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Broken Rotor Bar Detection in Three-phase Induction Motor Based on Multinomial Identity of Stator Current

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KEYWORDS

Signal-based fault detection;
Motor Current Signature Analysis (MCSA);
Broken Rotor Bar (BRB);
Squirrel Cage Induction Motor (SQIM);
Fast Fourier Transform (FFT).

Abstract. Motor current signature analysis is cited in many articles to detect the rotor bar fracture. Because of the small amplitude at the fault frequency relative to the main frequency amplitude, the former cannot be easily distinguished from the latter. As a solution, a method based on the algebraic identity of trinomial expansion of the stator current is proposed which enables us to display the difference between the frequency of the fault signature and the base frequency. In addition, the components at unwanted frequencies are attenuated using a low-pass filter. After that, frequency weighting techniques are used to magnify the component at the target frequency compared to the lower frequencies. Indeed, a weighting method based on differentiation is used, and another method based on convolution is proposed as tools to enhance the clarity of the frequency spectrum display for a broken rotor bar. To validate the proposed methods, they are examined on the laboratory data obtained from three different operating conditions, including the direct online start, the direct torque control, and the scalar control, and the results show the ability of the proposed methods in fault detection of an induction motor.

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1. Introduction

Squirrel cage induction motors (SQIM) are widely used in various industries [1–3]. In industries, where uninterrupted motor operation is necessary, timely detection of rotor faults is important, as these faults account for approximately 10% of all motor faults. This issue is especially critical in harsh environments, such as oil and gas environments, traction, and mines, where motor failures can result in heavy process losses [4, 5].

Over the past few years, the use of induction motors in the electric vehicle (EV) industry has become increasingly widespread. The electric motor is a crucial component of an EV as it converts electric energy to mechanical energy [6]. Therefore, any failure in any of its components can directly impact the reliability of the powertrain and the safety of passengers [7, 8]. As a result, it is crucial to develop an electric motor that enhances the efficiency and performance of EVs [9, 10]. Among the various types of electric motors used in EVs, the induction motor is more effective and economical than others due to its reliability, simple mechanical design, and effective field-weakening characteristics [9].

To increase the reliability of IMs used in EVs, researchers have focused on different fault diagnosis methods in the past decade, in line with the growth of the EV industry. These methods are aimed at identifying and diagnosing faults in IMs before they lead to motor failure, and include techniques such as vibration analysis, and motor current signature analysis (MCSA) [9, 11–19]. By implementing these fault diagnosis methods, the reliability of induction motors can be enhanced, thereby improving the overall performance and safety of EVs.

The broken rotor bar (BRB) is a type of rotor fault that can cause damage to other parts of the motor, including the winding, bearings, and mechanical parts. In addition, BRBs can lead to torque and speed pulsation and create harmonics in the current, air-gap flux, and induced voltage of stray flux [4, 20, 21]. A. H. Bonnett and C. Yung [22] listed the distribution of induction motor faults as bearing (69%), stator windings (21%), rotor bar (7%), and shaft/coupling (3%). Therefore, given that the BRB of SQIM is a common type of rotor defect [23], this article will focus on the diagnosis of BRBs.

Generally, there are three groups of fault detection methods [24–26]:

1. Signal-based methods [25, 27, 28]
2. Model-based methods [25, 29]
3. Knowledge-based methods [26, 30, 31]

Model-based approaches require a precise and accurate mathematical model of the motor, and knowledge-based approaches have low accuracy in transient conditions and require different and high-volume data for diagnosing different motors [32]. Therefore, signal-based methods are of great interest for fault detection in electric motors.

Any type of faults affects the general signals of the motor, such as current, torque, speed, and voltage, in a specific way and creates special harmonics in them. Most of the existing electrical condition monitoring and fault detection methods are based on the analysis of the measured output signals [4, 33, 34]. To detect the fault based on the signal, three steps are usually taken:

1. acquiring a suitable signal to detect the fault,
2. using the proper method to analyze the signal,
3. determining the index to make the decision about the faulty or healthy condition.

According to articles analyzing various types of motor output signals, research on fault diagnosis includes MCSA, methods based on terminal voltage analysis, air gap torque analysis, impedance sequence component analysis, leakage flux measurement, infrared detection, stray flux detection, vibration analysis, thermal analysis, acoustic analysis, electromagnetic field interference, and more [35–37]. Among these methods, MCSA is utilized in this paper due to its non-destructive nature, compatibility with several signal processing tools, and being a spectral analysis method that is commonly used for online and remote monitoring of induction motors in industrial environments [20, 38, 39]. The following are some MCSA methods: frequency spectral analysis, current envelope analysis method, components of negative, positive, and zero current sequences, and Park's vector representation of three-phase current and Clark transformation [5, 34, 40].

Although positive, negative, and zero sequence components of current or Park and Clark vector transformations can be used for MCSA, they require sampling of three-phase current [41], which increases the cost compared to single-phase current sampling, and there is no indicator to recognize the fault type in many cases. In the current envelope analysis method, there is a challenge to produce a suitable envelope without auxiliary processing tools, and it does not show clear results for fault detection. A common and simple frequency-domain method for detecting BRB is applying the fast Fourier transform (FFT) on the stator current and then analyzing the produced spectrum [4, 32]. However, the sampled current is almost always accompanied by noise, and for motors that operate at small slips, the

fault frequency is hidden in the shadow of the base frequency. This means that base frequency leakage can mask fault frequencies, making rotor fault detection difficult, and motor damage may progress to severe damage [42]. Therefore, direct application of frequency spectral analysis and FFT method on the stator current will not have a useful and usable result and requires initiatives and auxiliary processing tools.

