A comparison of some methods for structural damage detection

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Abstract. In principal, a proper analysis of the dynamic response of a structure can provide general indicators of its operational conditions. When the dynamic response changes due to variations of the physical properties of a structure, then one may conclude that some kind of damage has occurred. This paper presents an investigation of the robustness and comparison of four simple methodologies to both identify and quantify the damages in structures, based on the use of Frequency Response Functions (FRF) signals, Principal Component Analysis technique (PCA), and transmissibility. A steel beam with constant rectangular cross-section is used to compare the proposed approaches. At first, nine damaged scenarios are created, for each of which numerical examples are discussed; a database of FRFs is measured using modal testing. Then, PCA theory is applied to the FRF matrix, and global damage detection and quantification indices are defined using the first three principal components; Hotelling’s T-squared distribution is also applied, and two other indicators, transmissibility damage indicator and weighted damage indicator, are computed for the assessment of damage using transmissibility. The reported examples show that all proposed methods are able to detect and quantify damages at the initial stage.

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1. Introduction

Nowadays, the interest in the ability to monitor a structure and identify damages at the earliest possible stage is pervasive throughout aerospace structures, bridges, civil infrastructures, and mechanical engineering systems. Detection and localization of damage allows one to reduce maintenance costs and ensure safety [1-3]. Several non-destructive inspection methods (NDE) for the evaluation of the health condition of a structure are currently available such as acoustic or ultrasonic methods, magnet field methods, radiographs, eddy-current methods or thermal field methods, etc. Unfortunately, these experimental techniques may be difficult, costly and unreliable, because damage location must be known in advance, or it is often necessary to expose the structural elements and the equipment to the inspector for detecting damage, with relevant accessibility problems. This is the reason for which alternative approaches in recent decades are mainly based on the changes of the vibration characteristics or the responses of the structures caused by a structural damage; consequently, such approaches have received considerable attention in the literature [4-7]. For example, some authors have localized some damages by comparing identified mode shapes or their second-order derivatives [8] in varying levels of damage. Sampaio

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et al. [9] extended the method proposed in [8] with measured FRFs. Failing to consider just the FRFs in the low-frequency range, Friswell [10] presented an overview of the usage of inverse methods in damage detection and location by measured vibration data. Liu et al. [11] used the imaginary part of FRF shapes and normalized FRF shapes to achieve damage localization. Their method was illustrated by a numerical example of a cantilever beam. Natural frequency sensitivity was also used extensively for the purposes of damage localization. Ray and Tian [12] discussed the sensitivity of natural frequencies with respect to the location of local damage. In that study, damage localization has involved the consideration of changes in the mode shapes. Zhou et al. [13] and Zhou and Perera [14] used power spectral density transmissibility to detect damages using modal assurance criterion and artificial neural networks, respectively; Zhao et al. [15] discussed damage detection and localization using the transmissibility-based nonlinear feature analytically.

The fundamental idea of the vibration methods for damage detection is that modal parameters (natural frequencies, mode shapes, and modal damping) are functions of the physical properties of the structure (mass, damping, and stiffness). Therefore, changes in the physical properties will cause detectable changes in the modal properties. Therefore, this process involves the observation of a structure/system along the time using periodical measurements. In other words, most vibration-based damage detection methods can be considered as a form of the pattern recognition problem. As they look for the discrimination between two or more signal categories, e.g., before and after a structure is damaged or for differences in the damage levels or locations. In this situation, it is common to deal with a large variety of complex systems in which the number of variables to be measured can be unwieldy and even sometimes deceptive, because the implicit relationships can often be quite simple.

The main problem in applying this approach is the very small variation of dynamic response due to structural damage related to the local variation of stiffness, mass, and damping. Aiming to overcome these drawbacks, more explicit and capable methods are needed to detect the presence of damage even in the case of small variation of the dynamic response, in addition to the need for a method to reduce the requested amount of data. Several data reduction techniques are available for this purpose. The potential advantages of this kind of approaches can be summarized as follows:

- They do not require direct exposure of structural elements;
- They inspect the whole structure in one dynamic test;
- They favor a reduction in schedule and cost.

