

Modification of interfacial tension by considering the effect of porous medium during near miscible gas injection

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Abstract: Gas injection as one of the interesting enhance oil recovery (EOR) methods has been attracted many attentions, hence, numerous experimental and simulation studies of this process were investigated by several researchers. However, an investigation of some parameters such as the effect of injection gas, the effect interfacial tension (IFT) at minimum miscible pressure (MMP), named IFT₀ in the present study, the impact of porous medium on the IFT and subsequently on the gas injection process is still missing. Hence, in this paper, the effect of injection gases, IFT₀, and the influence of porous media on the IFT and then on the fractional flow of gas, saturation curve of gas, and relative permeability of oil and gas were investigated. Depending on the type of injection gases used, our findings indicate that different MMPs can be achieved. Additionally, the type of injection gases affects fractional flow, saturation, and relative permeability curves. Our investigation illustrated that the impact of IFT₀ aforementioned curves is depended on the miscible and immiscible conditions. The effect of porous medium and fracture on the IFT of system have observed, while modified IFT did not affect fractional flow, saturation, and relative permeability curves.

Keywords: Interfacial tension, Gas injection, Enhancing oil recovery, Minimum miscible pressure, Near miscible injection

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1. Introduction

It is essential to increase crude oil production to meet the increasing energy demand in the world. Improved oil recovery techniques, including gas injection, are essential for enhancing oil production [1, 2]. In gas injection method, hydrocarbon gas (i.e., produced and natural gas) and non-hydrocarbon gas (i.e., carbon dioxide, nitrogen) are used [3, 4], and gas can be

35 injected in near miscible, miscible, or immiscible conditions. The main mechanisms in gas
36 injection are reduction in oil viscosity and or interfacial tension (IFT), dissolved gas drive, and
37 volumetric gas injection [3, 4]. The extent to which each mechanism contributes depends on
38 the conditions of the reservoir and fluid [5]. The primary mechanism of gas flooding is the
39 reduction of the IFT and increasing the miscibility of the injection and reservoir fluid [6, 7].

40 Many researchers have investigated experimentally the effect of different factors on the gas
41 injection process. Shariatpanahi et al. [8] carried out two sets of experiments to investigate
42 the behavior of immiscible and water flooding. The researchers conducted their experiments
43 using two-dimensional porous micromodels with fractures. According to their findings, the
44 maximum oil recovery achieved through immiscible gas injection was 60%. Their oil
45 recovery after water flooding was more than the recovery of immiscible gas injection, and it
46 was about 75%. In 2005, Dastyari et al. [9] carried out an experiment to investigate the
47 immiscible gas injection in a micromodel under the influence of gravity. Their results showed
48 that residual oil saturation in case of natural depletion and in a situation that flow was aligned
49 with gravity was lower than gas injection in different angles. Nematzadeh et al. [10]
50 conducted an experimental study of secondary WAG injection in carbonate cores at low
51 temperature and different pressure conditions. Based on their results, before minimum
52 miscible pressure (MMP), enhancing the oil recover was observed by increasing the pressure.
53 They showed that miscible WAG resulted in higher oil recovery. In 2012, Motealleh et al.
54 [11] investigated the performance of WAG in one of Iranian reservoir. Their experimental
55 investigation showed that secondary miscible WAG injection resulted in the highest oil
56 recovery. Yu et al. [12] studied experimentally the efficiencies of nitrogen huff-n-puff and its
57 flooding in shale samples. The findings suggest that the effectiveness of N₂ huff-n-puff was
58 superior to that of N₂ flooding. Although both methods had similar efficiency before a
59 breakthrough, after breakthrough production rate by gas flooding was reduced.

60 Fahandezhsaadi et al. [13] studied N_2 injection for enhanced oil recovery (EOR) and
61 investigated the effects of induced fractures and pressure. They displayed gas breakthrough
62 and onset time of oil production were related to differential pressures and induced fractures.
63 Wang et al. [14] developed representative micromodel to study the EOR mechanism of the
64 injection of the immiscible CO_2 WAG at microscale. They showed injection of WAG after
65 continuous CO_2 injection could influence both carbon dioxide capture storage and oil
66 recovery. Li et al. [15] investigated the effectiveness of different injection strategies,
67 including WAG, cyclic gas, and continuous gas injection, for CO_2 storage and EOR in ultra-
68 low permeability samples. The performance of WAG in both EOR and storage was better
69 than continuous gas injection. The best injection scenario for storage and EOR was cyclic
70 CO_2 injection. Mahzari et al. [16] introduced a novel laboratory approach to study the
71 efficiency of huff-n-puff gas injection in shale oils. Two type of experiments were conducted
72 in a study that in a first one the core was saturated with moveable oil and in a second one the
73 core was saturated with associated gas and dead oil injection was injected in both
74 experiments. Based on their experiments, more oil production was achieved in core that
75 saturated with the live oil. Gandomkar and Sharif [17] examined the efficacy of
76 nanocomposites as direct thickeners for gas injection to address the primary
77 operational/technical challenge associated with gas injection, namely the low viscosity of the
78 gas. Their findings indicated that the P-1-D nanocomposite, consisting of graphene oxide,
79 could substantially enhance the viscosity of the gas. Reduction of IFT as result of utilize gas
80 thickeners was another results of this study. Pore-scale mechanisms of miscible and
81 immiscible gas injection in fractured carbonated was investigated by Chen and Mohanty [18].
82 Their findings indicated that the vugs were fully depleted after miscible gas injection,
83 whereas they remained fully saturated with oil after immiscible gas injection. According to
84 their findings, the ultimate oil recovery during immiscible injection in the matrix was affected

85 by the permeability contrast between the fracture and matrix. During miscible injection, oil
86 recovery was determined by diffusion in the early stages and miscible displacement in the
87 later stages of injection. Zhao et al. [19] studied the impact of citric acid isopentyl ester and
88 citric acid isobutyl ester on dropping the MMP of crude oil and CO₂. Based on their results
89 optimum injected slug size of chemical reagents resulted in reduction of MMP [19]. In
90 addition, more oil recovery was achieved as result of adding citric acid isobutyl ester [19].
91 Simulation of gas injection is another interesting study for most of the researchers. In 2002,
92 Uleberg et al. [20] simulated gas injection in a fractured reservoir. Their simulation was
93 based on compositional reservoir modeling. They developed a method for predicting of MMP
94 and minimum miscibility enrichment (MME) in fractured media. They showed the MMP and
95 MME in the fracture reservoir were higher than in a conventional single-porosity reservoir
96 [20]. Vicencio et al. [21] simulated the injection of nitrogen in a naturally fractured reservoir,
97 and they showed injected fluid, nitrogen, moved straight to the oil-gas contact. The main
98 reason for this phenomenon was destabilizing the displacement by gravity forces. In 2006,
99 Vicencio and Sepehmoori [22] investigated and simulated the injection of nitrogen in a
100 fractured reservoir. Based on their results, the gravity drainage mechanism depended on
101 nitrogen arrival time, depth of reservoir, and size of matrix block. Panfili and Cominelli [23]
102 utilized an Embedded Discrete Fracture Model (EDFM) to simulate gas injection in a
103 fractured reservoir. Based on their results, the proposed method of simulation, EDFM, was a
104 cost-efficient and highly effective solution for the simulation of fracture reservoirs from an
105 industrial viewpoint. Zhu et al. [24] proposed a novel gas injection scheme to improve oil
106 recovery in shale. In this scheme, gas would be injected from one fracture, and oil will be
107 produced from another fracture. Based on their results, the new proposed scheme resulted in
108 improving oil recovery. Wan et al. [25] simulated the potential for enhanced oil recovery
109 (EOR) in shale oil reservoirs through cyclic gas injection. Their results showed, as a contact

110 volume of fracture with matrix was high, its contribution to good productivity was high. Mu
111 et al. [26] introduced an analytical solution for the Buckley-Leverett (BL) equation in gas
112 flooding, taking into consideration miscibility. Wide data analysis conducted by Ahdaya and
113 Imqam [27] to determine the conditions that miscible injection could be applied. Based on
114 their results, CO₂ was the most common injection gas in the miscible gas injection process.
115 Their investigation showed the oil with API gravity of 35.1 to 45 °API and viscosity of 0.25
116 to 1.5 cP was used in the most experimental investigation. Mogensen and Xu [28] studied the
117 miscible nitrogen flooding in a lower permeability, high-temperature carbonate reservoir.
118 Based on their results, different behavior of nitrogen than other injection gas was revealed.
119 They showed that MMP became constant when more than 35% of nitrogen is existed in a
120 injection gas mixture. Kashkooli et al. [29] investigated capture and carbon storage-EOR and
121 they used the dynamic well flow settings as the optimization variables. Based on their results,
122 they proposed redefining the idea of "the more injection, the better". Their results showed the
123 reduction of water production in the optimized case. They showed the fraction of CO₂ that
124 both produced liquid and gas would be reduced in the optimized case.

125 Besides various methods have been developed to simulate the gas injection, BL is a simple
126 analytical method. Based on some sensible and essential assumptions, the theory of fractional
127 flow has been developed. The theory of fractional flow has been started with BL for water
128 injection. Then this theory has been applied for different EOR methods like polymer flooding
129 and gas flooding [30-35]. BL equation is known as an analytical solution for displacement
130 front in two-phase flow. BL equation has been used widely to predict the advance of a fluid
131 displacement front. The rate of penetration of injected water bank in porous media can be
132 predicted by BL equation. In order to obtain an analytical solution for BL equation, some
133 assumptions are considered: Two-phase flow is considered to be linear and horizontal,
134 injection fluid is gas, both displacing and displaced fluid are immiscible, formation contains

135 on a layer, the total flow rate is constant at all section of the medium, injected fluid, gas, is
136 injected at the inlet of medium, porous media is considered to be incompressible, the effect of
137 gravity and capillary pressure is negligible, there is no capillary transition zone and fingering,
138 porous media has a finite length, and it is homogeneous, the boundary conditions of porous
139 media are constant. [36]

140 Although there are several simulation studies in gas injection, the simple method that can
141 consider both immiscible and miscible conditions and consider the impact of porous media is
142 still missing. In this study, the BL method was employed to simulate the gas injection process
143 under both miscible and immiscible conditions, and the impact of the porous media in the gas
144 flooding process was examined. In order to consider the effect of miscibility, modification on
145 the relative permeability and viscosity of fluid was implemented. In addition, IFT was
146 modified to consider the impact of porous media.

