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A vehicle routing problem with two types of ships in container terminals

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KEYWORDS Vehicle routing problem; Routing of ships;

Routing of ships; Genetic algorithm; Tramp ships; Liner ships. **Abstract.** The Vehicle Routing Problem (VRP) is one of well-established and important topics in supply chain and logistics networks. The location-routing decision-making has a significant role to optimize the traveling cost per distance, total traveling time, and the number of vehicles in the supply chain networks. One of the recent advances in these systems refers to container terminals in the global trade centers. The new contributions of this model are to consider the routes of two types of ships (Tramp and Liner) with different properties and the time windows in order to minimize costs, simultaneously. The proposed model is solved by an exact solver using LINGO software and because of inherent complexity of the problem proposed in the real-world cases, the Genetic Algorithm (GA) is used to find an optimal/global solution in a reasonable span of time. Finally, an in-depth analysis and discussion are provided to conclude the main findings and practical implications of the results.

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1. Introduction and literature review

The Vehicle Routing Problem (VRP) is one of the most essential and famous combinational optimization problems that has been studied extensively. This problem was first raised by Dantzig and Ramser as a critical issue in the field of transport distribution and logistics. It was shown that applying management methods and optimization issues in transportation had significant effect on reducing commodity costs [1]. A few years later, Clarke and Wright improved the results obtained by Dantzig and Ramser (1959) [1] by presenting a greedy heuristic approach [2]. A clear trend found in the vehicle routing studies of recent decades hovers around the transportation by trucks. In this regard, some of them are mentioned in this paper [3-5]. Coelho et al. investigated the routing

*. Corresponding author. E-mail address: featebari@gmail.com (F. Etebari) problem of a heterogeneous fleet that was allowed to travel multiple times [6]. Most notably, Lokukaluge et al. examined the impact of weather forecasts on the ship safety and found that ship safety could affect the ship's route speed. Also, taking the optimal route will result in reduced fuel consumption and, consequently, lower air pollution [7].

Li et al. investigated the VRP with heterogeneous fleet and open routes [8]. In this problem, the customers' demand is supplied by a fleet that possesses a certain number of vehicles with different capacities and related costs depending on the type of vehicle. With increase in the amount of freight, cost-effective management of fuel costs and daily operating costs for heterogeneous ships have become important issues [9]. This increase in sea freight between ports, besides fuel costs issue, has other consequences such as the emission of CO_2 and NO_x gases. This environmental issue has recently drawn the attention of many media due to the negative impacts of climate change and air pollution. On the other hand, the cost of fuel and CO_2 production is strongly dependent on the speed of the ships. Therefore, this study considers the type of the ships and the routing decisions based on the time windows intended to decrease costs.

From the last decade, there are many optimization models that have been developed to solve the Quay Crane problems. For example, Zhihong and Na [10] presented a nonlinear mathematical programming model to reduce the time of servicing for ships arriving at the terminal at horizon times, taking into account the non-crossing constraint of the quay cranes. Chen et al. [11] presented a mixed integer programming model that addressed the unique features of scheduling problem of allocating cranes in the indented berths. Legato et al. [12] proposed an improved model for the scheduling of quay cranes, taking into account factors such as the performance rate of each crane, safety requirements, precedence of containers, ready time, and due date of each crane, while the cranes can move in one direction (unidirectional cranes). Chen et al. [13] focused on a particular strategy for clusterbased quay crane scheduling problem associated with moving the unidirectional cranes in a timeline. By using this strategy called unidirectional quay crane scheduling problem in the literature, the problem of scheduling the quay cranes is enhanced. To solve the problem, they also used the state-of-the-art algorithm, which provided a better structure for searching for an optimal solution. Imai et al. [14] provided a strategy for Berth Template Problem (BTPS) to select ships from applicants for limited time horizons. Al-Dhaheri and Diabat [15] focused on the problem of scheduling the quay cranes to minimize the processing time for each vessel so that their goal was to present a way to reduce the differences between the container loads stacked over a number of bays and create a balance between ship bays in the loading and unloading operations. They also overcame the limitation of the unilateral movement of the quay cranes and made it possible for them to move on both sides, even when the operation of one bay has not been completed. Al-Dhaheri et al. [16] proposed a new model that considered the constraints of ship stability, crane displacement time, task preemption, and unidirectional movement of cranes. Because of the possibility of unexpected breakdown of cranes and a negative impact of cranes rescheduling on the planned berth, ship owners and crane operations. Liu et al. [17] studied the rescheduling of the crane with the aim of reducing negative deviations from the initial scheduling. Wu and Ma [18] focused on the problem of scheduling quay cranes by considering the draft and trim constraints, with the goal of minimizing loading time. Agra and Oliveira [19] presented an integrated model of berth allocation, quay crane assignment, and scheduling problem, which considered a set of heterogeneous cranes with discretion for time and space The efficient operation of the terminal variables.

depends on proper planning of the container movement, called "stowage planning". Azevedo et al. [20] addressed the integrated problem of the 3D stowage planning problem and quay cranes scheduling problem in container vessels. Liang et al. [21] presented a coupling model to investigate the relationship between two aspects of the quay scheduling problem: task dispatch and quantity configuration of quay cranes. The first issue determines the loading sequence of cranes and the second issue determines the number of cranes allocated to each vessel. More recently, Safaeian et al. [22] developed an integrated Quay Crane Assignment and Scheduling Problem (QCASP) with Several Contractors. They applied a Teaching-Learning-Based Optimization algorithm (TLBO) to solve the problem.

The remainder of this paper is organized as follows. Section 2 presents problem description, assumptions, notations, and mathematical formulation of the problem. Section 3 discusses the proposed Genetic Algorithm (GA). Section 4 provides computational results. Sections 5 concludes this paper and offers future directions.

