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### Cryptanalysis of full-round SFN block cipher a lightweight block cipher, targeting IoT systems

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KEYWORDS Lightweight block cipher; SFN; Related-key differential cryptanalysis; Meet in the middle attack. **Abstract.** SFN is a lightweight block cipher designed to be compact in hardware and efficient in software for constrained environments such as the Internet of Things (IoT) edge devices. Compared to the conventional block ciphers that are either Feistel network-based or Substitution-Permutation (SP), it has a different structure and uses both the SP network structure and Feistel network structure to encrypt. The SFN supports key lengths of 96 bits and its block length is 64 bits and includes 32 rounds. In this paper, we propose a deterministic related-key distinguisher for 31 rounds of the SFN. We are able to use the proposed related-key distinguisher to attack the SFN in the known-plaintext scenario with the time complexity of  $2^{60.58}$  encryptions. The data/memory complexity of those attacks are negligible. In addition, we will extend it to a practical chosen-plaintext-ciphertext key recovery attack on full SFN with the complexity of  $2^{20}$ . We also experimentally verified this attack. Also, in the single key mode, we present a meet-in-the-middle attack against the full rounds for which the time complexity is  $2^{80}$  the SFN calculations and the memory complexity is  $2^{20.32}$  bytes. The data complexity of this attack is only two known plaintexts and their corresponding ciphertext.

#### 1. Introduction

A Lightweight Cryptography (LWC) design could be a cryptographic algorithm or protocol befitting for implementation in constrained environments including Radio Frequency Identification (RFID) tags, contactless smart cards, sensors, and so on.

A lightweight block cipher could be proper for such environments. It is worthy to note that block ciphers play a significant role in the security of communications as cryptography algorithms. Hence, the security analysis of block ciphers is of particular importance. To this end, in this paper, we apply related key and meet in the middle (MITM) attacks to analyze the lightweight block cipher SFN [1].

The notion of related key attack functions is based on the idea that the attacker has a prior awareness that

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(or chooses) there exists a relation between a number of keys and thus she can access the encryption functions under such related keys. The earliest attacks of this kind were developed independently by Biham [2] and Knudsen [3], and the concept of a related key attack was delineated by Biham [2].

The meet in the middle attack is one of the types of known-plaintext attacks [4]. The attacker is able to know some plaintext and their ciphertexts. Using MITM attacks it may be possible to break ciphers, which have two or more secret keys for multiple encryptions using the same algorithm. For example, the 3DES cipher works in this way. The MITM attack is first proposed to attack DES [5]. There are numerous studies that pertain to MITM attacks on block ciphers, including [6–10].

SFN was proposed by Li et al. [1]. It is a 64-bit block cipher in which the round function uses both the Substitution-Permutation (SP) network structure and Feistel network structure to encrypt.

#### 1.1. Our contribution

In this paper, we present the first third party analysis of SFN block cipher, to the best of our knowledge, and our contributions are as follows:

- We introduce a deterministic related key differential distinguisher against 31 rounds of SFN;
- We also employ the proposed distinguisher to apply a full round related key differential attack on SFN to recover the main key (96 bits) in known-plaintext mode with time complexity 2<sup>60.58</sup> and negligible data and memory complexity;
- We employ the proposed distinguisher to apply a full round related key differential attack on SFN to recover the main key (96 bits) with time complexity  $2^{20}$ , data complexity  $2^{17.92}$  and negligible memory complexityin chosen-plaintext-ciphertext mode. We also experimentally verify this attack;
- In single key mode, we introduce a meet in the middle attack on SFN to recover all the 96 bits of the main key with time complexity 2<sup>80</sup> and memory complexity 2<sup>20.32</sup> and negligible data complexity.

#### 1.2. Outline.

This article is organized as follows. In Section 2 we present some notations and also a brief description of SFN block cipher. The description of the related key attack in the known-plaintext scenario is given in Section 3. We present the related key attack in the chosen-plaintext-ciphertext scenario in Section 4. Meet in the middle attack of the cipher is described in Section 5. Finally, the conclusion is presented in Section 6.

