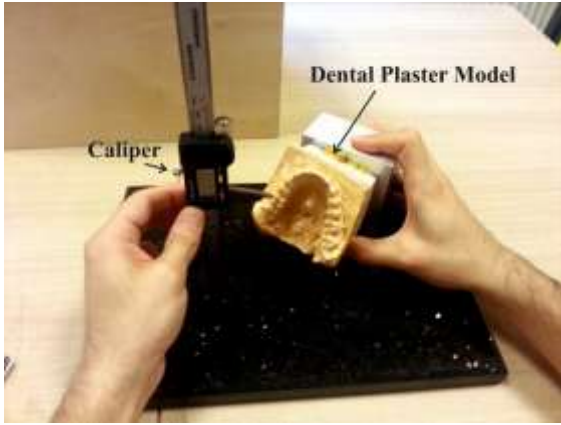
**Figure 5.** (a) Pre-operation dental plaster model (b) post-operation lower jaw positioned to rotation clockwise and moving backward (mandibula) (c) post-operation upper jaw model positioned to rotation anticlockwise and moving forward (maxilla).



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2 **Figure 6.** Upper and lower jaw measurement location points.

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(a)

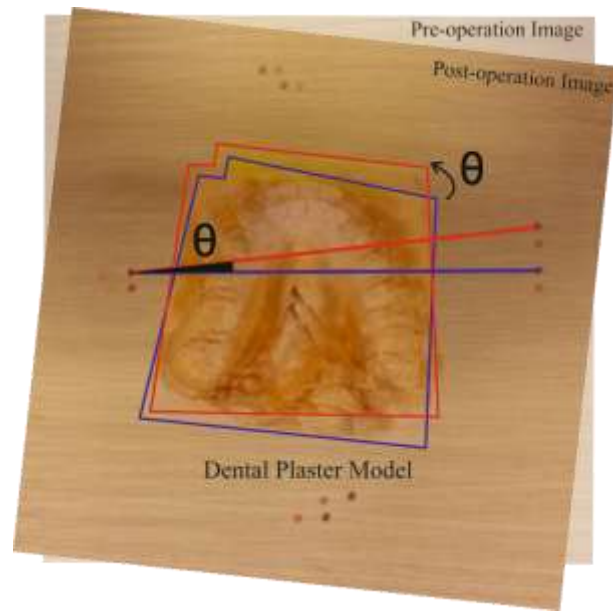
(b)

3

**Figure 7.** (a) Manual and (b) stereo vision measurements.

4

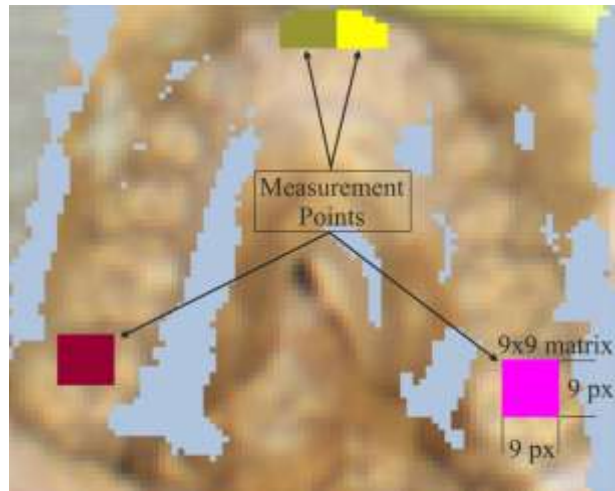




1

2 **Figure 8.** Dental plaster model image rotation.