2. Problem statement

In today's competitive world, lowering production costs and improving efficiency are among the priorities of industry managers' objectives and production policies, and each company tries to provide the best solutions to meet those needs. The success of many private, state, and military organizations depends on their ability to deliver optimal outputs, better products, and diverse services at a lower cost. The optimal delivery of these outputs (price, quality, performance, timely delivery, flexibility, and innovation) depends on the organization's ability to handle the exchange of materials, information, and money within and outside the organization. This exchange is known as supply chain and distribution networks. A vital issue in the supply chain is the use of methods that, in addition to managing and coordinating activities, improve and upgrade the supply chain. The objective of any distribution network model is to optimize the exchange among the network components. Therefore, based on the properties of the problem, the minimization of the objective function (usually of the cost type) is always taken into account, and these exchanges are manifested by customers' demand. Ideally, an appropriate distribution network design includes factors such as cost reduction, higher added value, and increased customer service by optimizing the communication between each node and its associated traffic flow. Establishing and simplifying these connections can reduce the total distance traveled in the network and improve the timing of loading and unloading sites. In the meantime, the issue

of transportation (as a vital element of the distribution networks between the various components of the supply chain) plays a significant role in achieving the above goals. The primary purpose of transportation planning is to minimize the cost of transporting goods and materials between the producer and consumer levels. Regarding the type of the problem under study, factors such as the distance of the route, the quality of the route in terms of structure and environment, traffic congestion, vehicle capacity, customer demand, service level, etc. are taken into account. The issue of vehicle routing is at the heart of distribution management.

Maritime transport has a broader history than other types of transportation such as trains, cars, and planes. However, from the perspective of operations research/management science, limited research has been conducted on the ship routing problem, compared to much research done in the area of VRP. However, attention to maritime transport has increased in recent decades and gained much importance.

The ocean-going vessels are divided into three main groups:

- 1. *Industrial ships:* These are the most common ocean transportation ships used to transport bulk products. In this case, all loads must be serviced and the goal is to reduce operating costs;
- 2. Tramp ships: In tramp ships, the objective is to increase profits by choosing the right cargo for a fleet of ships. Tramp ships carry the shipments from one point to another (much like a taxi). Also, tramp ships serve temporary customers who have requested relocation. In this case, the cargos must be transferred directly from the loading port to the discharge port at a specified time. Usually, tramp ships carry the loads for one customer at one time;
- 3. *Line ferries:* Line ferries follow a timetable and itinerary similar to line buses and usually carry loads for a large number of customers.

In this study, a routing problem is presented along with the ship movement scheduling for cargo transfer. Tramp and liners are considered, and the capacity and travel time of each ship vary.

In this problem, the ports are considered in two forms of discharge and loading. A certain amount of one cargo is loaded in one port and unloaded in another.

Each cargo has specified number, time window, loading, and unloading ports. The scheduling company provides an itinerary for loading and discharge of the ships. Some cargoes may not be considered in the schedule and treated as spot cargoes and, so, being serviced by tramp vessels. Tamp vessels increase the costs incurred to the company, as the cost of shipping by tramp vessels is much more expensive than the



Figure 1. Graphical display of ship routing problem.

company vessels. Besides, it is difficult to determine the cost of tramp ships in the itinerary as the delivery schedule is set 45 days before the onset of each part, and the global economy is subject to frequent cost fluctuations. For this reason, planners try to use liners as much as possible and to use the tramp vessels the least. The cargoes can be separated and loaded by more than one ship (if they do not surpass their loading and unloading time windows). The cargo can also be loaded from multiple ports and unloaded into multiple ports. Figure 1 shows a general view of the routing shipping problem. As can be seen, the departure and destination ports are different from the loading and unloading ports.

2.1. Assumptions

The main assumptions in this explicit forms are as follows:

- 1. Liners and tramps are heterogeneous;
- 2. Tramp vessels are rented, if required;
- 3. Tramps can service one cargo (tramps can only load in one port, while liners can load multiple times during one trip);
- 4. All loads must be serviced;
- 5. Each cargo has specific loading and unloading ports;
- Each loading and unloading port has a time window;
- 7. Each cargo can be serviced by tramp ships, liners, or both;
- 8. Each cargo can be serviced by more than one ship.

Table 1 defines the sets, parameters, and decision variables used in the formulation of the problem.

2.2. Mathematical formulation

The objective function of the problem and its restrictions is generally in the form of minimization and is as follows:

	Sets
\mathbf{Symbol}	Meaning
P	A set of ports where loading takes place, $P = \{1, 2, \cdots, n\}$
D	A set of ports where unloading takes place, $D = \{n + 1, n + 2, \cdots, 2n\}$
E	A set of departure and destination ports of the ships, $E = \{2n + 1, 2n + 2, \cdots, 2n + B\}$
k	A set of ships, $K = \{1, \cdots, k\}$
N	A set of middle ports, $N = P \cup D$
V	A set of all ports, $V = N \cup \{\nu_1, \cdots, \nu_n\} \cup \{\nu'_1, \cdots, \nu'_n\}$ in the graph $G = \{V, A\}$
A	A set of all routes, $A = V \times V$ in the graph $G = \{V, A\}$

Table 1.	Sets,	parameters,	and	decision	variables.