In this paper, damage detection in a steel beam is carried out using four new different methods by the vibration response data directly measured along a structure during modal testing. Those methods are able to identify and quantify the damage using transmissibility techniques, Hotelling’s T-squared distribution, and the principal components of FRF matrices.

The paper is organized in six sections. Section 2 gives a brief description of damage identification methods. Section 3 introduces the beam structure used for the validation of damaged scenarios investigated during modal testing. Section 4 describes the FE model of the considered beam and includes the application of adopted damage detection methods to the simulated damage scenarios. Section 5 presents experimental modal testing and related results. Finally, Section 6 concludes the paper.

2. Brief theoretical description of the developed methods

2.1. Principal component analysis

Principal Components Analysis (PCA) is a standard tool to identify patterns in data and represent the data in a manner that highlights their similarities and dissimilarities. In other words, PCA is an attractive numerical procedure for analyzing the basis of the variation present in a multi-dimensional dataset and identifying the most meaningful basis to re-express a dataset. PCA is called one of the most valuable results derived from applying linear algebra developed by Jolliffe [16] and Bishop [17]. It can be viewed as a statistical technique capable of realizing a dimensionality reduction, based on a transformation from the original set of variables into a new set of uncorrelated variables, i.e., the Principal Components (PC). Using an orthogonal projection, the original set of variables in an $N$-dimensional space is transformed into a new set of uncorrelated variables, the Principal Components, in a $P$-dimensional space, such that $P < N$. It is assumed that all FRF data are equally important in describing the underlying features of the baseline signals, and the standard “auto scaling” procedure is performed for pre-processing. By “auto scaling”, each column of the FRF matrix is arranged to have a zero mean (by subtracting the mean value of each column) and to have a unit variance (by dividing each column by its standard deviation). The procedure is described below. Using all available FRF data of the intact structure,
FRF matrix $H$ has $N$ rows of FRFs ($N$ observations from different sensors), each with $M$ frequency points. Each element is denoted by $H_{ij}(\omega)$. The mean response ($\bar{H}_i$) and standard deviation ($S_i$) of the $i$th row can be defined as follows:

$$\bar{H}_i = \frac{1}{M} \sum_{j=1}^{M} H_{ij}(\omega),$$

$$S_i^2 = \frac{1}{M} \sum_{j=1}^{M} (H_{ij}(\omega) - \bar{H}_i)^2.$$  \hspace{1cm} (1)

It is possible now to calculate response variation matrix, $\tilde{H}(\omega)_{N \times M}$, where a typical element of the $H_{ij}(\omega)$ FRF matrix can be replaced by:

$$\tilde{H}_{ij}(\omega) = \frac{H_{ij}(\omega) - \bar{H}_i}{S_i \sqrt{M}}.$$  \hspace{1cm} (2)

Sample covariance matrix, $C$, can be defined as follows [18, 19]:

$$C = \tilde{H}(\omega)_{N \times M}^{\top} \tilde{H}(\omega)_{M \times N},$$  \hspace{1cm} (3)

where $\tilde{H}(\omega)$ is the matrix transpose measurement, $C$ is a $N \times N$ matrix whose diagonal terms are the variance of $N$ variables, and non-diagonal terms represent the covariance between variables.

By definition, the Principal Components (PCs) are the eigenvalues and associated eigenvectors (principal loadings) of the covariance matrix:

$$C \psi_i = \lambda_i \psi_i.$$  \hspace{1cm} (4)

The first principal component, i.e., the highest eigenvalue and its associated eigenvector, represents the amount and direction of the maximum variability in the original data. The next one, which is orthogonal to the first component, represents the next most significant contribution from the original data, and so on. Finally, to perform PCA is simple in practice through the basic steps [20]:

1. Organize the dataset as a $M \times N$ matrix, where $M$ is the observations from different sensors and $N$ is the number of frequency lines;
2. Normalize the data to have zero mean and unity variance;
3. Calculate the eigenvectors and eigenvalues of the correlation (covariance) matrix;
4. Select the first eigenvectors as the principal components;
5. Transform the original data by means of the principal components (projection).