In order to increase the slip and distinguish between the fault frequency and the base frequency, a rotor breakage detection test has been performed in [43], which is not in the steady state motor operation mode. In [44], a normalized energy operator in the frequency domain is proposed for BRB fault detection, and energy operators have also been used to diagnose the broken rotor bar in some other papers [45]. Among the different methods, those that can be practical in the condition of high current noise are preferred, and in order to reduce the cost, sampling the current of one phase is preferable. Therefore, in this paper, we sample the current of one phase of the stator and use the sum square identity along with methods to remove unnecessary frequency components from the current signal. Moreover, to elevate the peaks at the fault frequency a weighting method based on the differentiating is used and a method based on convolution is proposed.

In other words, concerning the BRB fault detection the article proposes:

- applying the sum square identity, to separate the fault related component from the other unwanted components,
- elevating the peak at the fault frequency using the proposed method based on the convolution.

Different signal processing tools have been utilized in various studies. Typically, these tools can be categorized into three groups: time domain, frequency domain, and time-frequency domain [46]. Time domain indicators such as mean, median, peak, kurtosis, and skewness are less commonly used to detect BRB faults. Instead, some research studies have utilized time-frequency decomposition tools to identify fault components and harmonics [47, 48]. For example, the Hilbert-Huang transform is often used for analyzing non-linear and non-stationary signals, but identifying the signal with the fault frequency can be challenging [49]. Another commonly used time-frequency domain transform is the wavelet transform. In some applications, wavelet transform is used as a filter, and simple filters can also be effective. In some articles, wavelet transform has been used for time-frequency analysis of non-stationary signals [50]. In other cases, the short-time Fourier transform (STFT) has also been used [43], but it has lower ability compared to the wavelet transform.

Other methods belonging to the time-frequency signal processing tools include the adaptive slope transform, the Multiple Signal Classification (MUSIC) algorithm, the Wigner-Ville distribution, and the Choi-William distribution [51, 52]. While fault detection and evaluation in the time-frequency domain may require a skilled user with powerful pattern recognition techniques, it also takes more time for investigation and a relatively long start-up time.

In this paper, FFT is used for BRB fault detection due to its high speed and ease of analyzing the FFT spectrum results to identify the dominant frequency of the BRB. Furthermore, FFT is widely applied in other articles [53, 54] and provides the possibility to define an index for the detection of the severity of the fault and its type.

The rest of the paper is structured as follows: In Section 2, the methodology used in this study is explained. Sections 2.1 and 2.2 are dedicated to techniques for elevating the peak at the fault frequency, using derivation and convolution, respectively. Section 3 presents the benchmark and experimental results and the comparison between different methods is presented in Section 3.3. The paper concludes with a summary in Section 4.

2. Methodology

The fault-related component obtained through direct FFT analysis of the current signal is often characterized by a much lower amplitude when compared to the fundamental frequency component (as illustrated in Figure 1). Furthermore, given that the fault frequency is usually very close to the fundamental frequency, the latter can mask the former, particularly during low-slip operations. In other words, within the FFT spectrum, the fault frequency spectrum can be concealed within the shadow of the fundamental frequency spectrum, thus rendering the fault undetectable [55]. To overcome this issue, it is crucial to attenuate the fundamental frequency component while magnifying the fault frequency component to distinguish the fault frequency in the spectrum. To this end, one possible solution is to calculate the difference between the fault frequency and the base frequency. In this context, we propose a mathematical method that is based on a particular identity, which we present in the following.

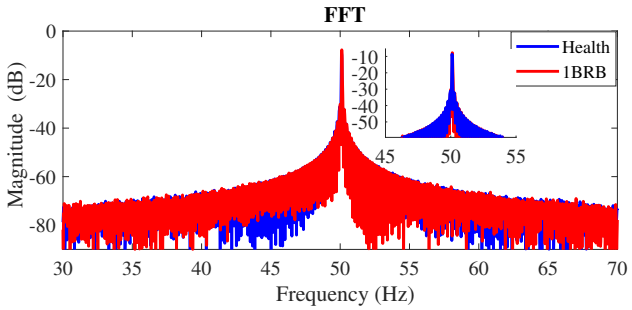


Figure 1. Direct application of FFT on stator current and comparison of the healthy rotor and one broken bar in DTC operating condition and low load.

The frequencies resulting from the BRB fault [56] are as Relation (1).

$$f_{brb} = (1 \pm 2ks)f_s = f_s \pm kf_f \tag{1}$$

where f_{brb} is the fault frequency of broken rotor bar, $k = 1, 2, 3, \ldots,$ s is slip, f_f is the difference between the base frequency and the fault frequency, which introduces the fault, and f_s is the fundamental (base) frequency. A fault detection method is proposed in which the fault signature concealed by the fundamental frequency component is detected using the trinomial expansion. To facilitate understanding of this approach, the identity of the trinomial expansion is presented in Relation (2).