A	A set of all routes, $A = V \times V$ in the graph $G = \{V, A\}$
	Parameters
Symbol	Meaning
i	The existing load in the <i>i</i> th port. Each load has two ports: the loading port (i) and discharge
	port $(n+1)$
V_k	Any k ship can move under the graph $G_k = \{V_k, A_k\}$ so that $V_k = N \cup \{\nu_k\} \cup \{\nu'_k\}$
A_k	Any k ship can move under the graph $G_k = \{V_k, A_k\}$ so that $V_k = N \cup \{\nu_k\} \cup \{\nu'_k\}$
T_{ijk}	Travel time from port i to port j by ship k
C_{ijk}	The cost of travel from the port i to port j by ship k (including the fixed cost of port j and
	travel cost)
L_i	The amount of loaded or unloaded cargo in port i if $i \in P$. $L_i = L_{n+i}$ if $i \in P$ and $n+i \in D$
	indicating that the amount of loading in port i is equal to the amount of unloading in port $n + i$
S_i	The time tasks to anchor in port i
H_k	Maximum capacity of ship k
E_i	The earliest arrival acceptable time in the time window for the port $i \in V$
F_i	The latest arrival acceptable time in the time window for the port $i \in V$
C_{bk}^{w}	The cost of selecting dock b as the departure of the ship k
$C_{bk}^{w'}$	The cost of selecting dock b as the destination of the ship k
R_i	Freight cost of tramps for shipment of cargo i which is proportional to the amount of the cargo
	Decision variables
Symbol	Mooning

Symbol	Meaning
x_{ijk}	1, if the ship passes through the arc (i, j) , 0 otherwise
q_{ik}	The amount of cargo in the ship k when it arrives at port i
a_{ik}	Time to reach port I by ship k
y_{ik}	A portion of the cargo in port i serviced by the ship (by liners)
Z_i	A portion of the cargo in port i that is serviced by tramp vessels
ν_k	The departure condition of ship k , $\nu_k = 2n + k$
ν'_k	The destination condition of ship k , $\nu'_k = 2n + h + k$
w_{bk}	1 if dock b is the departure of the ship k , 0 otherwise
w'_{bk}	1 if dock b is the destination of the ship k , 0 otherwise

$$\min \sum_{k \in K} \sum_{(i,j) \in A} C_{ijk} x_{ijk} + \sum_{i \in P} R_i L_i Z_i$$

$$+\sum_{b\in E}\sum_{k\in K} C_{bk}^{w} W_{bk} + \sum_{b\in E}\sum_{k\in K} C_{bk}^{w'} W_{bk}', \quad (1)$$

s.t.:

$$\sum_{k \in K} Y_{ik} + Z_i = 1 \qquad \forall i \in P,$$
(2)

$$\sum_{j \in V} x_{mjk} - \sum_{i \in V} x_{i,n+m,k} = 0$$
$$\forall \ k \in K, \quad \forall \ m \in P,$$
(3)

$$\sum_{j \in P} x_{bjk} = W_{bk} \qquad \forall \ k \in K, \quad \forall \ b \in E, \qquad (4)$$

$$\sum_{i \in D} x_{ibk} = W'_{bk} \qquad \forall \ k \in K, \quad \forall \ b \in E, \qquad (5)$$

$$\sum_{b \in E} W_{bk} \le 1 \qquad \forall k \in K, \tag{6}$$

$$\sum_{b \in E} W'_{bk} \le 1 \qquad \forall k \in K, \tag{7}$$

$$\sum_{i \in V} x_{imk} - \sum_{j \in V} x_{mjk} = 0 \qquad \forall \ k \in K, \quad \forall \ m \in P \cup D,$$
(8)

$$Y_{i,k} + Y_{n+i,k} = 0 \qquad \forall \ k \in K, \quad \forall \ i \in P, \qquad (9)$$

$$Y_{jk} \le \sum_{i \in V} x_{ijk} \qquad \forall k \in K, \quad \forall j \in P, \quad (10)$$

 $a_{ik} + S_i + T_{ijk} \le a_{jk} + M(1 - x_{ijk})$

$$\forall k \in K, \quad \forall i \in V, \quad j \in P \cup D, \tag{11}$$

$$E_i \le a_{ik} \le F_i \qquad \forall \ k \in K, \quad \forall \ i \in N,$$
 (12)

$$a_{ik} + T_{i,n+i,k} \le a_{n+i,k} \qquad \forall \ k \in K, \quad \forall \ i \in P,$$
(13)

 $q_{ik} + L_i Y_{ik} \le q_{jk} + M(1 - x_{ijk})$

$$\forall k \in K, \quad \forall i \in V, \quad j \in P \cup D, \tag{14}$$

 $q_{bk} \le H_k(1 - w_{bk}) \qquad \forall k \in K, \quad \forall b \in E, \quad (15)$

$$q_{ik} \le H_k \qquad \forall \ k \in K, \quad \forall \ i \in N, \quad (16)$$

$$x_{ijk} \in \{0,1\} \qquad \forall k \in K, \quad \forall (i,j) \in A_k, \quad (17)$$

$$Z_i \ge 0 \qquad \qquad \forall \ i \in P, \tag{18}$$

$$a_{ik} \ge 0 \qquad \forall k \in K, \quad \forall i \in V_k, \quad (19)$$

$$q_{ik} \ge 0 \qquad \qquad \forall \ k \in K, \quad \forall \ i \in V_k, \quad (20)$$

$$Y_{ik} \ge 0 \qquad \qquad \forall \ k \in K, \quad \forall \ i \in P, \qquad (21)$$

$$Y_{n+i,k} \le 0 \qquad \forall k \in K, \quad \forall i \in P.$$
 (22)