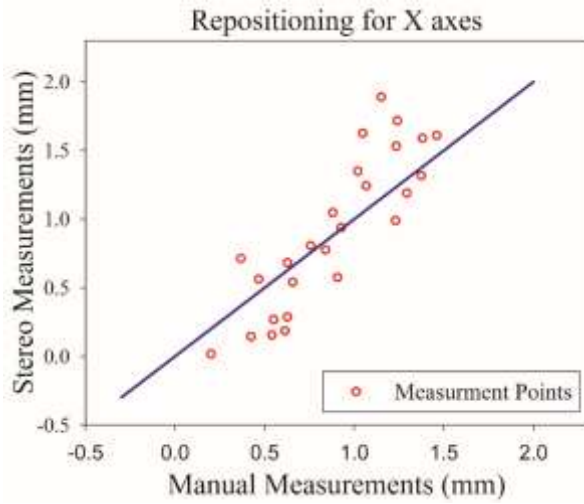
3



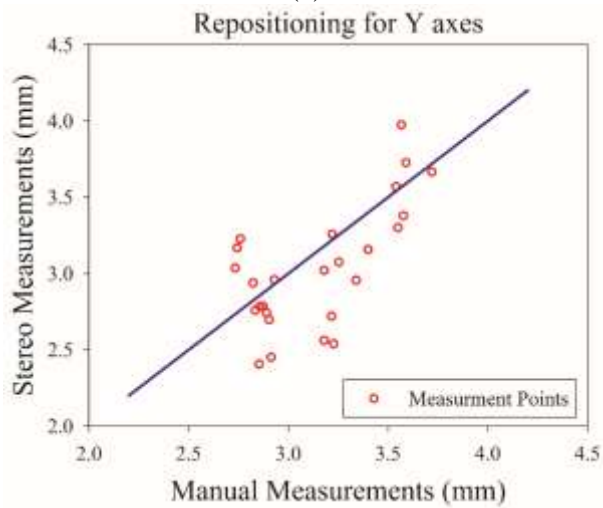
1

2 **Figure 9.** Segmentation.

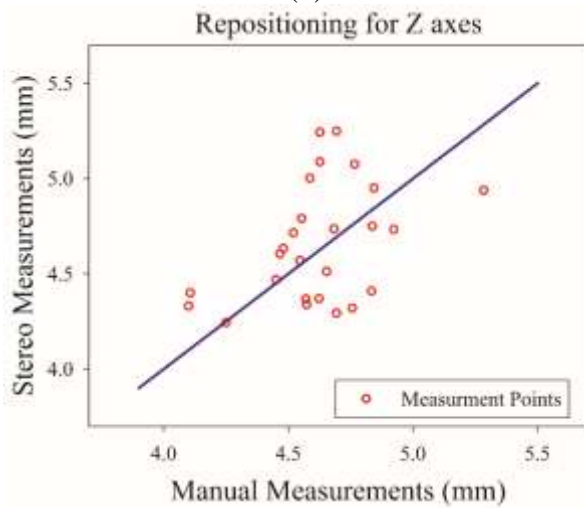
3



(a)



(b)



(c)

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7 **Figure 10.** Stereo measurements compared to manual measurements for the  
8 repositioning of (a) X, (b) Y and (c) Z axes.

1 **Table 1.** Repositioning experimental results for X axes (transversal) coordinates

Exp.	Upper Jaw													Mean Err.	$\sigma$		
	Right						Left										
Tooth No	7	6	5	4*	3	2	1	1	2	3	4*	5	6	7			
X	Man.	0.93	0.63	0.91		0.37	0.66	0.20	0.42	0.54	0.61		0.47	0.55	0.63		
	Str. Vis.	0.94	0.68	0.58		0.71	0.54	0.02	0.14	0.16	0.19		0.56	0.27	0.29		
	Err.	0.01	0.05	0.33		0.34	0.12	0.18	0.28	0.39	0.42		0.09	0.28	0.34		
Exp.	Lower Jaw													0.25	0.18		
Tooth No	7	6	5	4	3	2	1	1	2	3	4	5	6			7	
X	Man.	1.37	1.29	0.88	1.23	1.38	0.84	1.23	1.46	1.05	1.24	1.15	1.07	1.02	0.76		
	Str. Vis.	1.32	1.19	1.05	0.99	1.59	0.78	1.53	1.61	1.63	1.72	1.89	1.24	1.35	0.81		
	Err.	0.05	0.10	0.17	0.24	0.21	0.06	0.30	0.15	0.58	0.48	0.74	0.17	0.33	0.05		

\* = Physically not available,  $\sigma$  = Standard Deviation, Unit = millimeter (mm),  
 Man. = Manual, Str. Vis. = Stereo Vision, Err. = Error, Exp. = Experiments.