#### 2. Preliminaries

In this section, we give some notations and a brief description of SFN block cipher which will be used in the following parts.

#### 2.1. Notations

- ||: The concatenation of two binary strings.
- $X = (X_0 \cdots X_{15})$ : Represents a 64 bits string.  $X_0$  is the lowest value of its nibbles and  $X_{15}$  is the highest value one.
- $\Delta X$ : Represents a non-zero difference of X.
- $P^i$ : Represents the input of the (i + 1)th round encryption  $(i = 0, \dots, 31)$ .
- *RK*: Represents the front(low-value) 64 bits of the main keys.
- *CK*: Represents the back(high-value) 32 bits of the main keys for control signal keys.
- K = RK || CK: Represents the 96-bit main key.
- S<sup>i</sup> = (S<sup>i</sup><sub>0</sub> ··· S<sup>i</sup><sub>15</sub>): Represents the input of the *i*th round encryption of SFN (*i* = 1, ··· , 32). S<sup>i</sup><sub>0</sub> is the lowest value nibble of S<sup>i</sup>. It is also possible that S<sup>i</sup> is represented by a 4 × 4 matrix:

$$S^{i} = \begin{bmatrix} S_{0}^{i} & S_{1}^{i} & S_{2}^{i} & S_{3}^{i} \\ S_{4}^{i} & S_{5}^{i} & S_{6}^{i} & S_{7}^{i} \\ S_{8}^{i} & S_{9}^{i} & S_{10}^{i} & S_{11}^{i} \\ S_{12}^{i} & S_{13}^{i} & S_{14}^{i} & S_{15}^{i} \end{bmatrix}$$

- $RK^i = (RK_0^i \cdots RK_{15}^i)$ : Represents the (i + 1)th round keys  $(i = 0, \cdots, 31)$ ,  $RK_0^i$  is the lowest value nibble of  $RK^i$  and  $RK^{i\sim j}$  represents the *i*th to *j*th round keys.
- $\Delta RK^i$ : Represents the difference of the (i + 1)th round keys  $(i = 0, \dots, 31)$ .
- CK<sub>i</sub>: Represents the *i*th bit (*i* = 0, · · · , 31) of CK and CK<sub>i∼j</sub> represents the *i*th to *j*th bit of CK.
- $\Delta CK$ : Represents the difference of the control signal keys and  $\Delta CK_i$  represents the difference of the *i*th bit  $(i = 0, \dots, 31)$  of CK.
- $RK_F^{in}$ ,  $RK_F^{out}$ : Represent the input and the output states of the Feistel Key Expansion structure of the 32nd round, respectively.
- $RK_S^{in}$ ,  $RK_S^{out}$ : Represent the input and the output states of the SP Key Expansion structure of the 32nd round, respectively.
- $P_F$ ,  $P_S$ : Represent the input states of the Feistel structure and SP structure of encryption in 32nd round, respectively.
- 0<sup>n</sup>: Represents a sequence of n bits as 0, where n is a natural.
- Enc(P, I): The encryption of P, I is a 32-bit string and RK || I is as the main key.



Figure 1. Encryption procedure of SFN cipher [1].

- Dec(C, I): The decryption of C, I is a 32-bit string and RK || I is as the main key.
- $Enc(S^{(r+1)}, RK^{r\sim31}), CK_{r\sim31}, r), (r = 0, \dots, 31)$ : The partial encryption of  $S^{(r+1)}$ , the encryption would start from round (r + 1)th with round key  $RK^r$  and round control signal bit  $CK_r$ .
- $Dec(C, RK^{(r\sim31)}, CK_{(r\sim31)}, r), (r = 0, \cdots, 31)$ : The partial decryption of C, the decryption would end after getting  $S^{r+1}$ .
- $GF_2^4$ : The finite field with 16 elements. In this field sum is XOR.
- $\alpha(t)$ : Represents the 32-bit string  $0 \cdots 010 \cdots 0$ , the only 1 is in the position of t, where  $t = 0, \cdots, 31$ , e.g.,  $\alpha(31) = 0^{31}1$ ,  $\alpha(5) = 0^5 10^{26}$ .