In this model, the objective function (1) minimizes the total costs including the cost of servicing by tramps and liners and the cost of selecting the dock as the departure and destination. Constraint (2) indicates that all cargoes are serviced by liners and trampers (every cargo can be serviced by more than one vessel at a time). Constraint (3) relates to the protection of the load from the loading node to the discharge node, which means that if the ship k goes to the port i for loading *i*, it must meet the discharge port n + 1 for unloading cargo i. Constraint (4) implies that if the dock b is the departure of the ship k, then the ship kdeparts from the departure point to one of the loading ports or goes straight to its destination. Constraint (5) indicates that if the dock b is the destination of the ship k, then the ship k goes to its destination from one of the discharge ports or goes to the destination directly from its departure. Constraints (6) and (7) ensure that each ship can only have one departure and one destination. Constraint (8) indicates that if the vessel enters one of the middle ports, it must exit that port, too. Constraint (9) ensures that the amount of cargo loaded in port *i* by the liners is equal to the amount of cargo discharged at the corresponding node. Constraint (10) implies that if the ship k has been loaded in port j, it must have met port j. Constraint (11) presents that when ship k arrives at port j so that if skip k has passed arc $(i, j) \in A_k$, time of reaching ship k to port j is greater than or equal to the arrival time to port i plus the time of anchoring in port iplus the time of moving from i to j. Constraint (12) guarantees that the arrival time of the ship does not exceed the window time of port i. Constraint (13) indicates that the loading of cargo i by the ship koccurs before its discharge in its corresponding port. Constraint (14) expresses the existing cargo in ship kin port i similar to Constraint (11). Constraint (15) shows that cargo on board ship does not exceed the ship capacity. Constraints (16) to (22) determine the limits of decision variables.

3. Genetic Algorithm (GA)

To solve the proposed model as an NP-hard problem, a GA is applied. Nature-inspired optimization methods differ significantly from conventional optimization methods [23]. In conventional methods, each new solution candidate is selected as the new solution if it improves the Objective Function Value (OFV); however, in nature-inspired algorithms, all new candidate solutions have the opportunity to be chosen [24].

GA introduced by Holland [5] is one of the most important heuristic algorithms used to optimize different functions. In this algorithm, past information is extracted concerning the hereditary nature of the algorithm and used in the search process.

3.1. Solution structure display

The first and most crucial step in implementing a GA is the solution display [25]. The solution structure presented in this problem consists of five rectangular matrices that are given in Figures 2–6 and are described in turn:

The first matrix: This matrix is called T matrix. With this matrix, all possible routes are created ac-



Figure 2. The first chromosome string for establishing the route.



Figure 3. The second chromosome string to determine the ratio of loading of liner and tramp ships.



Figure 4. The third chromosome string to allocate loading and discharge ports to liners.



Figure 5. The fourth chromosome string to determine the departure port of the ship.



Figure 6. The fifth chromosome string to specify the destination port of the ship.

cording to the problem conditions. The dimension of this matrix is $1 \times 2P$, and P denotes the number of nodes in which the loading is done and the numbers 1 through 2P are randomly permutated there. Since each loading node has its corresponding discharge node, in some routes, the problem conditions are not met; therefore, unjustified solutions are removed using a heuristic algorithm.

In the heuristic algorithm, each route starts from the initial node and the modified path is generated in the second matrix. If the examined node is the loading port, it is placed at the beginning of the second matrix. However, if the examined node is the discharge node, there are two states. If its corresponding loading port has been serviced, it is added to the continuation of the second matrix; otherwise, it remains in its initial position and the procedure resumes from the beginning of the initial route again.

For example, if there are 5 loading ports and 5 discharge ports and the random path created by the string chromosome T, then Eq. (23) is the heuristic algorithm that operates as follows:

$$8 \to 9 \to 1 \to 2 \to 7 \to 3 \to 5 \to 10 \to 4 \to 6.$$
 (23)

First, nodes 8 and 9 are checked. Since both nodes are discharge nodes and their prerequisites have not been met, they are not transferred to the second matrix. Then, node 1 is transferred to the second matrix since it is a loading node. Each time that a node is moved to the second matrix, the first matrix is checked from the beginning of the route; therefore, after transferring port 1 to the modified matrix, Ports 8 and 9 are re-examined and they remain in their positions because their prerequisites have not been met. In the next step, node 2 is moved to the second matrix and still prerequisites of nodes 8 and 9 have remained unfulfilled. Node 7 is a discharge port and its corresponding loadig port (port 2) has already been serviced; therefore, it is added to the continuation of the modified matrix. Port 3 has no prerequisite and, then, the discharge port 8 is added to the modified matrix because its prerequisite (port 3) has been serviced. This process repeats until all ports are transferred to the second matrix. The modified route is as follows:

$$1 \to 2 \to 7 \to 3 \to 8 \to 5 \to 10 \to 4 \to 9 \to 6.$$
 (24)

The second matrix: This matrix is called Z matrix. This chromosomal string has $1 \times P$ dimensions and determines the ratio of loading in each port by liners and trampers. Numbers from 0 to 1 are assigned to each gene of the chromosome. For example, if the first gene has a value of 0.2, it means that 0.2 of the cargo of the first loading port is serviced by the tramp vessel.

The third matrix: This chromosomal string has $1 \times P$ dimensions and is called S matrix. The genes in this chromosome are numbered 1 to k, representing which ship is servicing, what loading port, and its corresponding discharge port. For example, if the problem has 5 loading ports, 5 discharge ports, and 2 liners and the first gene is assigned 2, it means that the loading port 5 and the discharge port 6 are serviced by ship 2.

The fourth Matrix: This chromosomal string has $1 \times k$ dimensions and is called O. This chromosome determines the origin of the vessels and assigns numbers 1 to b to each gene. For example, if the problem has 3 ports of departure and destination, each gene is assigned numbers 1 to 3. If the first gene of the chromosome has a value of 2, it means that the departure of the first vessel is port 2.

The fifth matrix: This chromosome is named D and acts exactly like the O chromosome, except that it determines the destination of each vessel.

4. Computational results

In this section, first, the parameters of the GA algorithm are adjusted; then, some random test problems are generated and the performance of the presented model is investigated by using an exact solver and the GA algorithm.