147 In the present study, after conducting the validation, the impact of injection gas on the IFT
148 was investigated. Afterward, the effect of IFT at MMP was investigated. The influence of
149 porous media on the IFT and the effect of modified IFT was studied in the next section.
150 Finally, conclusions of the present work were presented.

151 **2. Mathematical model**

152 In this section, a mathematical model and algorithm of study are presented. [Fig. 1](#) shows the
153 flow chart of the present study.

154 The mathematical model of this study is divided into three main sections: a) calculation of
155 IFT, b) modification of relative permeability, c) calculation of fractional flow and saturation
156 of gas.

157

158

Fig. 1: The flowchart of the numerical model

159

160 2.1 Calculation of IFT

161 IFT is known as one of the main parameters that affects the behavior of fluids in a reservoir.
162 It has an essential role in the oil industry, specifically in EOR. Several methods, both
163 experimental and mathematical methods, have been existed to calculate the IFT of
164 hydrocarbon fluids. Two common methods for the calculation of IFT are rising bubble and
165 pendant drop methods [37]. In the first method, a bubble will be upward in the denser phase.
166 In the second one heavier phase must be suspended in the lighter phase, and then by using
167 Young-Laplace equation, IFT can be determined [37]. In addition to different experimental
168 methods for the calculation of IFT, several empirical correlations can estimate the IFT of
169 system [37]. Ramey [38] modified Weinaug-Katz correlation for IFT, and in this study,
170 Ramey's correlation was utilized to calculate the IFT of the oil-gas system:

171

$$\sigma_{go}^{\frac{1}{4}} = P_o \left(x_o \frac{\rho_o}{M_{og}} - y_o \frac{\rho_g}{M_{go}} \right) - P_g \left(x_g \frac{\rho_o}{M_{og}} - y_g \frac{\rho_g}{M_{go}} \right) \quad (1)$$

172

173 Where x_o , x_g , y_o , and y_g show mole fraction of components in the oil phase and gas phase,
174 respectively. In the above equation, the density of oil and gas is showed by ρ_o and ρ_g ,
175 respectively. M_{og} and M_{go} denote the average molecular weight of oil and gas phase,
176 respectively; P_o and P_g denote the Parachor equation suggested by Whitson and Brule; σ_{go}
177 displays the IFT of oil and gas.

178 The following formula was used to calculate the aforementioned parameters [38, 39]:

179

$$M_o = \frac{6084}{(\gamma_{API} - 5.9)} \quad (2)$$

$$M_g = 28.97 \times \gamma_g \quad (3)$$

$$P_o = (2.376 + 0.0102 \times \gamma_{API}) \times M_o \quad (4)$$

$$P_g = (25.2 + 2.86 \times M_o) \quad (5)$$

$$x_o = \left(1 + \frac{7.521 \times 10^{-6} \times M_o \times R_s}{\gamma_o} \right)^{-1} \quad (6)$$

$$x_g = 1 - x_o \quad (7)$$

$$y_o = \left(1 + \frac{7.521 \times 10^{-6} \times M_o}{\gamma_o \times r_v} \right)^{-1} \quad (8)$$

$$y_g = 1 - y_o \quad (9)$$

$$\rho_o = \frac{\gamma_o + 2.179 \times 10^{-4} \times \gamma_g \times R_s}{B_o} \quad (10)$$

$$\rho_g = 9.3184 \times 10^{-2} \times \frac{P \times M_{go}}{62.4 \times Z \times T} \quad (11)$$

$$M_{og} = (x_o \times M_o + x_g \times M_g) \quad (12)$$

$$M_{go} = (y_o \times M_o + y_g \times M_g) \quad (13)$$

180

181 In the above equation, the molecular weight of gas and oil is shown by M_g and M_o ,

182 respectively. Here, R_s presents the solution gas-oil ratio, B_o represents oil formation volume

183 factor, and γ_o denotes the specific gravity of the oil. The specific gravity of oil can be related

184 to γ_{API} : $\gamma_{API} = \frac{141.5}{\gamma_o} - 131.5$. In addition, r_v represents vaporized oil in the gas phase. There

185 is a general assumption is used with the black oil approach. In this assumption $r_v = 0$,

186 therefore, $y_o = 1$, and $y_g = 0$. γ_g is the specific gravity of gas, and P , Z , and T display
 187 pressure, compressibility factor, and temperature. It is worthwhile to mention that there are
 188 several empirical correlations to compute the oil formation volume factor, compressibility
 189 factor, and solution gas-oil ratio. In our study, the following formula was used to calculate the
 190 above-mentioned parameters:

191 Sutton [40] suggested the following correlation to calculate critical temperature and pressure.

192

$$T_{pc} = 169.2 + 349.5 \times \gamma_g - 74 \times \gamma_g^2 \quad (14)$$

$$P_{pc} = 756.8 - 131.07 \times \gamma_g - 3.6 \times \gamma_g^2 \quad (15)$$

$$T_{pr} = \frac{T}{T_{pc}} \quad (16)$$

$$P_{pr} = \frac{P}{P_{pc}} \quad (17)$$

$$tpr = \frac{1}{T_{pr}} \quad (18)$$

193

194 In the above equation, T_{pc} and T_{pr} display pseudocritical and pseudoreduced temperature; P_{pc}
 195 and P_{pr} are pseudocritical and pseudoreduced pressure.

196 For the compressibility factor, Brill and Beggs' correlation was employed [41]:

197

$$Z = A + \frac{1-A}{e^B} + C \times P_{pr}^D \quad (19)$$

$$A = 1.39 \times (T_{pr} - 0.92)^{0.5} - 0.36 \times T_{pr} - 0.10 \quad (20)$$

$$B = (0.62 - 0.23 \times T_{pr}) \times P_{pr} + \left(\frac{0.066}{T_{pr} - 0.86} - 0.037 \right) P_{pr}^2 + \frac{0.32 \times P_{pr}^2}{10^E} \quad (21)$$

$$C = 0.132 - 0.32 \times \log(T_{pr}) \quad (22)$$

$$D = 10^F \quad (23)$$

$$E = 9 \times (T_{pr} - 1) \quad (24)$$

$$F = 0.3106 - 0.49 \times T_{pr} + 0.1824 \times T_{pr}^2 \quad (25)$$

198

199 Brill and Beggs' correlation constants are represented by the letters *A* to *F*. The Standing

200 correlation was utilized to compute the solution gas oil ratio and the formation volume factor

201 [42]:

202

$$R_s = \gamma_g \times \left[\left(\frac{P}{18.2} + 1.4 \right) \times 10^a \right]^{1.2048} \quad (26)$$

$$a = 0.00091 \times (T - 460) - 0.0125 \times \gamma_{API} \quad (27)$$

$$B_o = 0.9759 + 0.000120 \times \left[R_s \times \left(\frac{\gamma_g}{\gamma_o} \right)^{0.5} + 1.25 \times (T - 460) \right]^{1.2} \quad (28)$$

203

204 **2.2 Calculation of the relative permeability of the gas-oil system**

205 One of the main parameters affected by IFT is the relative permeability of the reservoir

206 fluids. Researchers have been proposed different models to predict the relative permeability.

207 Most of these models are tried to interpolate the relative permeability curves at the miscible

208 and immiscible conditions. A first model in this type was proposed by Coats [43], and this
 209 model was a function of IFT:

210

$$K_{RO} = F_K \times K_{ro}^{imm} + (1 - F_K) \times K_{ro}^{mis} \quad (29)$$

$$K_{RG} = F_K \times K_{rg}^{imm} + (1 - F_K) \times K_{rg}^{mis} \quad (30)$$

211

212 Where K_{RO} is a modified oil relative permeability which considered a both miscible, K_{ro}^{mis} ,
 213 and a immiscible, K_{ro}^{imm} , oil relative permeability. In addition, K_{RG} shows a modified gas
 214 relative permeability and the same as the modified oil relative permeability, both a miscible,
 215 K_{rg}^{mis} , and a immiscible, K_{rg}^{imm} , relative permeability are considered in these parameters. F_k is
 216 a relative permeability interpolation parameter that related to the IFT [43]:

217

$$F_K = \min \left[1, \left(\frac{\sigma}{\sigma_0} \right)^N \right] \quad (31)$$

218

219 In the above equation, σ and σ_0 are the IFT and the IFT at MMP, respectively [43].

220

$$S_{or} = F_K \times S_{or}^{imm} \quad (32)$$

$$S_{gi} = F_K \times S_{gi}^{imm} \quad (33)$$

$$S_{gn} = \frac{S_g - S_{gi}}{1 - S_{gi} - S_{or}} \quad (34)$$

221

222 Corey-Brooks [44] correlation was employed to compute the relative permeability of gas and
 223 oil under immiscible conditions:

$$K_{ro}^{imm} = K_{ro} \times (1 - S_{gn})^{n_o} \quad (35)$$

$$K_{rg}^{imm} = K_{rg} \times S_{gn}^{n_g} \quad (36)$$

$$K_{ro}^{mis} = (1 - S_{gn})^{n_m} \quad (37)$$

$$K_{rg}^{mis} = S_{gn}^{n_m} \quad (38)$$

224
 225 S_{or} and S_{gi} are a modified residual oil saturation, and an irreducible gas-phase saturation,
 226 respectively, and S_{or}^{imm} and S_{gi}^{imm} display the same parameters at an immiscible conditions.
 227 K_{ro} and K_{rg} present an oil relative permeability at an irreducible gas saturation and a gas
 228 relative permeability at a residual oil saturation, respectively. n_g and n_o , are an gas and a oil
 229 exponent for the Brooks-Corey functions. These parameters can be obtained through an
 230 immiscible relative permeability curve. n_m is a relative permeability index and in this paper
 231 n_m is considered 1.1.