Concerning the damage detection, firstly, Global Damage Index (GDI) can be introduced as a function of the first principal components (often the first three ones) as follows [20]:

$$\text{GDI}_{GDI} = \sqrt{\sum_{i=1}^{3} (\Delta PC_i)^2},$$  \hspace{1cm} (6)

where $\Delta PC_i$ represents the relative variation between the $i$th principal component related to the damaged situation and the actual or undamaged one. In general, due to the compression property strictly related to PCA, such a limited number of principal components are enough to guarantee good results [21].

2.2. Hotelling’s $T^2$ statistic

Hotelling developed a control procedure based on a concept referred to as statistical distance, a generalization of the $T$ statistic. The statistic was later named Hotelling’s $T^2$ in his honor. Hotelling’s $T^2$ takes into account the correlation between the variables based on analyzing the score matrix to check the variability of the projected data in the new space of the principal components [20].

Hotelling’s $T^2$ statistic is obtained for each data point from the concept of Euclidean distance, normalized with the covariance of the FRF Matrix [22]:

$$T^2(\omega_j) = H_j^T(\psi \Lambda^{-1} \psi^T)H_j,$$  \hspace{1cm} (7)

where $H_j$ is an $N$-column vector that represents the measurements from all sensors at the $j$th frequency point, $\psi$ is the eigenvector matrix related to the PCs, and $\Lambda$ is the principal component matrix.

The proposed damage indicator using Hotelling’s $T^2$ statistic can be expressed as a function of each data point as follows [20]:

$$DI_{T^2} = \frac{1}{M} \sum_{j=1}^{M} \left| \left( \Delta T^2(\omega_j) \right) \right|,$$  \hspace{1cm} (8)

where $\Delta T^2(\omega_j)$ represents the relative variation of the Hotelling’s $T^2$ statistic for each frequency between the damaged and undamaged models.

2.3. The transmissibility concept

The transmissibility concept [23] is briefly summarized in the following. Given a number of harmonic forces, $F_A$, that can be applied at coordinates $A$, the amplitudes at coordinates $U$, $X_U$ and at coordinates $K$, $X_K$ are related to those forces through $H_{UA}$ and $H_{KA}$:

$$X_U = H_{UA} F_A,$$  \hspace{1cm} (9)

$$X_K = H_{KA} F_A.$$  \hspace{1cm} (10)
Eliminating $F_A$ between Eqs. (9) and (10) gives:

$$X_U = H_U H_{KA}^{-1} X_K = T_{UK} X_K,$$

(11)

where $T_{UK}$ is the transmissibility matrix. The inversion in Eq. (11) is only possible if the number of coordinates $K$ is equal to or greater than the number of coordinates $A$. In the latter case, the pseudo-inverse must be used. Thus, from the measurement of $X_K$, one can calculate $X_U$, and vice versa; since $F_A$ has been eliminated from Eqs. (9) and (10), $T_{UK}$ does not depend on the magnitude of the forces. On the other hand, the division between two responses is also called transmissibility. However, this will be dependent on the magnitudes and location of the forces and is called “Direct Transmissibility”. For example, by dividing Eq. (11) by one of amplitudes $X_K$, say $X_S$, one has:

$$X_U/X_S = T_{UK} X_K/X_S, \quad \text{or}$$

$$\tau_{US} = T_{UK} \tau_K.$$

(12)

If only a single force is applied at coordinate $j$ and only two coordinates are related, say, $r$ and $s$, both types of transmissibility coincide and everything simplifies to:

$$\tau_{rs} \equiv \tau_{rj} = X_r/X_s = H_{rj}/H_{ij}.$$

(13)

It should be noted that the applied forces do not have to be harmonic. The expressions for the transmissibility remain valid for other types of excitation, including those of an impulsive or random nature [24].