4.1. Parameter setting

The quality of an algorithm is significantly influenced by its parameter values. One of the purposes of the design of the experiments is to change the input variables deliberately to detect and identify the output variations [26]. There are several methods to design the experiment. One of these methods is parameter tuning by the Taguchi method that proposes a minimum number of orthogonal experimental designs in which the factors can be independently verified. In this method, the Signal to Noise ratio (S/N) is used to determine the best combination of experiments. To measure the best N/S ratios, Taguchi has proposed three equations of (25)-(27) in which Y_i is the answer value in the ith experimental condition and n is the number of designed experiments. Also, in the equations, S and yare the mean and variance of the experiment answers,

respectively [27].

$$(S/N)_S = -10\log_{10}\left(\frac{\sum y_i^2}{n}\right),$$
 (25)

$$(S/N)_t = -10\log_{10}\left(\frac{1}{n}\sum \frac{1}{y_i^2}\right),$$
 (26)

$$(S/N)_T = -10 \log_{10} \left(\frac{y^2}{s^2}\right).$$
 (27)

To improve the performance of the proposed algorithms, we adjusted their input parameters by the Taguchi method. Because of the designed problems for the model, the parameter setting has been applied to Problem 20. Table 2 presents different levels of the parameters of the GA. The experiments are for algorithm L_9 using the Taguchi method. Table 3 presents the orthogonal arrays of the algorithm and its results.

 Table 2. Parameter levels of Genetic Algorithm (GA) algorithm.

Parameters	Low (1)	Medium~(2)	High (3)
npop	50	100	150
nIt	50	100	150
Pc	0.5	0.7	0.9
Pm	0.3	0.4	0.5

 Table 3. The designed experiments of Genetic Algorithm
 (GA) algorithm.

npop	nImp	$\max it$	bata	RPD	S/N
1	1	1	1	0.0250673	12.01784
1	2	2	2	0.116317	18.68716
1	3	3	3	0.107701	19.35564
2	1	2	3	0.078352	22.11898
2	2	3	1	0.116317	18.68716
2	3	1	2	0.063274	23.97548
3	1	3	2	0	80
3	2	1	3	0.094238	20.51548
3	3	2	1	0	80



Figure 7. S/N diagram of Genetic Algorithm (GA).

Table 4. The optimal values of parameters of FA and ICA algorithms.

Algorithm	Optimal value							
Aigoritinn	npop	nIt	\mathbf{PC}	$\mathbf{P}\mathbf{M}$				
ICA	150	150	0.7	0.4				

The S/N index obtained for each algorithm parameter in Figure 7 indicates the best level for the algorithm. The optimum values for each parameter are also shown in Table 4.

4.2. Random example in small and large scales In this section, the performance of the presented routing model and the GA algorithm extension is verified through 10 numerical examples on a small scale and 10 numerical examples on a large scale. Tables A.1 and A.2 in the Appendix illustrate the parameters of the examples generated on small and large scales. Smallscale examples are optimally solved by exact solver in LINGO 17.0 software using a 3.5 GHz PC and 8 $\,$ GB RAM. Also, all examples have been solved by the introduced GA algorithm in MATLAB. Then, the results of the B&B and GA methods were compared in terms of the OFV and CPU time. Each example was solved 20 times by the GA algorithm and, then, the average OFV and CPU time values were reported. Since differences between the exact method and GA are reasonable, the accuracy of model is proven.

Also, the routes of liners and tramps can be observed under the Rout column in Table 5. Figure 8 shows the graphical representation of the solution problem. In this problem, we have considered 8 loading ports (ports 1 to 8), 8 discharge ports corresponding to the loading ports (ports 9 to 16), and 2 ports for the



Figure 8. Graphical display of the problem.

ship's departure and destination (17 and 18). There are also 4 liner ships. The first and second ships had no movements. The third ship has met and been serviced by the yellow port, and the fourth ship has visited and serviced the orange ports. Ports 2, 3, 8, 10, 11, and 16 have been serviced by tramp ships. Besides, ports 17 and 18 are the departure and destination of the ships.

5. Conclusion

Conventionally, the Vehicle Routing Problem (VRP) is one of well-established and important topics in supply chain and logistic networks. The location-routing decision-making has a significant role to optimize the traveling cost per distance, total traveling time, and the number of vehicles in the supply chain networks most practically for container terminals in the global trade centers. The new contributions of this model were to consider the routes of two types of ships, the time windows, and a multi-modal transportation