232

233 **2.3 Calculating the viscosity of oil and gas**

234 The injection of gas results in a decrease in the viscosity of the oil, making it crucial to
 235 modify the viscosity of both the oil and gas for accurately simulating the gas injection
 236 process. In the present study, Todd-Longstaff [45] model was employed to calculate the
 237 effective gas and oil viscosity:

238

$$\mu_{oeff} = \mu_o^{1-\omega} \times \mu_m^\omega \quad (39)$$

$$\mu_{geff} = \mu_g^{1-\omega} \times \mu_m^\omega \quad (40)$$

$$\left(\frac{1}{\mu_m}\right)^{\frac{1}{4}} = \frac{S'_g}{S'_n} \times \left(\frac{1}{\mu_g}\right)^{\frac{1}{4}} + \frac{S'_o}{S'_n} \times \left(\frac{1}{\mu_o}\right)^{\frac{1}{4}} \quad (41)$$

$$S'_o = S_o - S_{or} \quad (42)$$

$$S'_g = S_g - S_{gi} \quad (43)$$

$$S'_n = S'_o - S'_g \quad (44)$$

239

240 Here μ_m shows a mixing viscosity and ω presents a mixing factor of the viscosity, and in this

241 study, $\omega = \frac{1}{3}$. In addition, the fluids effective viscosity and the fluids viscosity are presented

242 by μ_{oeff} , μ_{oeff} , μ_{oeff} , and μ_{oeff} , respectively.

243

244 **2.4 Calculating saturation and fractional flow of gas**

245 The BL equation was employed to measure the fractional flow of gas and gas saturation.

246 Derivation of the equation can be found in the different literature. The final formulas that

247 were used in this study are as follows [36]:

248

$$f_g = \frac{S_g^2}{S_g^2 + (1+S_g)^2 \times V} \quad (45)$$

$$\frac{df_g}{dS_g} = \frac{2 \times V \times (S_g - 1) \times S_g}{\left(V \times (S_g - 1)^2 + S_g^2\right)^2} \quad (46)$$

$$PVI = \frac{q_t \times t}{Area \times L \times \phi} \quad (47)$$

$$x_{sg} = PVI \times L \times \left(\frac{df_g}{dS_g} \right)_{S_g} \quad (48)$$

249

250 In the above equation, f_g shows a fractional flow of gas; $\frac{df_g}{dS_g}$ denotes the derivative of the

251 fractional flow of gas with respect to the gas saturation; V is a ratio of the viscosity ($\frac{\mu_g^{eff}}{\mu_o}$);

252 PVI is a dimensionless pore volume injection, $Area$, L , and ϕ display a cross-section area,

253 length of the domain, and porosity of the domain, respectively; q_t and t show a total injection

254 rate and an injection time. In addition, x_{sg} shows a distance moved by a specific S_g contour.

255

256 **3. Results and discussion**

257 **3.1 Numerical simulation**

258 Each step of the numerical simulation is shown in [Fig. 1](#), and the inputs parameters are

259 presented in [Table 1](#).

260

261 Table 1: Input parameters and their values used in numerical simulation

262

263 Model validation is the first step in an each simulation study. Hence, some of the existing

264 experimental findings and simulation studies were utilized to validate the developed model.

265 The first step involved evaluating the developed model for the density of reservoir oil, oil

266 formation volume factor, and solution gas-oil ratio using existing experimental data. [Fig. 2](#)

267 shows the comparison between the experimental value of the density of oil, oil formation

268 volume factor, solution gas-oil ratio, and fluid's relative permeability with their predicted

269 value. As shown in Fig. 2, the developed model in this study can predict the above-mentioned
270 properties very well, and its error in the prediction is low.

271

272 Fig. 2: a) Experimental and predicted oil density vs. pressure, experimental and predicted oil formation volume
273 factor vs. pressure, solution gas-oil ratio vs. pressure,, and relative permeability of oil and gas versus saturation

274

275 In the last step of validation, the predicted fractional flow curve of the present study compare
276 with the result of Mu et al. [26]. Fig. 3 shows the comparison of the fractional flow, and a
277 good match between Mu et al.'s study and our study is seen.

278

279 Fig. 3: Comparison predicted fractional flow of present study with Mu et al. [26]

280

281 **3.2 Effect of injection gas on the IFT**

282 This section presents an investigation into the impact of injection gas on IFT and,
283 consequently, on the relative permeability of gas and oil, gas saturation profile, and gas
284 fractional flow. Fig. 4 shows the IFT between different injection gases and oil.

285

286 Fig. 4: IFT between oil and injected gases

287

288 As shown in Fig. 4, MMP of carbon dioxide is less than two other gases, and methane has
289 higher MMP than nitrogen. Based on Fig. 4, near miscible pressure and IFT at MMP (IFT₀)
290 of three-injection gas were determined. We determined the near miscible pressure based on
291 the point that the IFT reached the value of less than 1 mN/m. Therefore, for carbon dioxide,
292 nitrogen, and methane, IFT₀ was 0.99 at a pressure of 796, 1518, and 3351 psi, respectively.
293 In order to study the impact of injection gases on the relative permeability, saturation curve
294 and fractional flow of gas, three injection pressures, 500, 1000 and 5000 psi, were used. At
295 500 psi, F_k was 1 (based the Equation (31)); therefore, the immiscible situation was

296 dominated. As shown in Fig. 5, once injected gases were in the immiscible condition, there
297 was not seen any impact on fractional flow, saturation, and relative permeability curves.

298

299 Fig. 5: Impact of injection gas on fractional flow, saturation, and relative permeability curves at injection
300 pressure of 500 psi

301

302 The second scenario involved injecting gas at a pressure of 1000 psi. Based on the Equation
303 (31), in this situation, CO₂ is injected as the miscible gas, while N₂ and CH₄ are injected as
304 the immiscible gases. As shown in Fig. 6, CO₂ resulted in an alteration in the relative
305 permeability of oil and gas and shifted their relative permeability to the right side.
306 Additionally, when CO₂ was used as an injected gas, a breakthrough occurred (subplot (b) of
307 Fig. 6). Furthermore, the effect of CO₂ in miscible conditions on the fractional flow curve is
308 shown in subplot (c) of Fig. 6. CO₂ is heavier than two other gases, therefore sooner than two
309 other ones reach to the miscible condition. As it is injected in the miscible conditions, it
310 moves faster in a porous media. Therefore, at the same time, it reaches the end of the domain
311 and has a breakthrough. In addition, it increases the relative permeability of oil more than the
312 other two gases.

313

314 Fig. 6: Impact of injection gas on fractional flow, saturation, and relative permeability curves at injection
315 pressure of 1000 psi

316

317 The injection pressure in the last scenario was set at 5000 psi, as depicted in Fig. 7. In this
318 scenario, all gasses are injected in the miscible conditions. As shown in subplot (a) of Fig. 7,
319 oil relative permeability once injection gas was CO₂, lied on the left side of other gases' oil
320 relative permeability. In addition, gas relative permeability in a scenario that CO₂ was used
321 as an injection gas was staying out on the right side of other gases. Oil and gas relative
322 permeability for a scenario in which CH₄ was the injection fluid was between two other

323 gases' relative permeability. The impact of injection fluid on the fractional flow curve is
324 presented in subplot (c) of Fig. 7. By increasing the injection pressure, all three gases are
325 injected as the miscible gases, a breakthrough of all gases occurred (Subplot (b) of Fig. 7). In
326 this case, the relative permeability of gas shifted to the left, while the relative permeability of
327 oil shifted to the right due to the presence of nitrogen and methane. The impact of nitrogen on
328 fractional flow, saturation, and relative permeability curves is more than two other gases.
329 Carbon dioxide, as the heavier gas among three injection gases, has less impact on fractional
330 flow, saturation, and relative permeability curves. The primary reason for this phenomenon is
331 that carbon dioxide has a lower IFT than the other two gases.

332

333 Fig. 7: Impact of injection gas on fractional flow, saturation, and relative permeability curves at injection
334 pressure of 5000 psi

335

336 3.3 Effect of IFT0

337 Four IFT0 for three gases were studied to investigate the effect of the IFT at MMP on
338 fractional flow, saturation, and relative permeability curves. Fig. 8-Fig. 11 show the impact of
339 IFT0 on fractional flow, saturation, and relative permeability curves. The injection pressures
340 were 500, 1000, 3000, and 5000 psi and carbon dioxide was used as an injection fluid. As
341 shown in subplot (a) of Fig. 8 through Fig. 11, an increase in the IFT0 results in decrease in
342 the relative permeability of oil and an increase in the relative permeability of gas. There is no
343 clear difference between IFT0 of 0.001 and 1 in this case. The front of gas at higher IFT0 was
344 more than the lower one. Therefore, higher IFT0 resulted in more distance move by the
345 injection gas at the same conditions (Subplot (b) of Fig. 8-Fig. 11). Subplot (c) of Fig. 8-Fig.
346 11 show increasing in the IFT0 shifted the fractional flow curve.

347

348 Fig. 8: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for carbon dioxide at an
349 injection pressure of 500 psi

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Fig. 9: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for carbon dioxide at an injection pressure of 1000 psi

Fig. 10: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for carbon dioxide at an injection pressure of 3000 psi

Fig. 11: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for carbon dioxide at an injection pressure of 5000 psi

The same as [Fig. 8-Fig. 11](#), [Fig. 12-Fig. 15](#) show the impact of IFT0 at different injection pressures on fractional flow, saturation, and relative permeability curves. In this part, methane was used as an injection fluid. As shown in [Fig. 12](#) and [Fig. 13](#), IFT0 is not affected in the outputs of the model. However, by increasing the injection pressure, 3000 and 5000 psi, the effect of IFT0 on each curve is evident. In other words, by increasing the injection pressure, the injection gas moves to miscible conditions; therefore, its effect on the outputs of the model was observed. Hence, if gas is injected in the immiscible conditions, the effect of IFT0 on the outputs of the model is negligible. Nevertheless, if the injection pressure is increased and the gas transitions to the miscible condition, the impact of IFT0 becomes apparent.

Fig. 12: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an injection pressure of 500 psi

Fig. 13: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an injection pressure of 1000 psi

381

382 Fig. 14: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an
383 injection pressure of 3000 psi

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385

386 Fig. 15: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an
387 injection pressure of 5000 psi

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389 The impact of IFT0 on fractional flow, saturation, and relative permeability curves at the
390 different pressures and once N₂ was used as an injection fluid is presented in [Fig. 16-Fig. 19](#).

391 At first injection pressure, 500 psi, the effect of IFT0 is negligible. By increasing the injection
392 pressure, alteration on fractional flow, saturation, and relative permeability curves is obvious.

393 Similar to the other two gases, increasing the injection pressure for nitrogen and transitioning
394 to the miscible condition impacts the fractional flow, saturation, and relative permeability

395 curves.