2.3.1. Damage detection and quantification using transmissibility

The motivation for using the transmissibility to detect damage relies on the fact that they are local quantities and correspond to the zeros of the FRFs, not with their poles; this “local characteristic” suggests a higher ability (or sensitivity) to detect changes in the dynamic behavior due to some kind of damages.

The Transmissibility Damage Indicator (TDI) is presented in [25]. It computes a set of direct transmissibilities along the structure: undamaged $(\tau_{rs})$ and damaged $(\tau_{rs}^d)$ at each frequency (ω). In a systematic way, one progresses along the structure calculating successive pairs of coordinates, i.e., those with $s = r + 1$.

The correlation between the undamaged and damaged transmissibilities is calculated; in principle, the smaller the degree of correlation, the larger the damage. The degree of correlation is evaluated with the Response Vector Assurance Criterion (RVAC) [26]:

$$\text{RVAC}(\omega) = \frac{\sum_{s=1}^{N-1} \tau_{rs}^d(\omega) \cdot \overline{\tau_{rs}(\omega)}^2}{\sum_{s=1}^{N-1} \tau_{rs}^d(\omega) \cdot \overline{\tau_{rs}(\omega)}},$$ 

$$s \equiv r + 1,$$

(14)

where “$\overline{\cdot}$” means the complex conjugate, and $N$ is the number of measured coordinates.

One can also take various measurements here, vary position $j$ of the applied force ($M$ positions), and sum up the results leading to the MRVAC (Multiple Response Vector Assurance Criterion) [25] which is obtained by Eq. (15) as shown in Box I.

The Transmissibility Damage Indicator is defined by Eq. (16), as shown in Box II, where $N_w$ is the number of frequencies. TDI varies from 0 to 1, from total damage to no damage, respectively.

2.4. Damage detection and quantification using weighted damage indicator

The Weighted Damage Indicator (WDI) is an improvement to the TDI, where the values of the MRVAC along the frequency range are taken into consideration together with the number of times that those results happen. The values of the MRVAC are classified in 10 intervals of 0.1 (MRVAC values from 1 to 0.9, 0.9 to 0.8..., 0.1 to 0). For each interval $i$, the contribution of the MRVAC value is given by:

$$\left( \frac{\sum_{j=1}^{N_w} \text{MRVAC}_j}{N} \right)_i,$$

where $n_i$ is the number of recorded observations, and the incidence of the number of occurrences in each

Box I
interval is \( n_i/N \). Therefore, a possible indicator of damage in each interval \( i \) is:

\[
A_i = \frac{\sum_{j=1}^{n_i} MRVAC_{ji}}{N} \times \frac{n_i}{N}.  \tag{18}
\]

which is 1 when there is no damage and 0 when there is total damage. To give more expression to the small values and less expression to the big ones, Eq. (18) is modified as follows:

\[
A_i = \left( \frac{\sum_{j=1}^{n_i} MRVAC_{ji}}{N} \right)^m \times \frac{n_i}{N}.  \tag{19}
\]

where \( m > 1 \). Adding ten intervals, the weighted damage indicator is defined as follows:

\[
WDI = \sum_{i=1}^{10} A_i = \frac{1}{N^{m+1}} \times \sum_{i=1}^{10} (n_i \times \text{Sum}_i)^m, \tag{20}
\]

where

\[
\text{Sum}_i = \sum_{j=1}^{n_i} MRVAC_{ji}; \tag{21}
\]

In Section 4, one can verify that an increase in exponent \( m \) allows for earlier detection of small damages. Five different values for exponent \( m \), 1 to 5, have been tested.

3. Application example

A steel beam with a constant rectangular cross-section was considered. Figure 1 shows the structure used in this study. The dimensions of the beam are 1.002 m in length, 0.035 m in width, and 0.006 m in thickness.

Nine levels of damage, D1 to D9, were considered. To simulate an actual damage condition, a saw cut was made between coordinates 15 and 16 at \( L_1 = 728.5 \) mm, as shown in Figure 1. The width of the crack was kept constant and equal to 1.5 mm. Cut depth \( d \) varied from 0.5 mm to 5 mm. The damaged scenarios are defined as scenarios D1-D9 in Table 1.