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca \tag{2}$$

where a, b, c are either numbers or variables. Considering an amplitude modulation caused by the fault and referring to Relation (1) with $k = 1$, the stator current can be expressed as following [57]:

$$\begin{aligned} x(t) &= \big(1 + Mcos(2\pi f_f t)\big) \cdot Acos(2\pi f_s t) \\ &= Acos(2\pi f_s t) + \frac{AM}{2} cos\big(2\pi(f_s - f_f)t\big) \\ &+ \frac{AM}{2} cos\big(2\pi(f_s + f_f)t\big) \end{aligned} \tag{3a}$$

where A and M are the fundamental current amplitude and the modulation depth, respectively. In cases of SQIM with rotor bar breakage, two sideband frequencies related to the rotor bar breakage will appear in the stator current signal spectrum, around the fundamental frequency (f_s). These frequencies are denoted by $f_2(= f_s - f_f)$ and $f_3(= f_s + f_f)$, and they are both situated in proximity to f_s. Let us consider Relation (3a) as a signal comprising three sinusoidal terms :

$$x(t) = a_1 cos\big(2\pi f_1 t\big) + a_2 cos\big(2\pi f_2 t\big) + a_3 cos\big(2\pi f_3 t\big) \tag{3b}$$

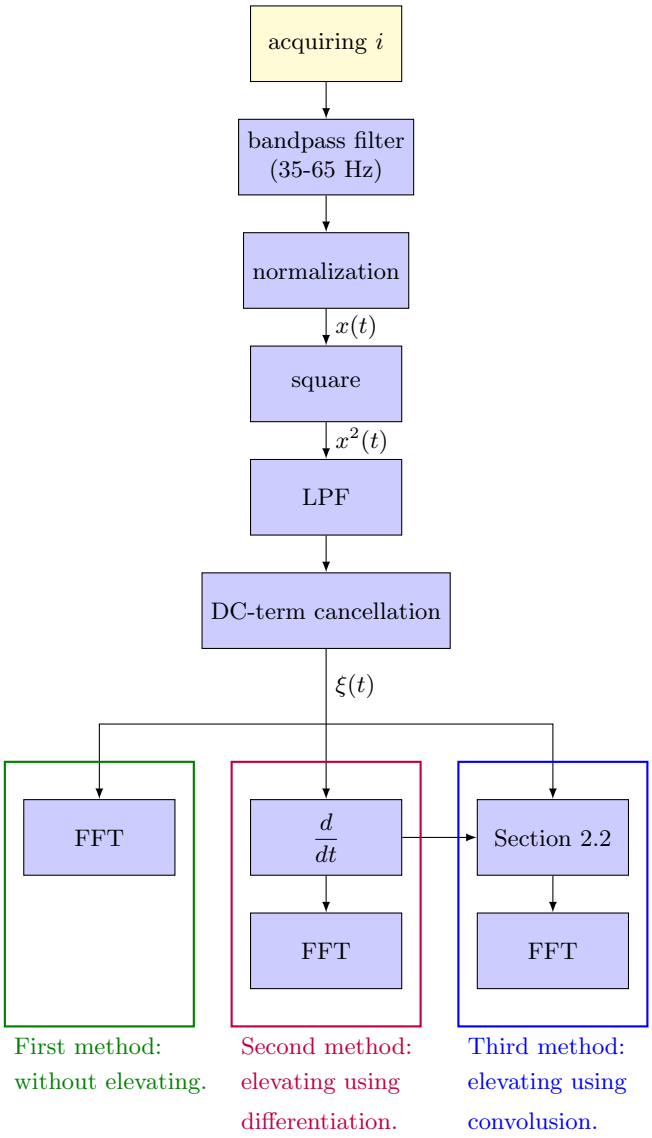


Figure 2. The flowchart of the proposed methods (LPF: low-pass filter, FFT: fast Fourier transform).

Here $f_1 = f_s$, $a_1 = A$, and $a_2 = a_3 = \frac{AM}{2}$. It is known that $cos\big(2\pi(f_3 - f_1)t\big) = cos\big(2\pi(f_1 - f_2)t\big)$ and $a_2 \cong a_3$. Using the trigonometric relations and neglecting the term of $2a_2a_3cos(2\pi f_2 t)cos(2\pi f_3 t)$, due to its very small amplitude, yields:

Table 1. Analysis of terms and frequency components of Relation (4)