396

397 Fig. 16: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
398 injection pressure of 500 psi

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400

401 Fig. 17: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
402 injection pressure of 1000 psi

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404

405 Fig. 18: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
406 injection pressure of 3000 psi

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408

409 Fig. 19: Impact of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
410 injection pressure of 5000 psi

411

412 3.4 Effect of modified IFT

413 In the most experimental and simulation studies, IFT of the bulk medium was used for
414 calculation, and the effect of porous media was missed. However, the property of the porous
415 media, i.e., porosity and permeability, affected the IFT. This section presents the modification
416 of IFT for CO₂ injection, taking into account the effect of porous media, using the developed
417 code. Afterward, based on modified IFT, fractional flow, saturation, and relative permeability
418 curves were recalculated. As the developed code calculated the IFT of bulk and porous
419 media-based compositional model, we used compositional model for the bulk medium.
420 Therefore, we can have a better comparison between IFT of the bulk and the porous media. r_p
421 was used to show the impact of the porous media on the IFT:

$$422 \quad r_p = \sqrt{\frac{k}{\phi}} \quad (49)$$

423
424 Where k and ϕ show permeability and porosity, respectively. Based on [Table 1](#), for our
425 porous media, the value of r_p is 10. [Table 2](#) shows the IFT of crude oil- CO₂ at two different
426 pressure for the both bulk and the porous media.

427
428 Table 2: IFT of crude oil-CO₂ at two-injection pressure for bulk and porous media

429
430 [Fig. 20](#) and [Fig. 21](#) show the impact of the bulk and the porous media on fractional flow,
431 saturation, and relative permeability curves at two injection pressures of 500 and 1000 psi. It
432 is worthwhile to mention that in the both cases, the value of the IFT₀ was 1.

433
434 Fig. 20: Impact of bulk and porous media on fractional flow, saturation, and relative permeability curves for
435 carbon dioxide as an injection gas at an injection pressure of 500 psi

436

437 Fig. 21: Impact of bulk and porous media on fractional flow, saturation, and relative permeability curves for
438 carbon dioxide as an injection gas at an injection pressure of 1000 psi

439

440 As shown in Table 2, the medium has an effect on IFT; however, the influence of medium on
441 fractional flow, saturation, and relative permeability curves was negligible. The primary
442 reason for this phenomenon is F_K , which influences fractional flow, saturation, and relative
443 permeability curves. As the value of F_K or both mediums was the same, no significant effect
444 on the aforementioned curves was observed.

445 3.5 Effect of fracture

446 This section presents an investigation into the impact of fractures on IFT, fractional flow,
447 saturation, and relative permeability curves. In this study, k and φ for the fracture reservoir
448 are 13.57 md and 0.1638; therefore, the r_p of the fracture medium is 3000. Table 3 shows the
449 IFT of crude oil-CO₂ for the fracture medium in two-injection rate.

450

451 Table 3: IFT of crude oil-CO₂ at two-injection pressure for fracture media

452

453 Fig. 22 presents the effect of the fracture on fractional flow, saturation, and relative
454 permeability curves. As shown in Table 3, in both injection pressure, the IFT is more than
455 IFT₀; therefore, there is not seen any effect of two different injection pressures on the
456 aforementioned curves.

457

458 Fig. 22: Impact of fracture medium on fractional flow, saturation, and relative permeability curves for carbon
459 dioxide as an injection gas at an injection pressure of 500 psi and 1000 psi

460

461 In the present study, based on BL method, a process of gas injection in the both miscible and
462 the immiscible conditions was studied. Modification on the relative permeability and

463 viscosity of fluids cause the developed code can investigate the gas injection in the
464 immiscible, miscible, and the near miscible conditions. This advantage of the developed code
465 can give a suitable view of the performance of the injection gas before the process of EOR in
466 the reservoir. By this modification, the performance of each injection gas at the various
467 conditions can be checked and based on the achieved results a suitable decision can be made for
468 the selection of EOR method. Another advantage of the developed code is considering the
469 impact of porous media. By considering the effect of the porous media on gas injection
470 process, accurate simulation of gas injection in the reservoir can be achieved. In order to
471 better simulate and mimic the process of the gas injection, variations in the composition of
472 injection and reservoir fluids during gas injection must be considered and investigated. In the
473 developed code, the mechanism of gas injection cannot be investigated and determined.

474

475 **4. Conclusions**

476 The current study investigated the gas flooding process, focusing on the effects of different
477 gases, modified IFT, and IFT at MMP, on fractional flow, saturation, and relative
478 permeability curves. The key findings of this study can be summarized as follows:

479 1. Different gases resulted in different IFT and MMP. Methane has higher IFT and lower IFT
480 belongs to carbon dioxide. The primary reason for this phenomenon is the molecular weight
481 of the gases. Carbon dioxide has a higher molecular weight and lower IFT than the other two
482 gases. However, methane has a lower molecular weight, and it has higher IFT.

483 2. Under an injection pressure of 500 psi, the injection gas had no discernible impact on the
484 fractional flow, saturation, and relative permeability curves. However, increasing the
485 injection pressure to 1000 psi resulted in fractional flow, saturation, and relative permeability
486 curves being influenced by the injection gas.

487 3. Nitrogen and methane have lower molecular weight than carbon dioxide, therefore shift
488 relative permeability of gas to the right side and the relative permeability of oil to the left
489 side.

490 4. Carbon dioxide as a heavier gas resulted to breakthrough at injection pressure of 1000 psi.

491 5. The impact of injection gas on fractional flow, saturation, and relative permeability curves
492 is dependent on factors such as injection pressure, IFT0, and the condition of the injection
493 gas. At injection pressure of 500 psi, all three gases are in immiscible condition. IFT0, IFT at
494 near miscible pressure, is lower than the IFT of each gas and F_k was 1; therefore, there was
495 not any difference among injection gases. However, by increasing injection pressure,
496 fractional flow, saturation, and relative permeability curves affected by injection gases. In
497 other words, IFT0 can affected the output of model in the miscible conditions.

498 6. Porous media and fracture affected IFT severely, however as IFT0 was 1, F_k for both
499 medium and injection pressure was the same. Therefore, the impact of these mediums on
500 fractional flow, saturation, and relative permeability curves is negligible.

501

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504 providing financial support for this study.

505

506 **Abbreviations**

507 *Nomenclature*

508 EOR = Enhanced Oil Recovery

509 MMP = Minimum miscibility pressure

510 MME = Minimum miscibility enrichment

511 BL = Buckley-Leverett

512 *Symbols*

513 x_o = Mole fraction of oil in oil phase

514 x_g = Mole fraction of gas in oil phase

515 y_o = Mole fraction of oil in gas phase

516 y_g = Mole fraction of gas in gas phase

517 ρ_o = Density of oil phase, $\frac{lbm}{ft^3}$

518 ρ_g = Density of gas phase, $\frac{lbm}{ft^3}$

519 M_{og} = Average molecular weight of oil phase, $\frac{lbm}{lbmol}$

520 M_{go} = Average molecular weight of gas phase, $\frac{lbm}{lbmol}$

521 P_o = Parachor equation for oil phase

522 P_g = Parachor equation for gas phase

523 σ_{go} = IFT of gas and oil, $\frac{dynes}{cm}$

524 M_o = Molecular weight of oil phase, $\frac{lbm}{lbmol}$

525 M_g = Molecular weight of gas phase, $\frac{lbm}{lbmol}$

526 R_s = Solution gas oil ratio, $\frac{scf}{STB}$

527 B_o = Oil formation volume factor, $\frac{bbl}{STB}$

528 γ_o = Specific gravity of oil

529 γ_g = Specific gravity of gas

530 γ_{API} = American Petroleum Institute

531 r_v = Vaporized oil in the gas phase, $\frac{scf}{STB}$

532 p = Pressure, *psia*

533 Z = Compressibility factor

- 534 T = Temperature, R
- 535 P = Pressure, $psia$
- 536 T_{pc} = Pseudocritical temperature, R
- 537 P_{pc} = Pseudocritical pressure, $psia$
- 538 T_{pr} = Pseudoreduced temperature
- 539 P_{pr} = Pseudoreduced pressure
- 540 A-F = Constants for Brill and Beggs' calculation to calculate compressibility factors
- 541 K_{RO} = Oil relative permeability
- 542 K_{RG} = Gas relative permeability
- 543 K_{ro}^{mis} = Miscible oil relative permeability
- 544 K_{rg}^{mis} = Miscible gas relative permeability
- 545 K_{ro}^{imm} = Immiscible oil relative permeability
- 546 K_{rg}^{imm} = Immiscible gas relative permeability
- 547 F_k = Relative permeability interpolation parameter
- 548 σ_0 = Interfacial tension at minimum miscible pressure, $\frac{dynes}{cm}$
- 549 σ = Interfacial tension at different pressure, $\frac{dynes}{cm}$
- 550 S_{or} = Residual oil saturation
- 551 S_{gi} = Irreducible gas phase saturation
- 552 S_{or}^{imm} = Residual oil saturation at immiscible condition
- 553 S_{gi}^{imm} = Irreducible gas phase saturation at immiscible condition
- 554 K_{ro} = Oil relative permeability at irreducible gas saturation
- 555 K_{rg} = Gas relative permeability at residual oil saturation
- 556 n_o = Gas exponent for Brooks-Corey functions
- 557 n_g = Oil exponent for Brooks-Corey functions

- 558 n_m = Relative permeability index
- 559 n_m = Read-in exponent
- 560 $\mu_{o\text{eff}}$ = Oil effective viscosity, *mPa.s*
- 561 $\mu_{g\text{eff}}$ = Oil effective viscosity, *mPa.s*
- 562 μ_o = Oil viscosity, *mPa.s*
- 563 μ_g = Gas viscosity, *mPa.s*
- 564 μ_m = Mixing viscosity, *mPa.s*
- 565 ω = Mixing factor
- 566 f_g = Fractional flow of gas
- 567 $\frac{df_g}{dS_g}$ = Derivative of the fractional flow of gas with respect to gas saturation
- 568 V = Viscosity ratio
- 569 PVI = Dimensionless pore volume
- 570 $Area$ = Cross section area, m^2
- 571 L = Length of investigated domain, *m*
- 572 ϕ = Porosity of domain, %
- 573 q_t = Total injection rate, $\frac{m^3}{hr}$
- 574 t = Injection time, *hr*
- 575 x_{S_g} = Distance moved by a specific S_g contour, *m*