Three damages are shown in Figure 2.

Firstly, a numerical study based on the Finite-Element Method was carried out. Then, the experimental modal testing was completed.

4. Numerical analysis

To verify the effectiveness of the damage detection algorithms, introduced in Section 2, from a numerical point of view, the numerical modal analysis based on the finite-element package FEMAP-MSC/NASTRAN was used to simulate the procedure corresponding to the experimental operation. Figure 3 shows the 3D Finite-Element Model used to simulate a beam, considered as the reference structure. The geometry of the beam was assumed as a plate with 0.035 m width, 1.002 m length, and 0.006 m thickness. The meshes consist of 32064 CHEXA elements. The elastic modulus and the density of all parts are \( E = 1.8905 \times 10^7 \) Pa and \( \rho = 7.860 \times 10^3 \) kg/m\(^3\), respectively. Indeed, modal testing was
simulated by FEM analysis using MSC/NASTRAN, applying a unitary impulse load on point No. 3 of the panel; 23 FRFs were computed in the range of 1–800 Hz, with a frequency resolution of 0.25 Hz for 23 selected grids (red color nodes), representing the locations of accelerometers (corresponding to the same point on experimental testing) on the mentioned structure. In this study, to validate and correct the initial FE beam model, a correlation analysis between numerical and experimental beam data is considered for the healthy beam. Generally, correlation analysis is a technique to examine quantitatively and qualitatively the correspondence and difference between analytically and experimentally obtained modal parameters [20]. Dynamic response, namely natural frequencies and mode shapes, were used as the indices for the objective function (that must be minimized) of the correlation analysis. In this case, first, for the mode shape vectors, the Modal Assurance Criterion (MAC) was adopted to make a comparison between numerical and experimental mode shapes. The initial $	ext{Err}_{F\text{r},e}$ values of the natural frequencies of the first seven flexural modes are reported in Table 2. Besides the $	ext{Err}_{F\text{r},e}$ values, also displayed are the absolute differences between numerically and experimentally obtained frequencies prior to the optimization procedure [20].

Finally, Table 3 shows a comparison between the initial (before updating) and final (after updating) design variables. According to the result of the optimization in Table 4, it was inferred that the numerical model simulates the experimental model quite well, and they are matched very well. Therefore, the optimized model of the beam can be used in the next two sections as a representation of the experimental beam structures for application of the proposed damage identification techniques.

The nine damaged scenarios (D1-D9 according to Table 1) were simulated by removing the necessary elements of the beam. For each scenario, the FRF input matrix was generated. In order to simulate an actual measurement, the responses were polluted with a level of 3% random noise. The responses at all frequencies, for each damage scenario, were used to calculate, $\text{GDI}_{PC}$, $\text{DI}_{T\text{h}}$, TDI, and WDI indicators. Figure 4 shows the results obtained with the application of $\text{GDI}_{PC}$ damage indicator for all damage cases, without noise and with 3% added random noise.

Figure 5 shows the results obtained with the application of $\text{DI}_{T\text{h}}$ damage indicator for all damage cases, without noise and with 3% added random noise.

Figure 6 shows the results obtained with the

<table>
<thead>
<tr>
<th>Table 3. Optimization analysis results of beam.</th>
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<tbody>
<tr>
<td>Design variable</td>
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<tr>
<td>-----------------</td>
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<td>$E$ beam</td>
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<table>
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<tr>
<th>Table 2. Comparison of the natural frequencies between numerical and experimental beam data before updating.</th>
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<tr>
<td>Mode (#)</td>
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<td>---------</td>
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<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
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<tr>
<td>4</td>
</tr>
<tr>
<td>5</td>
</tr>
<tr>
<td>6</td>
</tr>
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<td>7</td>
</tr>
</tbody>
</table>
Table 4. Comparison of the natural frequencies between numerical and experimental beam data after updating.