Term	**Frequency**	**Used for fault detection**	**Frequency elimination method**
$a_1^2 cos^2(2\pi f_1 t)$	DC and $2f_s$	no	DC part by removing the average value and $f = 2f_s$ by low pass filter
$a_2^2 cos^2(2\pi f_2 t)$	DC and near $2f_s$	no	DC part by removing the average value and $f \approx 2f_s$ by low pass filter
$a_3^2 cos^2(2\pi f_3 t)$	DC and near $2f_s$	no	DC part by removing the average value and $f \approx 2f_s$ by low pass filter
$2a_1 a_2 cos\big(2\pi(f_1 - f_2)t\big)$	Difference of base and fault frequencies	yes	needed for fault diagnosis
$a_1 a_2 cos\big(2\pi(f_1 + f_2)t\big)$	nearly $2f_s$	no	$f \approx 2f_s$ by low pass filter
$a_1 a_3 cos\big(2\pi(f_1 + f_3)t\big)$	nearly $2f_s$	no	$f \approx 2f_s$ by low pass filter

$$x^2(t) \cong a_1^2 cos^2(2\pi f_1 t) + a_2^2 cos^2(2\pi f_2 t) + a_3^2 cos^2(2\pi f_3 t) + 2a_1 a_2 cos(2\pi(f_1 - f_2)t) + a_1 a_2 \big[cos(2\pi\big(f_1 + f_2)t\big) + cos\big(2\pi(f_1 + f_3)t\big)\big] \quad (4)$$

Thus, decomposing Relation (4) yields one component at DC and five terms with frequencies twice or nearly twice the base frequency ($2f_s$) and one component at the difference of the base frequency and the fault frequency or at $f_1 - f_2 (= f_f = 2sf_s)$. Five components among them are filtered out and the DC-term is removed by subtracting the mean value from the signal, and only the component at the frequency of $f_1 - f_2$ is used in the proposed fault detection method. Table 1 shows all of these components and indicates that which of them are going to be used in the proposed fault detection technique. Therefore, what remains is the following signal, which is used to diagnose the faulty motor:

$$\xi(t) = 2a_1 a_2 cos(2\pi(f_1 - f_2)t) \quad (5)$$

To obtain the component at $f_1 - f_2$ the stator current signal is gathered. Then using a band pass filter the component around the base frequency are kept and after normalization the square of the signal ($x^2(t)$) is computed. An low-pass filter (LPF) is used to attenuated the remaining unwanted parts. The cut-off frequency can be tuned at half of the base frequency. The DC component yet remains and it is filtered out by means of DC-term cancellation. The spectrum of the resultant signal is compute through FFT. The flowchart of the proposed technique is shown in Figure 2. By applying the trinomial expansion identity to the stator current signal and subsequently removing unwanted frequencies, a resulting signal can be obtained that contains Relation (5). As mentioned in first method in Figure 2 the component at the differential frequency of this expression can be obtained by using FFT transformation. There are also two other methods in the flowchart which are going to be explained in the following subsections.

2.1. Elevating the peak at the fault frequency using derivation

After differentiating Relation (5), the following equation is obtained, in which the amplitude is weighted by the difference between the fault frequency and the base frequency:

$$\frac{d\xi(t)}{dt} = -4\pi(f_1 - f_2)a_1 a_2 sin\big(2\pi(f_1 - f_2)t\big) \quad (6)$$

This technique elevates the peak at the fault frequency in comparison to the neighboring peaks at lower frequencies, making the fault signature more prominent and facilitating fault detection.

2.2. Elevating the peak at the fault frequency using convolution

The convolution of two time-discrete signals x and y is defined as follows [58]:

$$(x * y)[n] = \sum_{m=-\infty}^{+\infty} x[m] \cdot y[n-m] \tag{7}$$

Based on the convolution theorem, convolution in the time domain corresponds to multiplication in the frequency domain [53, 55, 59].

$$\mathcal{F}\big((x * y)[n]\big) = X(\omega) \cdot Y(\omega) \tag{8}$$

Therefore, by performing the convolution of the $\xi(t)$ and its derivative $\dot{\xi}(t)$ in the time domain while strengthening the fault component amplitude with frequency weighting in the time domain, the fault frequency amplitude is magnified in the frequency domain. Consequently, in the FFT spectrum, the amplitude of the fault frequency is amplified, while the amplitude of the frequency components around the fault frequency is weakened. The block diagram of the proposed method is shown in Figure 3.

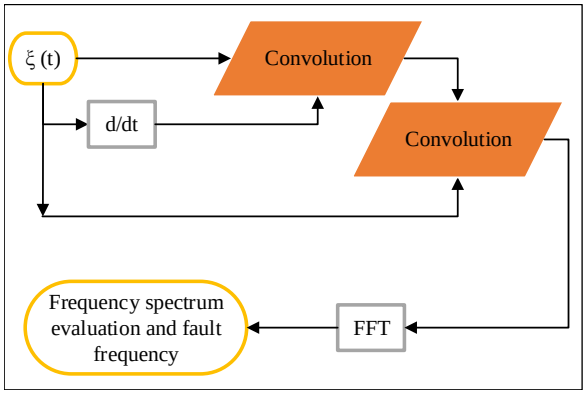


Figure 3. Proposed method for high resolution FFT (fast Fourier transform).

By using this technique, the peak at the fault frequency in the FFT spectrum is more pronounced compared to neighboring peaks. This means that the fault signature becomes more visible in the spectrum with high resolution. Repeating the convolution will increase the visibility in a great extent.

3. Benchmark and experimental results

The characteristics of the motor under examination are presented in Table 2. The experimental setup comprises a 3 kW AC generator, a 1.5 kW induction motor with broken rotor bars, and the corresponding load, a LA55-PSP1 Hall effect current sensor and a DSP, TMS320F28379D and a control drive and a computer. The resolution level of the DSP analog to digital converter is 12 bits. A photo of the setup is illustrated in Figure 4.