#### 2.2. Brief description of SFN

SFN, as a unique structure, consists of an SP network and a Feistel network [1]. Its block and the key lengths are 64 bits and 96 bits, respectively. The 96-bit main key is divided into the 64-bit round key as  $RK^0 \in$  $\{0,1\}^{64}$  and 32-bit control signal key as  $CK \in \{0,1\}^{32}$ . The  $RK^0$  conducts AddRoundKey and KeyExpansion, and the  $CK = CK_0 \parallel CK_1 \parallel \cdots \parallel CK_{30} \parallel CK_{31}$ is considered to be the control signal, and each bit of the control signal carries out one and only one round operation. In the case of a detailed signal key, when the bit of the control signal is 0, SFN chooses SP network structure to perform encryption or decryption, while the Feistel network structure conducts *KeyExpansion*. However, if the bit of the signal is 1, SFN selects Feistel network structure to carry out encryption or decryption and the SP network structure pursues *KeyExpansion* [1] (see Figure 1).

The details of the SFN round function is given in Figure 1. The 4-bit S-boxes  $S_1$ , and  $S_2$  of SFN are defined as:

$$S_1 = \{C, A, D, 3, E, B, F, 7, 8, 9, 1, 5, 0, 2, 4, 6\}$$

and

$$S_2 = \{B, F, 3, 2, A, C, 9, 1, 6, 7, 8, 0, E, 5, D, 4\},\$$

respectively. Both of the *MixRows* and *MixColumns* layer apply a matrix  $M_{4\times 4}$  which its 16 elements are in  $GF_2^4$  (its characteristic polynomial is  $x^4 + x + 1 = 0$ ):

$$M = \begin{bmatrix} 1 & 2 & 6 & 4 \\ 2 & 1 & 4 & 6 \\ 6 & 4 & 1 & 2 \\ 4 & 6 & 2 & 1 \end{bmatrix}.$$

In SFN the input of every rounds is represented as a  $4 \times 4$  matrix say  $S^i, i \in \{0, 1, \dots, 31\}$ , so the *MixColumns* and *MixRows layer* of *i*th round can be represented by  $MS^i$  and  $S^iM$  respectively. For more details of SFN structure we refer the readers to [1].



**Figure 2.** A distinguisher on full SFN, where  $\overline{0}$  means  $0^{64}$ .

#### 3. Related key with known-plaintext attack

In this section, we will discuss the security of the SFN against the related key differential cryptanalysis in the known-plaintext scenario.

#### 3.1. First key recovery attack

Consider the two secret related key inputs to be  $K^0 = (RK^0 \parallel CK)$  and  $\overline{K^0} = (RK^0 \parallel \overline{CK})$ , where  $\Delta CK = CK \oplus \overline{CK} = \alpha(31)$  and hence  $\Delta K^0 =$  $K^0 \oplus \overline{K^0} = 0^{64} \parallel lpha(31) = 0^{95} \parallel 1.$ Hence given C and  $\overline{C}$ , respectively produced by  $(P^0, K^0)$ and  $(P^0, \overline{K^0})$ , the output differentials after 31-round encryption are  $\Delta P^{31} = 0^{64}$  and  $\Delta K^{31} = (\Delta R K^{31} \parallel \Delta C K_0 \cdots \Delta C K_{31}) = (0^{64} \parallel \alpha(31) = 0^{95} \parallel 1)$  with a probability of 1, which is a distinguisher for 31st rounds of the SFN. Since  $\Delta CK_{31} = 1$ , refer to Figure 2, the adversary would not be able to determine the difference of ciphertexts (differential output). However, she gets a distinguisher for 31st rounds of the SFN, and she is able to do key recovery on the 32nd round of the cipher. The procedure of the key recovery of this round is given in Algorithm 1.