<table>
<thead>
<tr>
<th>Mode (#)</th>
<th>Experimental beam (Hz)</th>
<th>Numerical beam (Hz)</th>
<th>Absolute difference (Hz)</th>
<th>$\text{Err}<em>{F</em>{\text{x}}}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>30.06</td>
<td>29.80</td>
<td>0.26</td>
<td>0.87</td>
</tr>
<tr>
<td>2</td>
<td>81.52</td>
<td>82.14</td>
<td>0.61</td>
<td>0.75</td>
</tr>
<tr>
<td>3</td>
<td>160.53</td>
<td>161.00</td>
<td>0.47</td>
<td>0.30</td>
</tr>
<tr>
<td>4</td>
<td>265.72</td>
<td>266.11</td>
<td>0.38</td>
<td>0.14</td>
</tr>
<tr>
<td>5</td>
<td>395.10</td>
<td>397.45</td>
<td>2.35</td>
<td>0.59</td>
</tr>
<tr>
<td>6</td>
<td>551.63</td>
<td>554.98</td>
<td>3.35</td>
<td>0.61</td>
</tr>
<tr>
<td>7</td>
<td>732.53</td>
<td>738.66</td>
<td>6.41</td>
<td>0.88</td>
</tr>
</tbody>
</table>

Figure 4. Result obtained with the 3PC GDI indicator for all damage levels using simulation data: (a) Without noise, and (b) 3% added noise.

Figure 5. Result obtained with the DIT$^2$ indicator for all damage levels using simulation data: (a) Without noise, and (b) 3% noise.

Figure 6. Result obtained with the TDI indicator for all damage levels using simulation data: (a) Without noise, and (b) 3% noise.
Figure 7. Result obtained with the WDI indicator for all damage levels using simulation data: (a) Without noise, and (b) 3% noise.

Application of TDI damage indicator for all damage cases, without noise and with 3% added random noise.

Figure 7 shows the results obtained with the application of WDI damage indicator for all damage cases, without noise and with 3% added random noise.

The results observed in Figures 4–7 show that all the proposed methods, with the exception of $GDI_{IPC}$, can detect all damages very well. As seen in Figures 5 and 6, a small level of the damages is not so easily detectable with TDI and (DI$_{T^2}$) indicators, while the other two indicators improve the early detection of damage, as they seem able to detect low levels of damage, which is of significance in critical situations. In the case of WDI indicator, this improvement is more evident when higher values of $m$ exponent are used.

The choice of the value of this exponent is directly related to the effect that the damage may have on the structure under study, being especially important for critical structures where the damages should be detected as early as possible. In addition, it is possible to see that all the damage indicators remain stable even in the presence of noise, thanks to the filtering capability of these methods.

5. Experimental testing

The experimental testing was carried out on free-free boundary conditions by suspending the beam using elastic bungees. Twenty-three equally spaced points for translation response measurements were considered, and the test item was excited pseudo-randomly by a Bruel & Kjaer 4809 shaker, powered by a Bruel & Kjaer 2706 power amplifier at several locations. In each test session, four excitation forces were applied at points 3, 7, 12, and 19, one at a time. The force was transmitted through a stinger and measured by a Bruel & Kjaer 8200 force transducer. The responses were measured by 23 CCLD accelerometers. The signals were fed into the Multi-Channel Data Acquisition Unit Bruel & Kjaer 2816 (PULSE) and analyzed directly with the Labshop 6.1 Pulse software from the attached laptop (Dell series 400). The frequency analysis of the beam was 0–800 Hz containing a frequency resolution equal to 0.25 (3200 lines). Hanning windows for force and responses, and 15 averages to obtain the accelerations. Figure 1 shows the location of the shaker as well as the 23 fixed accelerometers. Again, nine various damage scenarios have been analyzed, and the FRF input matrix was measured for each scenario. The responses at all frequencies, for each damage scenario, were used to calculate $GDI_{IPC}$, DI$_{T^2}$, TDI, and WDI indicators. Figure 8 shows the results obtained with the application of $GDI_{IPC}$ damage indicator for all damage levels using experimental testing data.