Figure 4. The experimental setup and the rotor with two broken bars.

Table 2. The specifications of the experimented motor.

Parameter	Value
Rated Power	1.5 kW
Rated Frequency	50 Hz
Rated Speed	1500 RPM
Efficiency	85.3%
Rotor Bar no.	28
Rated Voltage (Δ, Y)	220/380 V
Rated Current (Δ, Y)	5.7/3.3 A
Power Factor	0.81
Pole no.	4
Air Gap Length	0.25 mm

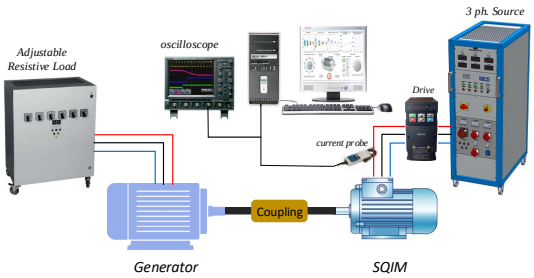


Figure 5. Schematic diagram of the test (SQIM: squirrel cage induction motor).

The proposed methods were tested under three different operating conditions, including direct online start (DOL), direct torque control (DTC), and scalar control. Each operating condition was evaluated under three load levels: light, medium, and heavy (full) loads.

The light load mode represented the condition where no electric load was connected to the generator. In the medium and full load modes, 600 watts and 1200 watts of electric loads were respectively connected to the generator. Accounting for the 80% efficiency of the generator, the load on the motor was 750 watts and 1500 watts for medium and full load modes respectively. The sampling frequency used was 10 kHz. The experimental setup was illustrated in Figure 5.

For instance, in DOL operation mode under the light load condition, the signal to be analyzed is shown in Figure 6. After removing the DC component and the component at frequencies around twice the base frequency ($f = 2f_s$), the resulting signal is used for analysis. The rotor speed in this case is 1493 RPM, and the corresponding slip is $s = 7/1500 = 0.467\%$. The results for three scenarios, including the healthy state, one broken rotor bar, and two broken rotor bars, are depicted in Figure 7.

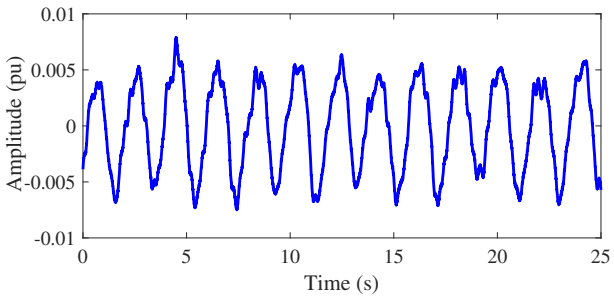


Figure 6. Sample output signal containing Relation (5) in DOL operating mode under the light load.

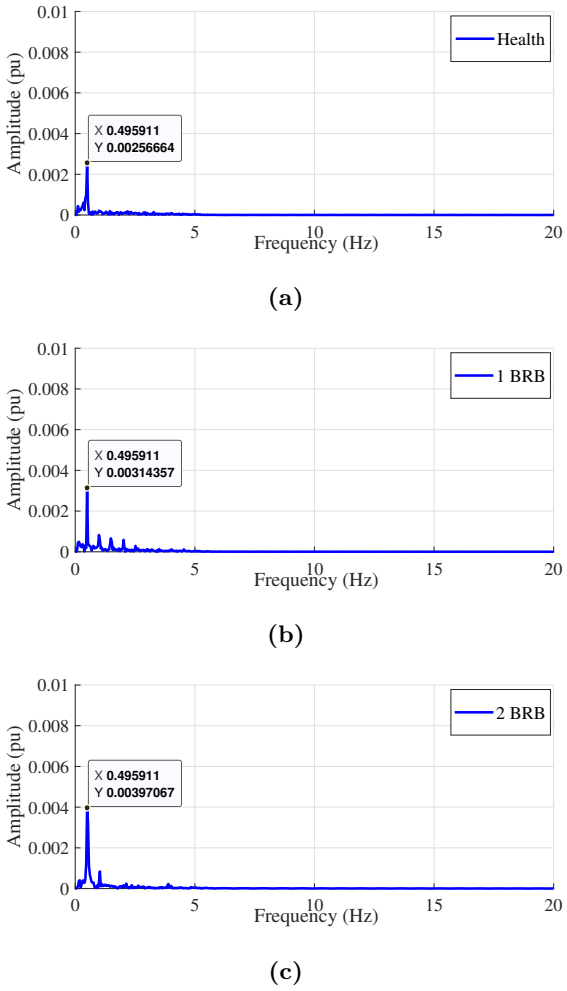
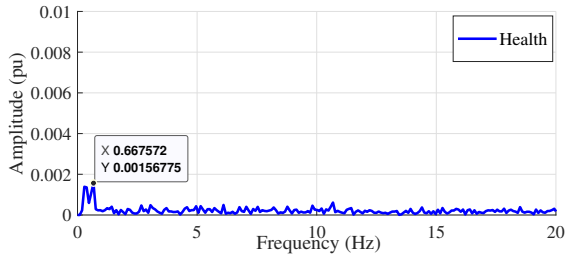


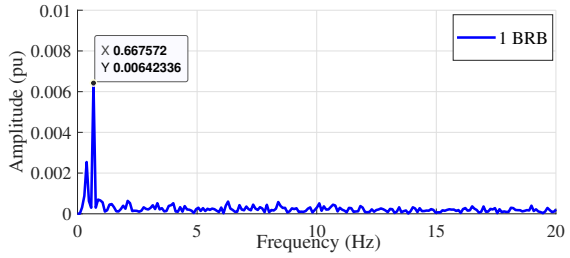
Figure 7. Produced spectrum, under the light load mode in the case of DOL operating conditions, with (a) healthy rotor, (b) one broken bar, and (c) two broken bars.