	\mathbf{Exact}	Exact GA					
No.	Rout	OFV	$egin{array}{c} {f CPU} \\ {f time} \\ {f (s)} \end{array}$	Rout	OFV	Mean CPU time (s)	Gap
1	$ \begin{array}{cccc} k1: & 11 {\rightarrow} 1 {\rightarrow} 6 {\rightarrow} 4 {\rightarrow} 2 {\rightarrow} 9 {\rightarrow} 3 \\ & {\rightarrow} 7 {\rightarrow} 8 {\rightarrow} 5 {\rightarrow} 10 {\rightarrow} 11 \end{array} $	47	1123	$\begin{array}{c} k1 \colon 11 {\rightarrow} 1 {\rightarrow} 6 {\rightarrow} 4 {\rightarrow} 2 {\rightarrow} 9 {\rightarrow} 3 {\rightarrow} 7 {\rightarrow} 8 \\ {\rightarrow} 5 {\rightarrow} 10 {\rightarrow} 11 \end{array}$	47	4.7	0
2	$\begin{array}{c} k2 \colon 8 \longrightarrow 1 \longrightarrow 4 \longrightarrow 3 \longrightarrow 2 \longrightarrow 6 \longrightarrow 5 \longrightarrow 7 \\ k3 \colon 8 \longrightarrow 3 \longrightarrow 6 \longrightarrow 8 \end{array}$	55	264	$k2: 8 \rightarrow 1 \rightarrow 4 \rightarrow 7$ $k3: 8 \rightarrow 3 \rightarrow 6 \rightarrow 2 \rightarrow 5 \rightarrow 8$	61	3.5	0.1
3	$\begin{array}{ccc} k3: & 8 \rightarrow 3 \rightarrow 6 \rightarrow 2 \rightarrow 1 \rightarrow 4 \\ & \rightarrow 5 \rightarrow 7 \end{array}$	34.1	2	$k3: 8 {\rightarrow} 3 {\rightarrow} 6 {\rightarrow} 2 {\rightarrow} 1 {\rightarrow} 4 {\rightarrow} 5 {\rightarrow} 7$	34.1	3.5	0
4	$\begin{array}{ccc} k1: & 9 {\rightarrow} 2 {\rightarrow} 6 {\rightarrow} 4 {\rightarrow} 8 {\rightarrow} 1 {\rightarrow} 3 \\ & {\rightarrow} 5 {\rightarrow} 7 {\rightarrow} 10 \end{array}$	47.03	52	$k2: 9 \rightarrow 4 \rightarrow 8 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 10$	50.67	3	0.07
5	$k1: 9 \rightarrow 1 \rightarrow 3 \rightarrow 5 \rightarrow 7 \rightarrow 10$ Tramp ship: 2,4,6,8	30.98	20	$k2: 9 \rightarrow 1 \rightarrow 5 \rightarrow 3 \rightarrow 7 \rightarrow 10$ Tramp ship: 2,4,6,8	36.78	3	0.18
6	$\begin{array}{rl} k2: & 11 \longrightarrow 4 \longrightarrow 8 \longrightarrow 2 \longrightarrow 6 \longrightarrow 1 \\ & \longrightarrow 5 \longrightarrow 9 \\ \text{Tramp ship: } 3,7 \end{array}$	33.57	16	k2: $9 \rightarrow 4 \rightarrow 8 \rightarrow 2 \rightarrow 6 \rightarrow 1 \rightarrow 5 \rightarrow 9$ Tramp ship: 3,7	33.57	4	0
7	$\begin{array}{ccc} k1: & 9 {\rightarrow} 2 {\rightarrow} 4 {\rightarrow} 8 {\rightarrow} 3 {\rightarrow} 7 \\ & \rightarrow 6 {\rightarrow} 1 {\rightarrow} 5 {\rightarrow} 10 \end{array}$	45.16	267	$\begin{array}{ccc} k1 \colon 9 {\rightarrow} 2 {\rightarrow} 4 {\rightarrow} 8 {\rightarrow} 3 {\rightarrow} 7 {\rightarrow} 6 {\rightarrow} 1 \\ {\rightarrow} 5 {\rightarrow} 10 \end{array}$	45.16	4.2	0
8	$\begin{array}{cccc} k1 \colon & 11 {\rightarrow} 1 {\rightarrow} 6 {\rightarrow} 3 {\rightarrow} 8 {\rightarrow} 4 {\rightarrow} 9 \\ & \rightarrow 5 {\rightarrow} 10 {\rightarrow} 2 {\rightarrow} 7 {\rightarrow} 13 \end{array}$	38	2521	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39	5	0.02
9	$\begin{array}{c} k1: \ 11 \rightarrow 1 \rightarrow 6 \rightarrow 4 \rightarrow 3 \rightarrow 9 \\ \rightarrow 8 \rightarrow 5 \rightarrow 10 \rightarrow 12 \end{array}$ Tramp ship: 2,7	38.36	87	$k1: 11 \rightarrow 1 \rightarrow 6 \rightarrow 5 \rightarrow 10 \rightarrow 12$ Tramp ship: 2,3,4,7,8,9	39.96	4	0.04
10	$k1: 15 \rightarrow 5 \rightarrow 11 \rightarrow 2 \rightarrow 8 \rightarrow 15$ Tramp ship: 1,3,4,6,7,9,10,12	44.6	414	$k1: 15 \rightarrow 5 \rightarrow 11 \rightarrow 2 \rightarrow 8 \rightarrow 15$ Tramp ship: 1,3,4,6,7,9,10,12	44.6	3.6	0
11	_		More than one hour	$\begin{array}{l} k2: \ 15 \longrightarrow 5 \longrightarrow 11 \longrightarrow 14 \\ k3: \ 13 \longrightarrow 4 \longrightarrow 10 \longrightarrow 2 \longrightarrow 8 \longrightarrow 14 \\ \text{Tramp ship: } 1,3,6,7,9,12 \end{array}$	78.66	5	
12	—		More than one hour	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	51.56	4.5	
13	_	_	More than one hour	k2: $15 \rightarrow 2 \rightarrow 9 \rightarrow 6 \rightarrow 13 \rightarrow 15$ Tramp ship: 1,3,4,5,7,8,10,11,12,14	89.7	4	
14	_		More than one hour	$\begin{array}{l} k2 \colon 15 {\rightarrow} 4 {\rightarrow} 11 {\rightarrow} 5 {\rightarrow} 12 {\rightarrow} 7 {\rightarrow} 14 {\rightarrow} 15 \\ \text{Tramp ship: } 1,2,3,6,8,9,10,13 \end{array}$	94.8	5	
15	—		More than one hour	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	64.96	6	
16	_		More than one hour	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	70.44	6	

 Table 5. The calculation results of numerical examples on small and large scales.