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577

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690

691 **Tables and figures caption**

692 **Tables:**

693 Table 1: Inputs parameters and their values used in numerical simulation

694 Table 2: IFT of crude oil-CO₂ at two-injection pressure for bulk and porous media

695 Table 3: IFT of crude oil-CO₂ at two-injection pressure for fracture media

696

697 **Figures:**

698 Fig. 1: The flowchart of the numerical model

699 Fig. 2: a) Experimental and predicted solution gas-oil ratio vs. pressure, b) Experimental and predicted oil
700 formation volume factor vs. pressure, c) experimental and predicted oil density vs. pressure

701 Fig. 3: Schematic of an ANFIS model with two inputs parameter three injection pressures of 14, 22, and 30 MPa

702 Fig. 4: IFT between oil and injected gases

703 Fig. 5: Effect of injection gas on fractional flow, saturation, and relative permeability curves at injection
704 pressure of 500 psi

705 Fig. 6: Effect of injection gas on fractional flow, saturation, and relative permeability curves at injection
706 pressure of 1000 psi

707 Fig. 7: Effect of injection gas on fractional flow, saturation, and relative permeability curves at injection
708 pressure of 5000 psi

709 Fig. 8: Effect of IFT₀ on fractional flow, saturation, and relative permeability curves for carbon dioxide at an
710 injection pressure of 500 psi

711 Fig. 9: Effect of IFT₀ on fractional flow, saturation, and relative permeability curves for carbon dioxide at an
712 injection pressure of 1000 psi

713 Fig. 10: Effect of IFT₀ on fractional flow, saturation, and relative permeability curves for carbon dioxide at an
714 injection pressure of 3000 psi

715 Fig. 11: Effect of IFT₀ on fractional flow, saturation, and relative permeability curves for carbon at an injection
716 pressure of 5000 psi

717 Fig. 12: Effect of IFT₀ on fractional flow, saturation, and relative permeability curves for methane at an
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720 injection pressure of 1000 psi
- 721 Fig. 14: Effect of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an
722 injection pressure of 3000 psi
- 723 Fig. 15: Effect of IFT0 on fractional flow, saturation, and relative permeability curves for methane at an
724 injection pressure of 5000 psi
- 725 Fig. 16: Effect of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
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730 injection pressure of 3000 psi
- 731 Fig. 19: Effect of IFT0 on fractional flow, saturation, and relative permeability curves for nitrogen at an
732 injection pressure of 5000 psi
- 733 Fig. 20: Effect of bulk and porous media on fractional flow, saturation, and relative permeability curves for
734 carbon dioxide as an injection gas at an injection pressure of 500 psi
- 735 Fig. 21: Effect of bulk and porous media on fractional flow, saturation, and relative permeability curves for
736 carbon dioxide as an injection gas at an injection pressure of 1000 psi
- 737 Fig. 22: Effect of fracture medium on fractional flow, saturation, and relative permeability curves for carbon
738 dioxide as an injection gas at an injection pressure of 500 psi and 1000 psi

Table 1

Inputs parameters	Value
P_b (Bubble point pressure)	1379 psi
T_{res} (Reservoir temperature)	643.77 R
API (API of reservoir oil)	19.96
L (Length of the simulated domain)	200 m
μ_o (Oil viscosity)	1.81 mPa.s
μ_g (Gas viscosity)	0.035 mPa.s
K_{ro} (Oil relative permeability at irreducible gas saturation)	0.9
K_{rg} (Gas relative permeability at residual oil saturation)	0.6181
S_{or} (Residual oil saturation)	0.24
S_{oi} (Initial saturation of oil)	0.95
S_{gi} (Initial saturation of gas)	0.05
n_o	2.1079
n_g	2.9852
N	1/4
k	20 md
φ	0.2

740

741

Table 2

Injection pressure (psi)	IFT of bulk media (mN/m)	IFT of porous media (mN/m)
500	9.48	3.13
1000	7.26	2.18

742

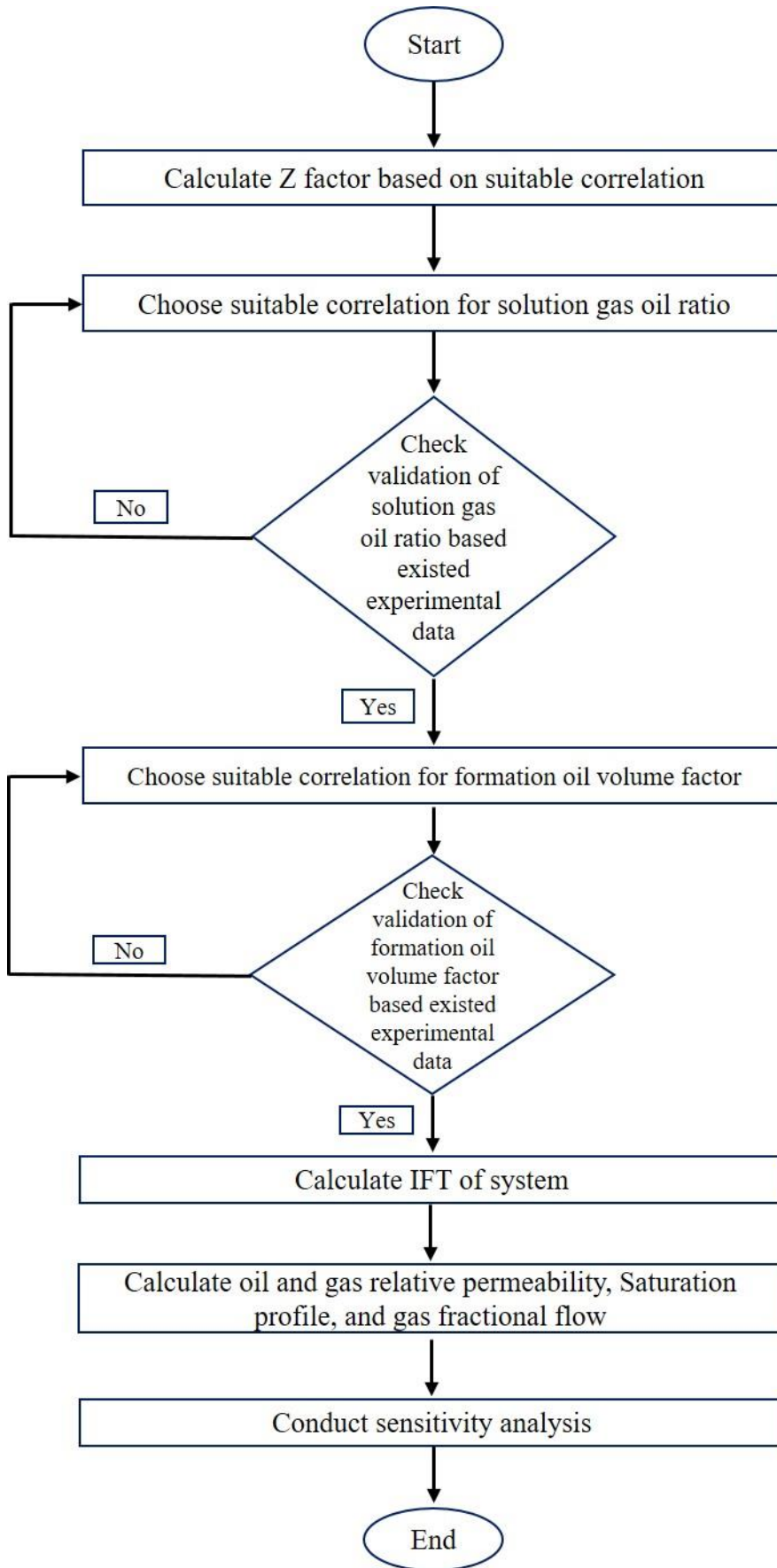
743

Table 3

Injection pressure (psi)	IFT of fracture media (mN/m)
500	9.38
1000	7.18

744

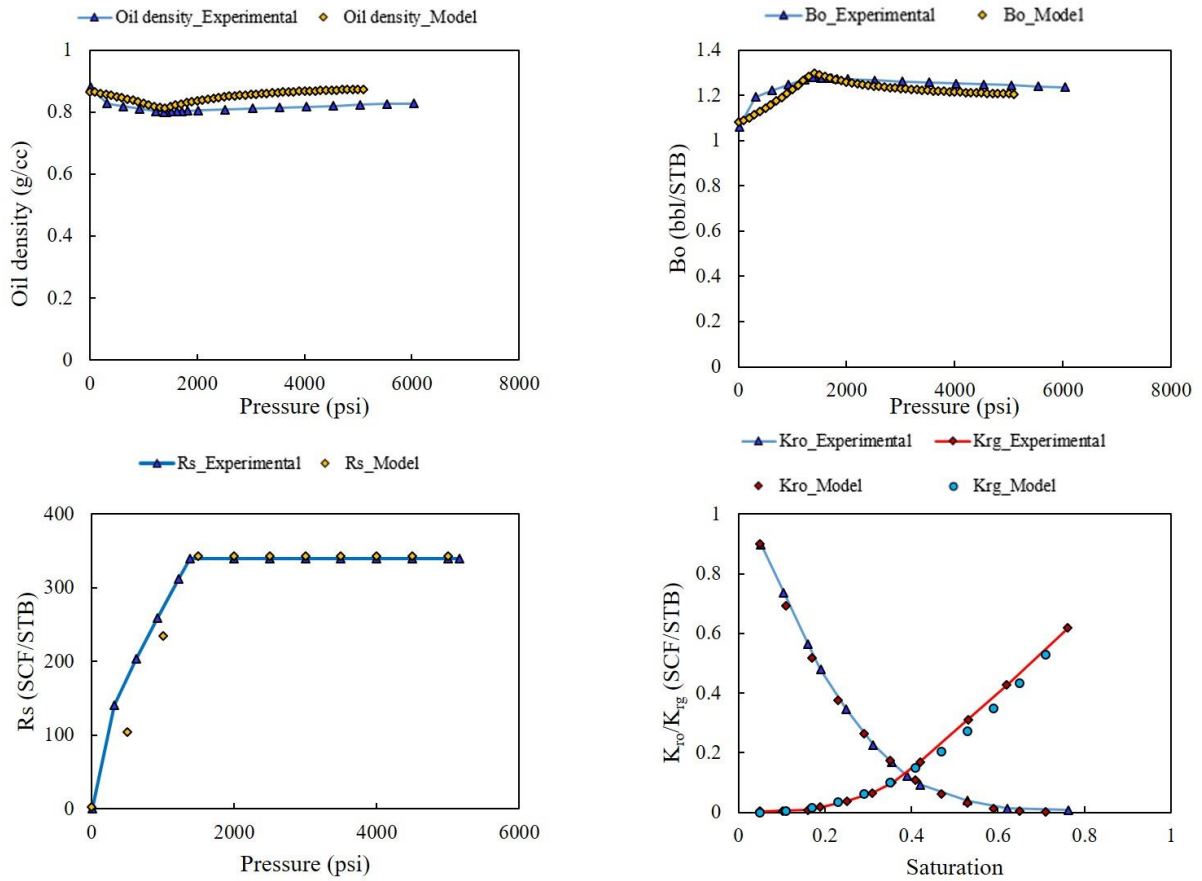
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Fig.1