To determine the attack complexity, is dominated by  $2^{64}$  guesses for  $RK_F^{32}$ , the last round key, and related partial decryption which costs 3 rounds of SFN. We should also exhaustively search the 32 bits of CK that are not involved in the first attack to find the correct key. Therefore, the total time complexity of the first attack is  $(2^{64} \times 3)\frac{1}{32} + 2^{32} \simeq 2^{60.58}$  32-round SFN encryptions.

•
$$RK^{31} \leftarrow algorithm \ 1$$
  
for each choice of  $RK_F^{out}$  (2<sup>64</sup> choices) do  
1) Decrypt one round Feistel Key Expansion to  
calculate the value of  $RK_F^{in}$ . Next, drive  
 $RK_S^{in}$ , encrypt one round SP KeyExpansion  
and calculate  $RK_S^{out}$ ;  
2) One round decryption of  $(C, RK_F^{out})$  and  
 $(\overline{C}, RK_S^{out})$  are assigned to  $P_S$  and  $P_F$ ;  
3) if  $P_S \oplus P_F = 0^{64}$  then  
 $| RK^{31} \leftarrow RK_F^{out}$   
else  
(a).One round decryption of  $(\overline{C}, RK_F^{out})$  and  
 $(C, RK_S^{out})$  are assigned to  $P_S$  and  $P_F$ ;  
(b). if  $P_S \oplus P_F = 0^{64}$  then  
 $| RK^{31} \leftarrow RK_F^{out}$ 

Algorithm 1. The first key recovery attack on the SFN.

#### 4. Related-key with chosen-plaintext -ciphertext attack

In this section we present a new attack to recover the main key in chosen-plaintext-ciphertext scenario with time complexity  $2^{20}$  and data complexity  $2^{17.92}$ . Let us assume the adversary can choose an arbitrary ciphertext C and request from an oracle, say O-RK, the corresponding plaintext with the key RK||CK or  $RK||\overline{CK}$ , where  $CK \oplus \overline{CK}$  is a fixed 32 bits difference which its hamming weight is one. We denote the answers of O-RK with the key RK || CK by Dec(C, CK)and with the key  $RK || \overline{CK}$  by  $Dec(C, \overline{CK})$ . Also, she or he can choose an arbitrary plaintext P and request from the oracle O-RK the corresponding ciphertext with the key RK || CK or  $RK || \overline{CK}$  that we denote them by Enc(P, CK) and  $Enc(P, \overline{CK})$ , respectively. In the attack, we will find the bit of  $CK_{31}$  first and then we recover the 64 bits of  $RK^{31}$  and after that, we look for  $CK_{30}$  and  $RK^{30}$ , then we find  $CK_{29}$  and  $RK^{29}$ and so on. Finally we get  $CK_0$  and  $RK^0$ . Remember  $K = RK \parallel CK = RK^0 \parallel CK_0 \parallel \cdots \parallel CK_{31}$ , so the key K has been recovered.

Suppose P is an arbitrary plaintext and the adversary is given Enc(P, CK) and  $Enc(P, \overline{CK})$ where  $CK \oplus \overline{CK} = 0x0000001$ . Enc(P, CK) and  $Enc(P, \overline{CK})$  and then based on the with relation between them we would try to recover the  $RK^{31}$ . Unfortunately, it worked very slowly and because of that we decided to apply a new approach. In our method, we denote Enc(P, CK) by  $C_0$  and  $C_1$ , when the bit of  $CK_{31}$  is 0 or 1, respectively. It is obvious that there are so many relations between  $C_0$  and  $C_1$ , and for using of them, we look at  $C_0$  as a new plaintext,  $RK^{31}$  as a new main key,  $C_1$  as a new corresponding ciphertext and at whole of them as a new scheme which we call it  $\Gamma_{32}$  (Figure 3). We found a multioutputs differential characteristic for this new scheme (see Figure 4). By using this differential characteristic and some other similar characteristics, we found  $CK_{31}$ first,  $RK_{31}$ , other control signal bits, and round keys then. For more details refer to Subsection 4.2.