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1 **Table 2.** Repositioning experimental results for Y axes (vertical) coordinates

		Upper Jaw													Mean Err.	$\sigma$
Exp.		Right						Left								
Y	Tooth No	7	6	5	4*	3	2	1	1	2	3	4*	5	6	7	
	Man.	2.93	2.87	2.91		2.82	2.85	2.73	2.76	2.74	2.83		2.89	2.86	2.90	
	Str. Vis.	2.96	2.79	2.45		2.94	2.41	3.04	3.23	3.17	2.76		2.74	2.78	2.70	
	Err.	0.03	0.08	0.46		0.12	0.44	0.31	0.47	0.43	0.07		0.15	0.08	0.20	
		Lower Jaw													0.26	0.19
Exp.		Right						Left								
Y	Tooth No	7	6	5	4	3	2	1	1	2	3	4	5	6	7	
	Man.	3.59	3.57	3.55	3.34	3.25	3.23	3.22	3.18	3.18	3.22	3.40	3.54	3.58	3.72	
	Str. Vis.	3.73	3.98	3.30	2.96	3.08	2.54	2.72	3.02	2.56	3.26	3.16	3.57	3.38	3.67	
	Err.	0.14	0.41	0.25	0.38	0.17	0.69	0.50	0.16	0.62	0.04	0.24	0.03	0.20	0.05	

\* = Physically not available,  $\sigma$  = Standard Deviation, Unit = millimeter (mm),  
 Man. = Manual, Str. Vis. = Stereo Vision, Err. = Error, Exp. = Experiments.

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1 **Table 3.** Repositioning experimental results for Z axes (sagittal) coordinates

		Upper Jaw													Mean Error (mm)	$\sigma$
Exp.		Right						Left								
Tooth No		7	6	5	4*	3	2	1	1	2	3	4*	5	6	7	
	<b>Man.</b>	4.63	4.77	4.83		4.92	4.84	5.28	4.52	4.48	4.47		4.25	4.11	4.10	
<b>Z</b>	<b>Str. Vis.</b>	5.24	5.08	4.41		4.73	4.75	4.94	4.72	4.63	4.61		4.24	4.40	4.33	
	<b>Err.</b>	0.62	0.31	0.42		0.19	0.09	0.34	0.20	0.15	0.14		0.01	0.29	0.23	
		Lower Jaw													0.25	0.17
Exp.		Right						Left								
Tooth No		7	6	5	4	3	2	1	1	2	3	4	5	6	7	
	<b>Man.</b>	4.55	4.55	4.69	4.57	4.59	4.84	4.68	4.65	4.45	4.62	4.69	4.76	4.63	4.57	
<b>Z</b>	<b>Str. Vis.</b>	4.79	4.57	5.25	4.34	5.00	4.95	4.74	4.51	4.47	4.37	4.29	4.32	5.09	4.37	
	<b>Err.</b>	0.24	0.02	0.56	0.23	0.42	0.11	0.05	0.14	0.02	0.25	0.40	0.44	0.46	0.20	

\* = Physically not available,  $\sigma$  = Standard Deviation, Unit = millimeter (mm),

Man. = Manual, Str. Vis. = Stereo Vision, Err. = Error, Exp. = Experiments.

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1 **Table 4.** The consistency levels of the Cronbach's Alpha

<b>Cronbach's Alpha</b>	<b>Internal Consistency</b>
$\alpha \geq 0.9$	Excellent (High-Stakes Testing)
$0.7 \leq \alpha < 0.9$	Good (Low-Stakes Testing)
$0.6 \leq \alpha < 0.7$	Acceptable
$0.5 \leq \alpha < 0.6$	Poor
$\alpha < 0.5$	Unacceptable

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1 **Table 5.** Cronbach's Alpha ( $\alpha$ ) reliability analysis results

<b>Cronbach's Alpha (<math>\alpha</math>) Reliability Analysis</b>	<b>Manual Measurements</b>	<b>Stereo Vision Measurements</b>	<b>Manual + Stereo Vision Measurements</b>
<b>X axes (Transversal)</b>	0.976	0.979	0.977
<b>Y axes (Vertical)</b>	0.981	0.974	0.978
<b>Z axes (Sagittal)</b>	0.907	0.901	0.904

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