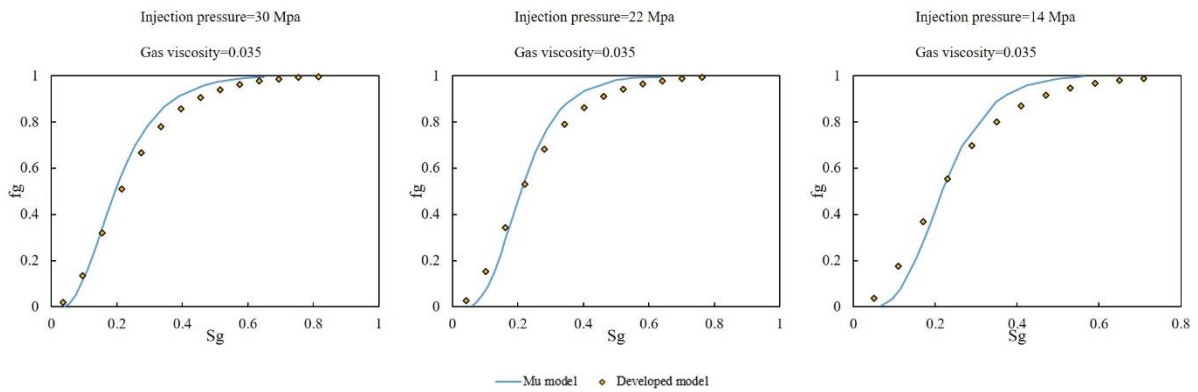


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Fig. 2



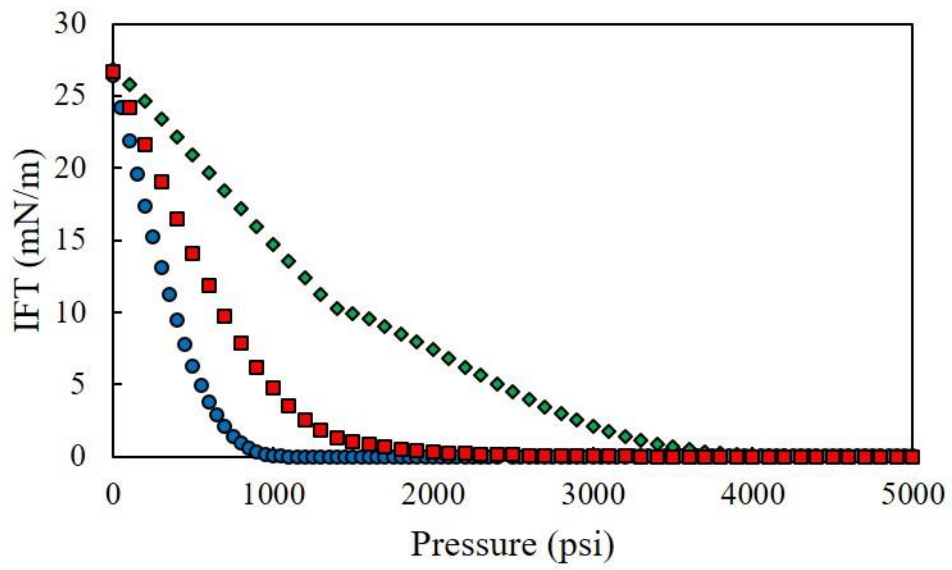
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Fig.3

● IFT (CO2) ◆ IFT (CH4) ■ IFT (N2)

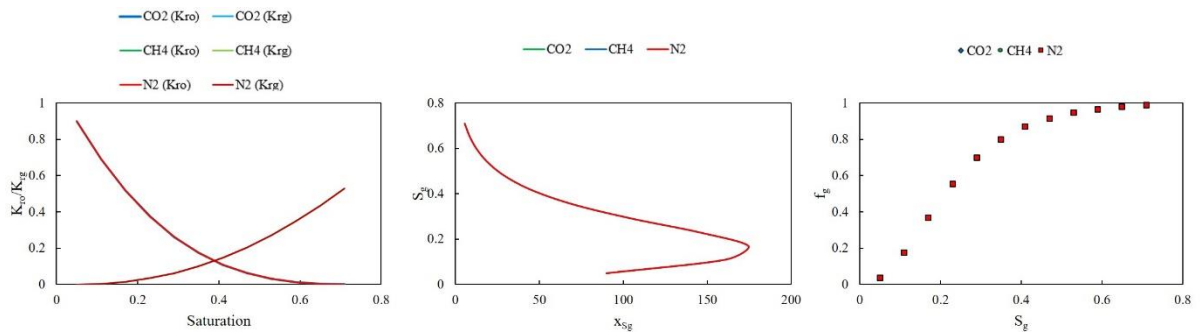


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Fig.4

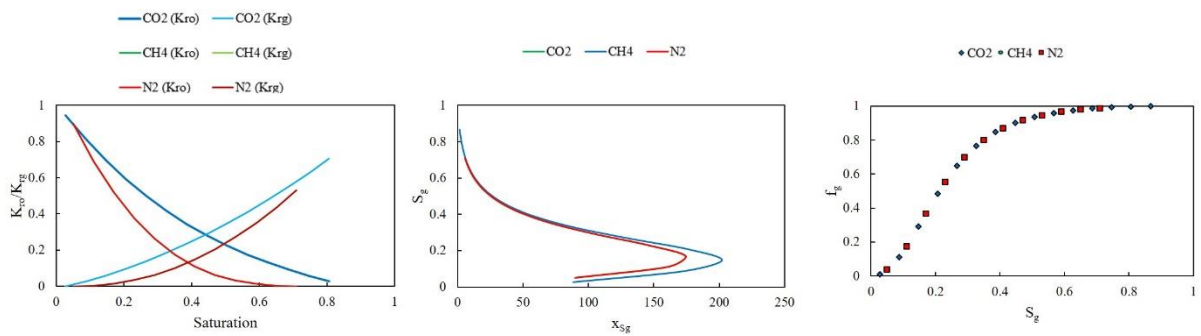


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Fig.5



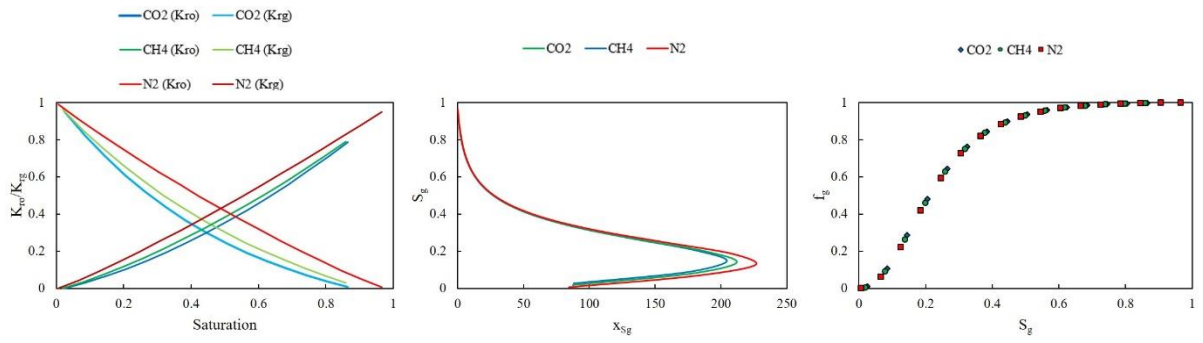
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Fig.6

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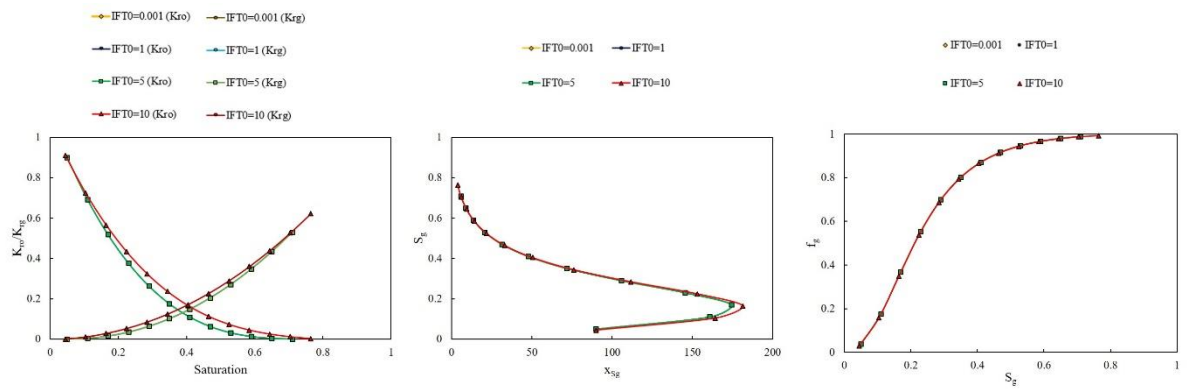


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Fig.7

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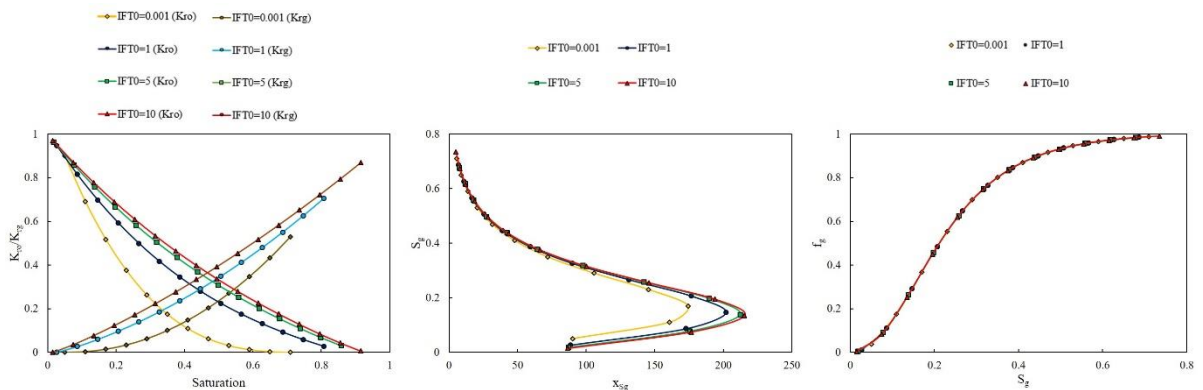