		Exac	et	GA			
No.	Rout	OFV	$egin{array}{c} { m CPU} \ { m time} \ { m (s)} \end{array}$	Rout	OFV	Mean CPU time (s)	Gap
17	_	_	More than one hour	k1: $18 \rightarrow 4 \rightarrow 12 \rightarrow 5 \rightarrow 13 \rightarrow 7 \rightarrow 15 \rightarrow 6 \rightarrow 14 \rightarrow 18$ Tramp ship: 1,2,3,8,9,10,11,16	89.26	5	_
18			More than one hour	k3: $18 \rightarrow 5 \rightarrow 13 \rightarrow 4 \rightarrow 12 \rightarrow 7 \rightarrow 15 \rightarrow 17$ k4: $18 \rightarrow 1 \rightarrow 9 \rightarrow 6 \rightarrow 14 \rightarrow 17$ Tramp ship: 2,3,8,10,11,16	70.26	5.5	
19			More than one hour	$\begin{array}{ll} k1: & 19 \rightarrow 6 \rightarrow 15 \rightarrow 8 \rightarrow 17 \rightarrow 1 \rightarrow 10 \rightarrow 9 \rightarrow 18 \rightarrow 19 \\ k2: & 19 \rightarrow 5 \rightarrow 14 \rightarrow 7 \rightarrow 16 \rightarrow 4 \rightarrow 13 \rightarrow 20 \\ \end{array}$ Tramp ship: 2,3,11,12	66.46	6.5	_
20			More than one hour	k3: $14 \rightarrow 5 \rightarrow 11 \rightarrow 13$ k4: $14 \rightarrow 1 \rightarrow 7 \rightarrow 4 \rightarrow 10 \rightarrow 14$ k5: $14 \rightarrow 6 \rightarrow 12 \rightarrow 14$ Tramp ship: 2,3,8,9,13,14	39.46	5	_

Table 5. The calculation results of numerical examples on small and large scales (continued).

system simultaneously. The proposed was solved by an exact solver as well as a Genetic Algorithm (GA) for large-scale tests. The performance of GA was enhanced by a Taguchi experimental design method. Finally, an in-depth analysis and discussion were provided.

This research can open several new contributions for the future works. No doubt other heuristics and metaheuristics can solve the proposed problem practically and computationally better than GA. Therefore, more efforts to solve heuristically the proposed problem are needed. The sustainability dimensions and environmental protections can be ordered to improve the proposed modeling by a multi-objective optimization as a potential continuation of this paper.

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Appendix A

Parameters of the examples generated on small and large scales are shown in Tables A.1 and A.2.

No.		Problem Information										
	Р	D	E	k	T_{ijk}	C_{ijk}	R_i	${old S}_i$	E_i	F_{i}	H_k	Li
1	1 - 5	6-10	3	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[100, 200]	$\operatorname{Randi}(1,5)$	0	100	1000	$\operatorname{Randi}(50,100)$
2	1 - 3	4-6	2	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[13, 20]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(20,30)$	(120, 110, 130)	Randi(80,130)
3	1 - 3	4-6	3	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.02, 0.9]	$\operatorname{Randi}(1,5)$	0	Randi(30,60)	$(80,\!110,\!150)$	$\operatorname{Randi}(50,120)$
4	1 - 4	5-8	2	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(80,120)$	(80, 110)	$\operatorname{Randi}(70,110)$
5	1-4	5-8	2	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	Randi(80,130)	(80,130)	$\operatorname{Randi}(50,100)$
6	1-4	5-8	3	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.3]	Randi(1,6)	0	Randi(80,130)	(130, 140)	$\operatorname{Randi}(70,120)$
7	1-4	5-8	3	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.15, 0.2]	$\operatorname{Randi}(1,5)$	0	Randi(80,130)	(130,100,110)	Randi(100,120)
8	1 - 5	6-10	3	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	$[0.35,\!0.6]$	$\operatorname{Randi}(1,5)$	0	Randi(100,110)	(150, 200, 100)	Randi(80,110)
9	1 - 5	6-10	3	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.02, 0.2]	$\operatorname{Randi}(1,5)$	0	Randi(100,110)	(100, 100)	$\operatorname{Randi}(80,120)$
10	1 - 6	7-12	3	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.6]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(20,60)$	(80,120)	$\operatorname{Randi}(70,130)$
11	1 - 5	6-10	3	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	$[0,\!0.6]$	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(20,60)$	(80, 120)	$\operatorname{Randi}(70,120)$
12	1 - 7	8-14	2	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(100,110)$	$(80,\!130)$	$\operatorname{Randi}(70,130)$
13	1 - 7	8-14	3	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(30,70)$	$(70,\!100)$	$\operatorname{Randi}(80,150)$
14	1 - 7	8-14	2	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.9]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(40,80)$	(100, 130)	$\operatorname{Randi}(80,140)$
15	1-8	9-16	2	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.03, 0.9]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(90,110)$	(100, 100)	$\operatorname{Randi}(80,120)$
16	1-8	9-16	3	3	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(100, 120)$	(100, 100)	$\operatorname{Randi}(80,120)$
17	1-8	9-16	2	2	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	$[0,\!0.5]$	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(100,110)$	(100, 110)	$\operatorname{Randi}(70,120)$
18	1-8	9-16	2	4	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(100,110)$	(100, 150)	Randi(100,150)
19	1 - 9	10-18	2	4	$\operatorname{Randi}(0,10)$	$\mathrm{Randi}(0,\!10)$	[0.01, 0.5]	$\operatorname{Randi}(1,5)$	0	$\operatorname{Randi}(100,130)$	(100, 140)	$\operatorname{Randi}(70,130)$
20	1 - 6	7-12	2	5	$\operatorname{Randi}(0,10)$	$\operatorname{Randi}(0,10)$	[0.02, 0.5]	$\operatorname{Randi}(1,5)$	0	Randi(100,110)	$(90,\!140)$	Randi(80,110)

Table A.1. Parameters of random instances in small and big sizes.