Figure 8 illustrates the analysis results for the case of DTC under the light load operation mode, where the rotor speed is 1490 RPM. The analysis was conducted for three scenarios, including the healthy rotor, one broken rotor bar, and two broken rotor bars, and the results are presented in Figure 8.

Figure 9 shows the results for the case of scalar control under the light load mode of operation. In this case the rotor speed is 1492 RPM and the situation of healthy motor, one broken rotor bar and two broken rotor bars are studied.



(a)



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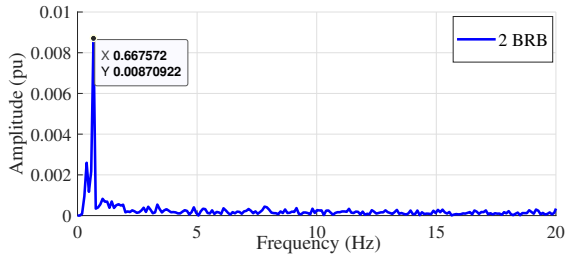
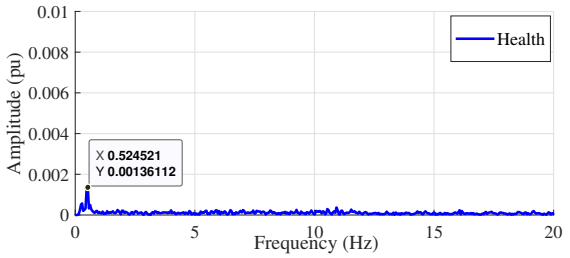
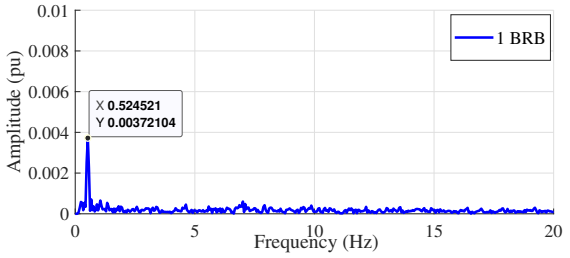


(c)

Figure 8. Produced spectrum, under the light load mode in the case of DTC operating conditions, with (a) healthy rotor, (b) one broken bar, and (c) two broken bars.



(a)



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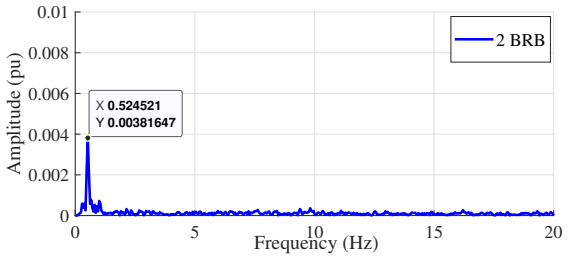


(c)

Figure 9. Produced spectrum, under the light load mode in the case of scalar control, with (a) healthy rotor, (b) one broken bar, and (c) two broken bars.

Table 3 demonstrates that there is a strong correlation between the fault frequencies obtained from Relation (1) and those obtained from the proposed method. Additionally, there is a relationship between the peak values and the number of BRBs, as evidenced by the results presented.

As seen in Table 3, the results are presented for three operational states of the motor including DOL, DTC, and the scalar control. The provided results include the frequency deviation of the fault and the base frequency of the stator current signal in Hz. The fault spectrum amplitude is also given in per-unit. The results are categorized for low, medium, and full load motor conditions, considering motor states with a healthy rotor, one broken bar, and two broken bars. For each load condition, the fault frequency spectrum amplitude increases with the number of broken bars. As the motor load increases, the fault frequency also increases due to increased slip.

3.1. Amplifying peaks using derivation

The results for the DOL operating condition under full load, with one BRB, without frequency weighting and

with frequency weighting through derivation, are depicted in Figure 10. Comparison of Figure 10 (a) and (b) reveals that the differentiating technique increases the ratio of the peak value at the fault frequency relative to the lower frequency region.

Table 3. Summarizing the frequency results obtained by the method (DOL: direct on-line, DTC: direct torque control, BRB: broken rotor bar).