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Fig.8

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Fig.9

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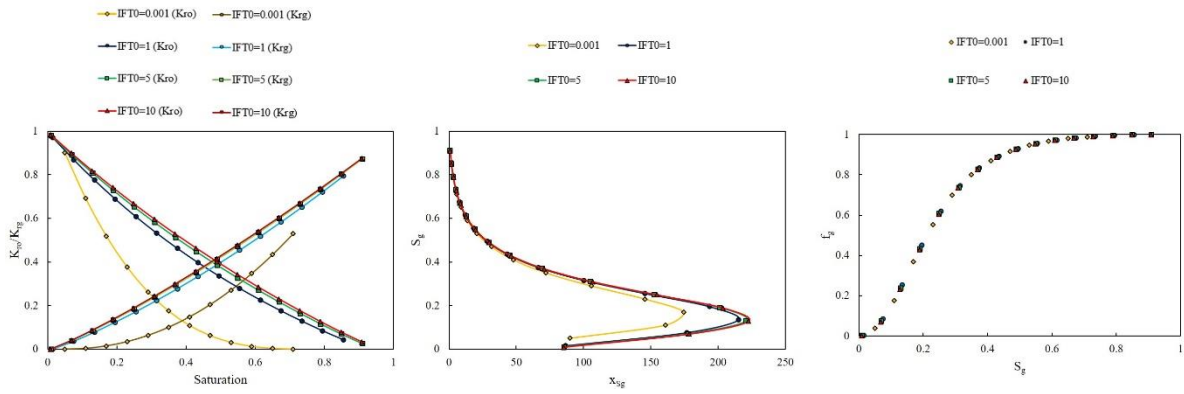