Figure 9 shows the results obtained with the application of (DI$_{T^2}$) damage indicator for all damage levels using experimental testing data.

Figure 10 shows the results obtained with the application of TDI damage indicator for all damage levels using experimental testing data.

Figure 11 shows the results obtained with the application of WDI damage indicator for all damage levels using experimental testing data.

The results observed in Figures 8–11 show that all the proposed methods can detect and differentiate all damages reasonably well. As one can see in Figure 8, $GDI_{IPC}$ is the method that is more inconsistent. In
algorithms. Two new damage indicators, GDI_{PC} and D_{T2}, were developed, and the results compared with TDI, and WDI are presented in [24]. The following major conclusions can be highlighted:

- All the mentioned damage indicators (GDI_{PC}, D_{T2}) based on PCA and TDI, WDI based on the RVAC correlation factor) are readily available from the measurements. This is very useful because it means that they need neither any modal identification nor any analytic or numerical model of the structure; all of them use directly the frequency response functions without any further treatment or analysis;

- The WDI indicator takes into consideration the correlation values along the frequency range, as well as the number of times they occur, leading to results that are more sensitive as compared to the others for the detection and relative quantification of damage, especially in an early detection stage;

- All the damage indicators are robust enough with respect to noise, thanks to the filtering capability of these methods;

- From all the tested indicators, GDI_{PC} indicator is the one that provides the weakest results when applied to the experimental case;

- Developed methods are robust and efficient and are able to predict structural conditions by analyzing dynamic data changes. The introduced methods require only minimal measurement information to detect damages in structures precisely;

- Several damage detection algorithms are employed to extract the data from the beam specimens testing, and all of them require both healthy and damaged data information to detect the damage.

References


Biographies

Kamal Rezvani was a PhD student graduated from Politecnico di Milano, the Department of Science and Technology of Aerospace, Italy. He is working on Vibration-Based Damage Identification Techniques. He obtained his first undergraduate degree in Mechanical Engineering from Islamic Azad University in 2007. During his undergraduate studies, he learned the fundamental mechanical principles. After that, he continued his education at the same university to receive his MS degree in the field of Engineering-Applied Design with specialty in modeling the metal forming.
Dr. Rezvani not only did a lot of research on modelling and simulation of dynamic processing with different methods (like FEM and Experimental), but also did some research on damage and fracture phenomenon. It should be noted that he was a successful student during his Bachelor and Master programs, known to be a distinguished student. Now, Dr. Rezvani is a Postdoctoral Fellow in Aerospace Engineering in the Faculty of New Sciences & Technologies, University of Tehran.

Nuno Manuel Mendes Maia obtained his BS and MS degrees (1978 and 1985, respectively) in Mechanical Engineering from Instituto Superior Tecnico (IST), Technical University of Lisbon (TU Lisbon). He received his PhD degree in Mechanical Vibrations (1989) from Imperial College, University of London, UK. He had his habilitation in Mechanical Engineering (2001) from Instituto Superior Tecnico, Technical University of Lisbon, TU Lisbon. Dr. Maia has authored around 80 international conferences on the subject of modal analysis and structural dynamics since 1998. He is an Associate Editor of the Shock and Vibration Journal, a member of the Society for Experimental Mechanics (SEM), a member of the International Institute of Acoustics and Vibration (IAV), and of the Portuguese Society of Acoustics (SPA), where he is responsible for the area of vibrations. Currently, he supervises 5 PhD students; he has participated and coordinated various national and international research projects in the area of modal analysis and structural vibrations. As the chairman of the International Conference on Structural Engineering Dynamics (ICEDyn), he is responsible for organizing the conference. His current research interests are modal analysis and modal testing, updating of finite-element models, coupling and structural modification, damage detection in structures, modeling of damping transmissibility in multiple degree-of-freedom systems, and force identification.

Mohammad Hossein Sabour obtained his BS degree (1990) in Mechanical Engineering from University of Tehran. Also, he obtained his MS degree (1993) in the same field from Tarbiat Modares University, and his PhD degree in Aerospace Engineering (2005) from Concordia University, Canada.