Table A.2. Parameters of random instances in small and big sizes.

				Problem in	formation				
				N	0.				
	1		2	:	3		4	5	
C_{bk}^w	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C_{bk}^w	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C_{bk}^w	$C^{w'}_{bk}$
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	0 0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	0 0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0	$10\;11\;\;8$	$9\ 13\ 11$	$10 \ 11 \ 9$	$9\ 13\ 11$	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0	$15 \ 8 \ 10$	$14\ 11\ 8$	15 8 8	$11\ 12\ 9$	0 0	0 0	0 0 0	$0 \ 0 \ 0$
0 0	0 0			$11\ 12\ 7$	$14\ 11\ 8$	$11 \ 9$	$11\ 11$	$9 \ 9 \ 12$	$12 \ 9 \ 11$
0 0	0 0					$10 \ 14$	$9 \ 12$	$17 \ 12 \ 11$	9 8 8
$10 \ 11$	$9 \ 13$								
$15 \ 8$	$11\ 12$								
11 12	14 11								
	6	م ا	7		8)	1()
C_{bk}^w	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
0 0	0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
8 10	13 8	8 8 11	$9\ 13\ 11$	8 9 8	$15 \ 11 \ 9$	0 0	0 0	0 0	0 0
$11\ 12$	9 11	$14\ 13\ 10$	$11\ 12\ 9$	$13\ 12\ 12$	$15\ 10\ 11$	0 0	0 0	0 0	0 0
99	1114	$15 \ 7 \ 9$	$14\ 11\ 8$	$9 \ 14 \ 10$	$11\ 15\ 14$	4 4	45	0 0	0 0
						56	45	0 0	0 0
						3 5	53	54	44
								44	54
	-		0		0		4	56	43
I	$\frac{1}{C^{w'}}$		$\frac{2}{C^{w'}}$	$-\frac{1}{C^w}$	$\frac{3}{C^{w'}}$	$-\frac{1}{C^w}$	$\frac{4}{C^{w'}}$	$-\frac{1}{C^w}$	$C^{w'}$
	C_{bk}	C_{bk}	0.0	C_{bk}	0.0	C_{bk}	C_{bk}	C_{bk}	0.0.0
		0 0	0 0	0 0	0 0		0 0 0	000	000
		0 0	0 0	0 0	0 0		0 0 0	000	000
		0 0	0 0	0 0	0 0		0 0 0	000	000
		0 0	0 0	0 0	0 0		0 0 0	000	000
		0 0	0 0	0 0	0 0		0 0 0	000	000
			0 0		0 0		0 0 0	000	000
			0 0				0 0 0	000	000
0 0 0		0 0	0 0	0 0	0 0		0 0 0	000	000
			0 0				0 0 0	000	000
0 0 0	0 0 0	0 0	0 0	0 0	0 0	0 0 0	0 0 0	000	000
0 0 0	0 0 0	0 0	0 0	0 0	0 0	0 0 0	0 0 0	000	000
$12\ 12\ 8$	14 8 11	0 0	0 0	0 0	0 0	0 0 0	0 0 0	000	000
9 8 12	10 11 9	0 0	0 0	0 0	0 0	0 0 0	0 0 0	000	000
14 8 12	8 12 8	13 10	10 13	14 11	8 10	14 11 11	0 0 0	000	000
11012	0 12 0	11 11	14 11	9 14	11 12	9 14 8	$11 \ 8 \ 11$	000	000
				8 10	14 12	0 11 0	$7 \ 11 \ 9$	564	584
				0 10				354	427
								001	'

	Problem information										
	No.										
10	6	1	7	1	8	1	9	20			
C^w_{bk}	$C^{w'}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$	C^w_{bk}	$C^{w^\prime}_{bk}$	C^w_{bk}	$C^{w^{\prime}}_{bk}$	C^w_{bk}	$C^{w'}_{bk}$		
0 0 0	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0 \ 0$	00000		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0 \ 0$		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0 \ 0$		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
0 0 0	000	0 0	0 0	0000	0000	0000	0000	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	$0 \ 0 \ 0 \ 0$	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	0000	00000	00000		
0 0 0	000	0 0	0 0	0000	0000	0000	0000	00000	00000		
$0 \ 0 \ 0$	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	0000	85687	$5\ 5\ 9\ 3\ 7$		
$0 \ 0 \ 0$	000	0 0	0 0	0000	0000	$0 \ 0 \ 0 \ 0$	0000	$6\ 1\ 8\ 1\ 6$	$2\;3\;1\;5\;6$		
0 0 0	000	0 0	0 0	0000	0000	0000	0000				
0 0 0	000	0 0	0 0	0000	0000	0000	0000				
$5\ 6\ 4$	584	8 5	9 10	$1\;5\;4\;8$	$1 \ 9 \ 3 \ 6$	$0 \ 0 \ 0 \ 0$	0000				
$3\ 5\ 4$	$4\ 2\ 7$	$9\ 10$	4 5	$2 \ 9 \ 4 \ 1$	$2\ 4\ 4\ 8$	$0 \ 0 \ 0 \ 0$	0000				
$8\ 10\ 4$	974					$1\;5\;4\;8$	$1 \ 9 \ 3 \ 6$				
						$2 \ 9 \ 4 \ 1$	$2\ 4\ 4\ 8$				

Table A.2. Parameters of random instances in small and big sizes (continued).

Biographies

Mojgan Safaeian was born in Behbahan, Iran and raised in Tehran, Iran. She earned her BSc degree in Computer Science from Sheikh-Bahaee University, Isfahan, Iran (2010). She also received her MSc degree in Industrial Engineering from Azad University, Qazvin, Iran (2013).

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