Fig.10

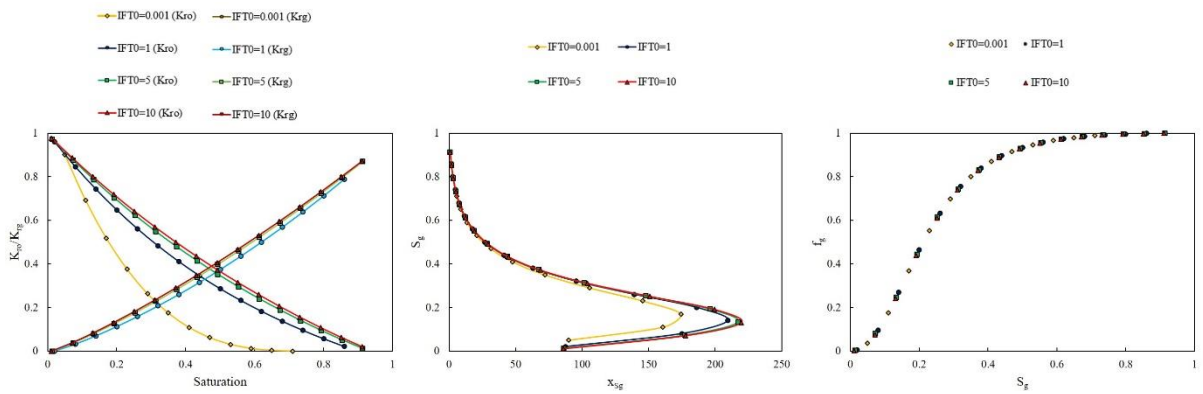


Fig.11

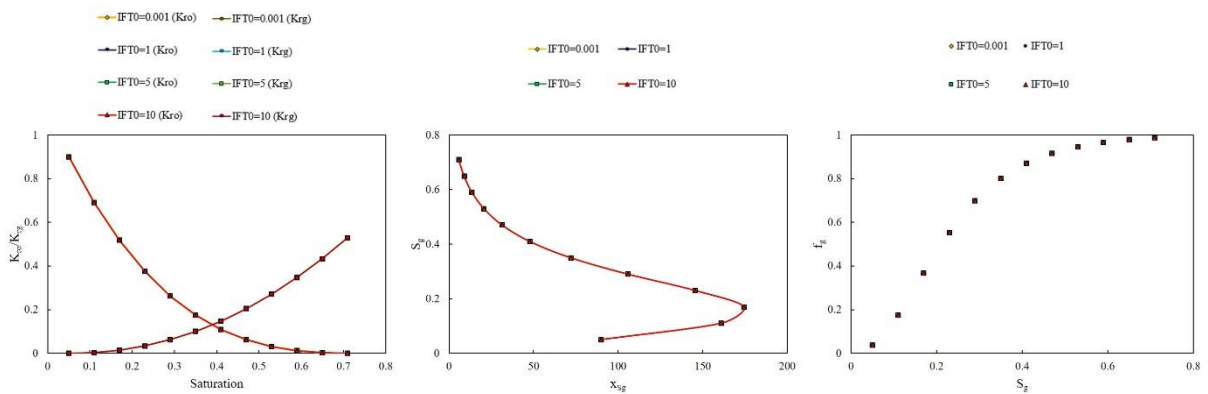


Fig.12

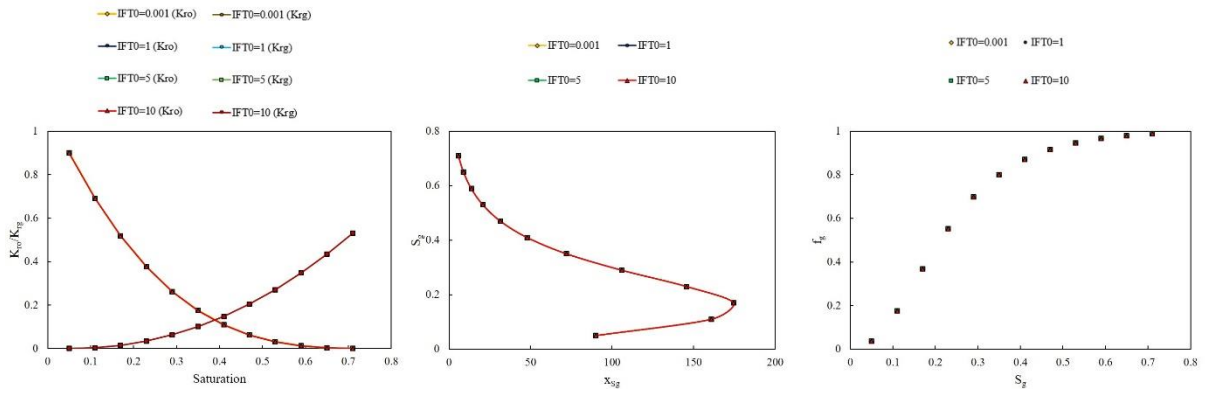


Fig. 13

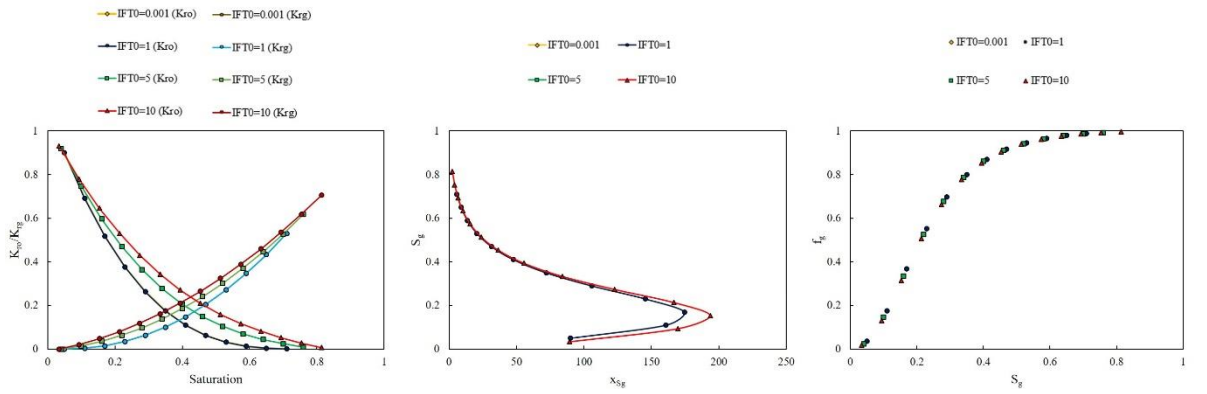


Fig. 14

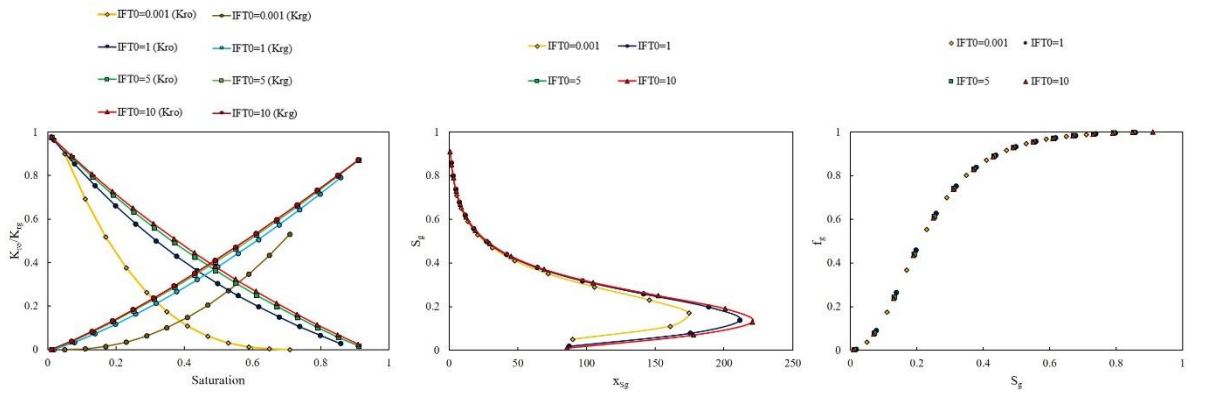


Fig. 15

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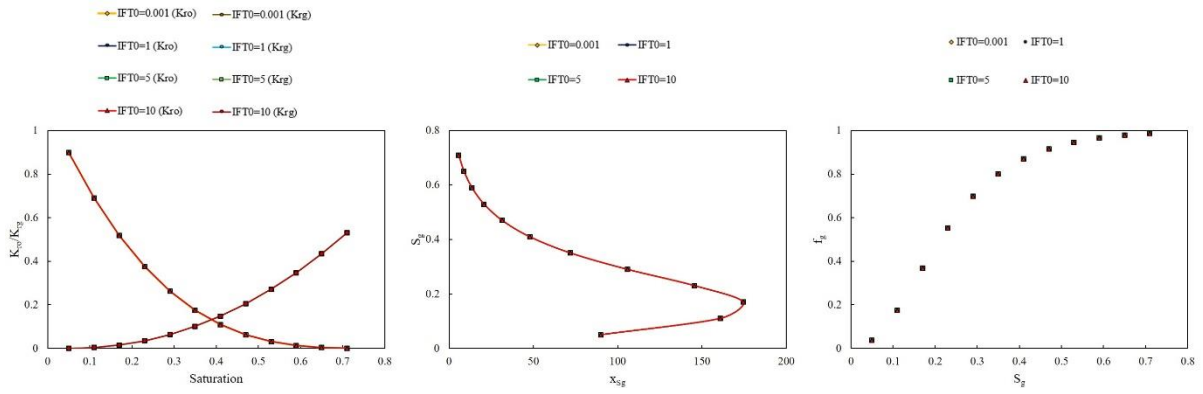


Fig. 16

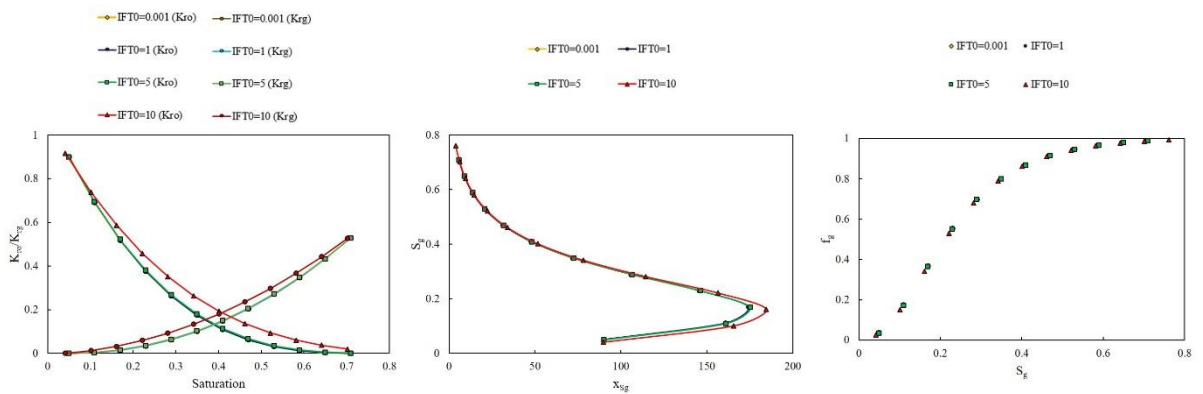


Fig. 17

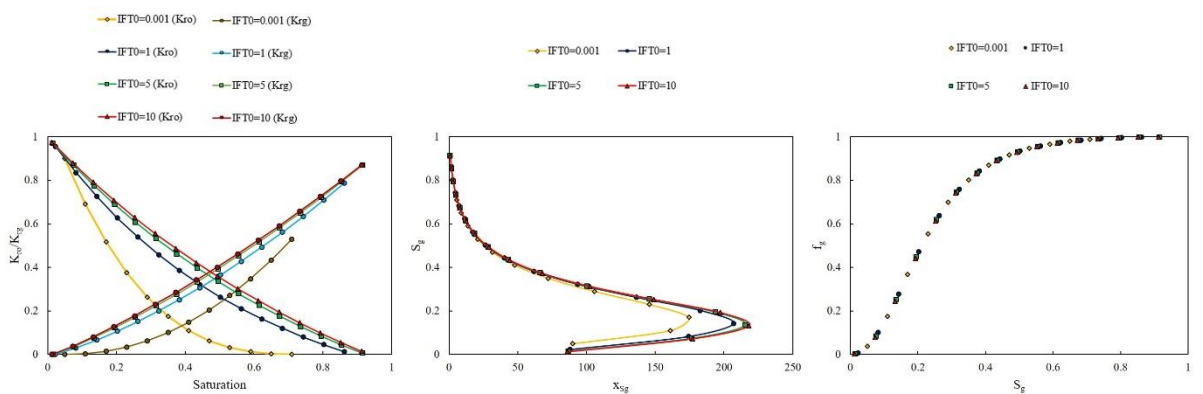


Fig. 18

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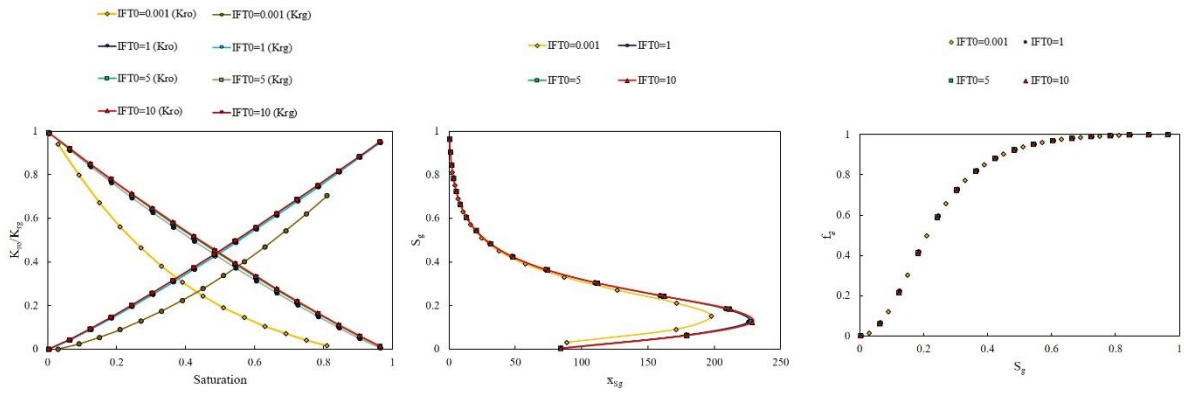
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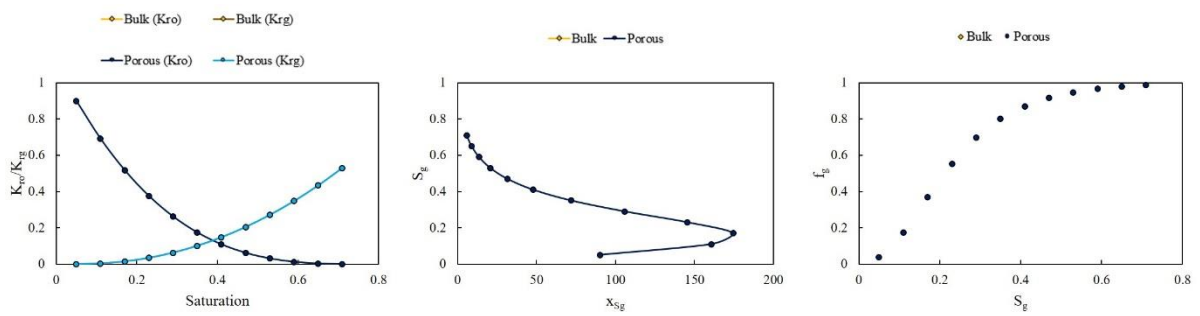


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Fig. 19

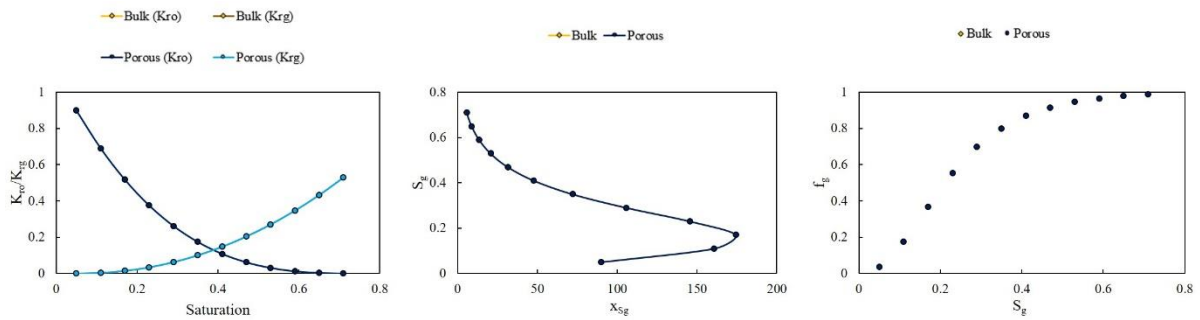


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Fig. 20



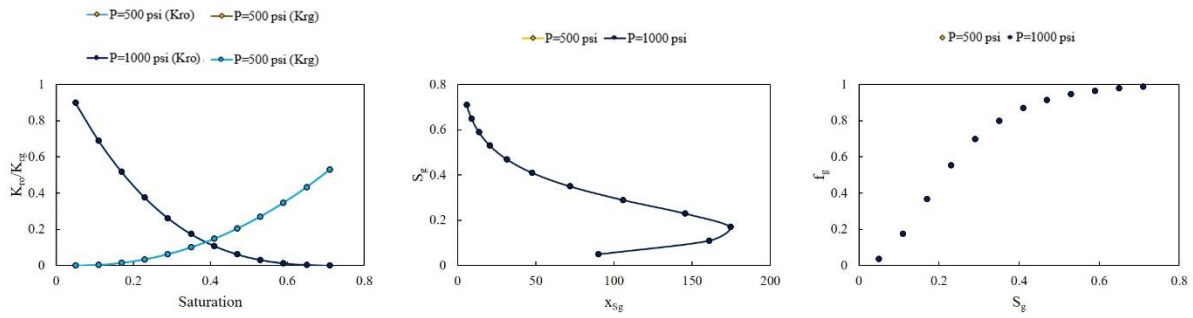
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Fig. 21



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Fig. 22

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