Starting Method	Load Amount	Motor Status	Ampl. (pu)	$F_{mesured}$ (Hz)
DOL	Low	Healthy	0.00256664	0.495911
		1BRB	0.00314357	0.495911
		2BRB	0.00397067	0.495911
	Medium	Healthy	0.00403241	1.15256
		1BRB	0.00546961	1.22071
		2BRB	0.00626237	1.2207
	Full	Healthy	0.00365003	2.32697
		1BRB	0.00383345	2.32697
		2BRB	0.00455207	2.36511
DTC	Low	Healthy	0.00156775	0.667572
		1BRB	0.00642336	0.667572
		2BRB	0.00870922	0.667572
	Medium	Healthy	0.00207091	1.4782
		1BRB	0.00647853	1.4782
		2BRB	0.00825256	1.52588
	Full	Healthy	0.00113611	2.81334
		1BRB	0.00402521	2.81334
		2BRB	0.00514829	2.86102
Scalar	Low	Healthy	0.00136112	0.524521
		1BRB	0.00372104	0.524521
		2BRB	0.00381647	0.524521
	Medium	Healthy	0.0026973	1.19209
		1BRB	0.00603295	1.23978
		2BRB	0.00728799	1.28746
	Full	Healthy	0.0028846	2.38419
		1BRB	0.00459908	2.43187
		2BRB	0.00413	2.47955

3.2. Amplifying peaks using convolution

By using this technique, the peak at the fault frequency in the FFT spectrum is more pronounced compared to neighboring peaks. This means that the fault signature becomes more visible in the spectrum with high resolution. To illustrate, Figure 11 depicts the fault frequency spectrum using the proposed method during DOL operation under full load conditions with a single BRB. Figure 12 illustrates the fault frequency spectrum under light load mode and during DTC operation.

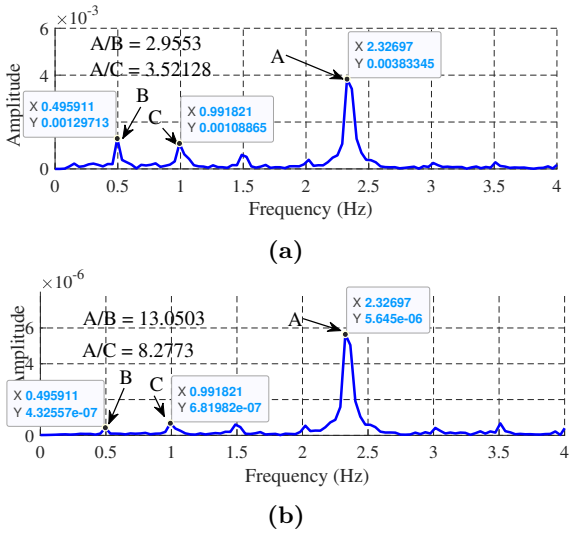


Figure 10. Comparison of fault frequency detection (a) without frequency weighting and (b) with frequency weighting through derivation. Using derivation, the ratio of amplitude at point A (fault frequency) to the amplitude of the neighboring peaks is increased in Figure 10b.

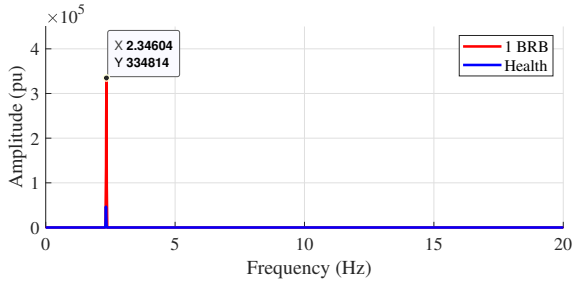


Figure 11. Fault frequency spectrum using third proposed method in DOL operation at full load state and one BRB.

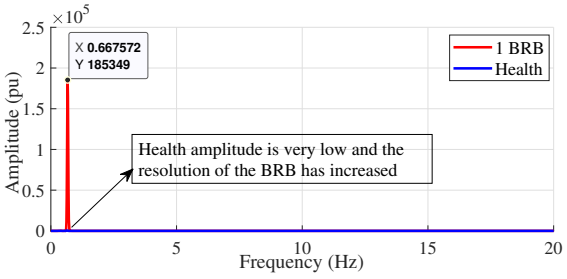


Figure 12. Fault frequency spectrum using third proposed method in DTC operation at light load state and one BRB.

Figure 13 shows the scalar operation mode and light load condition to distinguish the severity of faults with one or two broken rotor bars from the healthy state. The figure illustrates that the proposed method accurately detects the state and severity of faults compared to the healthy state.

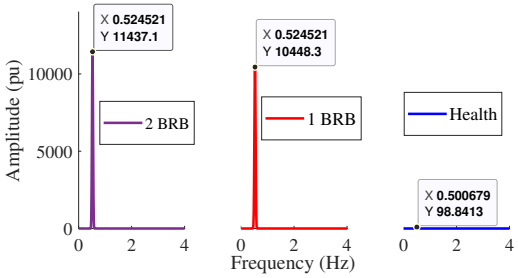
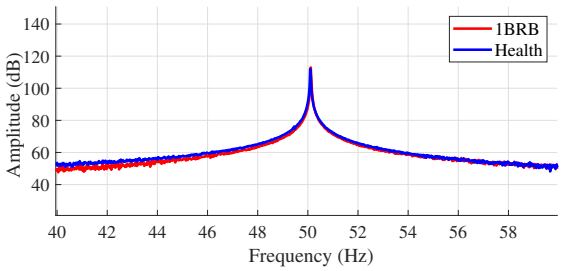


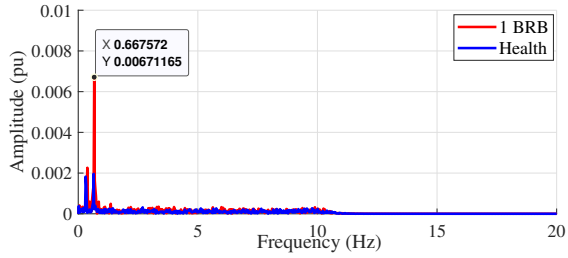
Figure 13. Comparing healthy, one and two broken bars condition in the scalar operation mode and light load (third proposed method).

3.3. Comparison

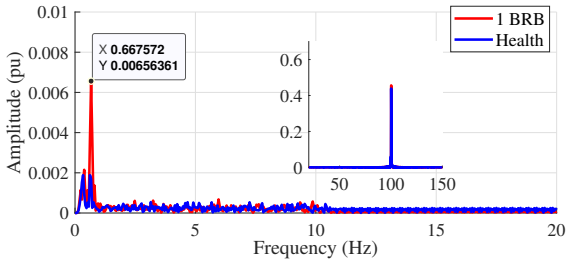
To compare the proposed method with some competitors these methods are used to detect one BRB in the case of DTC and low load. The stator current signal is filtered using BPF. The results of applying FFT on the stator current is shown in Figure 14 (a). As it can be seen differentiating between the healthy and faulty condition is not straightforward. In Figure 14 (b) the results obtained by FFT of envelope of signal is presented. In this method, an analytic signal that is a complex signal is produced. The real part is the stator current and the imaginary part is its orthogonal produced by Hilbert transform. Using this method the fault can be detected but the difference between healthy and faulty conditions is not clear. In addition, a component with relatively high amplitude is there around the base frequency which is not shown in Figure 14 (b).



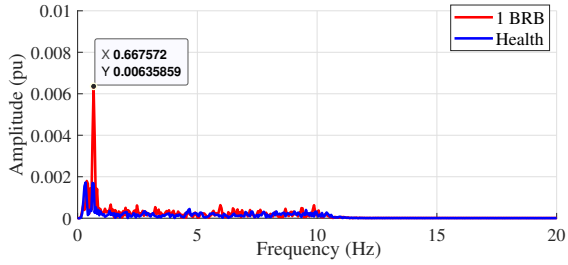
(a)



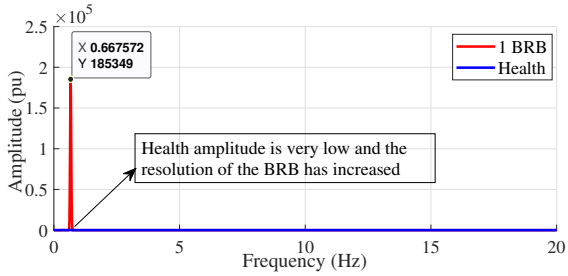
(b)



(c)



(d)



(e)

Figure 14. Comparison of the proposed method with other methods: (a) FFT,(b) the envelope method, (c) the square of stator current without filtering, (d) the square of current with filtering (the first proposed method), and (e) the third proposed method based on convolution and differentiation. All results are for the case of DTC under low load and for both healthy and one BRB conditions.

The spectrum of the square of current without any other filtering is shown in Figure 14 (c). It is observed that the component at twice the base frequency is high. The spectrum of the square of the current after applying the mentioned filters is presented in Figure 14 (d). This is the first proposed method of Figure 2. Comparing Figure 14 (b) and Figure 14 (d) reveals that the first proposed method is as successful as the envelope method while it dose not have any component at high frequency.

Finally, the results of the third proposed method of Figure 2 is shown in Figure 14 (e). As illustrated the faulty situation can be easily distinguished from the healthy condition. Because the second proposed method is not better than the third one, its results are not presented in this comparison.

4. Conclusion

This article presents a diagnostic approach to identify and detect the broken rotor bar defect in squirrel cage induction motors using the identity of the square of sum, and the results are compared and analyzed. To validate the proposed methods, laboratory data obtained from three different operating conditions, including Direct-On-Line (DOL) start, Direct Torque Control (DTC), and scalar control, are examined, and the results demonstrate the effectiveness of the proposed methods in fault detection of induction motors.

Through the analysis of results and formulas, it is evident that the proposed method accurately identifies the broken rotor bar defect in squirrel cage induction motors. As the severity of the rotor bar breakage increases, the amplitude of the spectrum at the fault frequency also increases. Additionally, a frequency weighting tool is presented to enhance the clarity of observing the fault frequency in the resulting spectrum. The resolution of the proposed method is shown to be higher with the frequency weighting tool, which involves differentiation of the signal under spectral analysis to obtain a frequency weighting factor combined with convolution.

In conclusion, this article presents a high-resolution broken rotor bar fault detection method, which has the potential to improve the performance of induction motors in various applications.

The proposed method can be examined on the other signals such as the stator voltage to find out its efficacy with them. Future work may focus on the detection of combined faults, which may occur simultaneously or fault detection in the presence of the oscillations naturally caused by the load or the supply.

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