Figure 3. The new scheme  $\Gamma_{32}$  from  $C_0$  to  $C_1$  for the SFN cipher, where the  $C_0$  and  $C_1$  are the ciphertext when  $CK_{31}$  is 0 or 1, respectively. At  $\Gamma_{32}$  two 64 bits subkeys  $K_0$  and  $K_1$  are made from the round key  $RK^{31}$  with Feistel and SP network, respectively.



**Figure 4.** A multi-output characteristic (because the stars can vary) for the new scheme  $\Gamma_{32}$  from  $C_0$  to  $C_1$ . The values of differences of input nibbles 0, 4 and 12 can vary simultaneously. In fact the *nibble0*, *nibble4* and *nibble12* of input differences must choose from a proper set. It is while its 8 low-value output nibbles differences do not vary and stay zero. Also, the positions of 16 input nibbles can rotate to the right (from LSB to MSB) by 1, 2 or 3 nibbles, e.g., there exist a similar characteristics with input difference 0x0060000000B00020 and the same previous output.

$\begin{bmatrix} * & * & * & * \\ * & * & * & * \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} =$	$M \cdot \begin{bmatrix} 0 & 0 & 0 & 0 \\ x & 0 & 0 & 0 \\ y & 0 & 0 & 0 \\ z & 0 & 0 & 0 \end{bmatrix} \cdot M = M \cdot \begin{bmatrix} 0 & 0 & 0 & 0 \\ x & 2x & 6x & 4x \\ y & 2y & 6y & 4y \\ z & 2z & 6z & 4z \end{bmatrix}$	
$= \begin{bmatrix} 2x + 6y + 4z \\ x + 4y + 6z \\ 4x + y + 2z \\ 6x + 2y + z \end{bmatrix}$	$ \begin{array}{cccc} 2(2x+6y+4z) & 6(2x+6y+4z) & 4(2x+6y+4z) \\ 2(x+4y+6z) & 6(x+4y+6z) & 4(x+4y+6z) \\ 2(4x+y+2z) & 6(4x+y+2z) & 4(4x+y+2z) \\ 2(6x+2y+z) & 6(6x+2y+z) & 4(6x+2y+z) \end{array} $	

Boy	Τ
DUA	т.

Table 1. The fifteen solution for x, y and z. Every column is a solution. The blue column is the values for the characteristic of Figure 4.

х	1	2	3	4	5	6	7	8	9	A	В	C	D	E	F
у	7	E	9	F	8	1	6	D	A	3	4	2	5	C	B
z	8	3	В	6	E	5	D	C	4	F	7	A	2	9	1

#### 4.1. The structure of $\Gamma_{32}$

As we explained before, we denoted the new scheme by  $\Gamma_{32}$  that  $C_0$  is its plaintext,  $RK^{31}$  is its main key and  $C_1$  is its ciphertext. Two 64 bits subkeys  $K_0$  and  $K_1$ are made from its main key  $RK^{31}$  (Figure 3).  $K_0$  and  $K_1$  are made with Feistel and SP network structure, respectively. They are the first and last round key at  $\Gamma_{32}$ . The new scheme uses  $RK^{31}$  for second round key after  $K_0$ , and half of it (i.e., the 32 lowest value bits) before  $K_1$  as third round key. We found a differential trail with the probability  $2^{-22}$  for  $\Gamma_{32}$ . There was an interesting situation at this trail: The 8 lowest nibbles of the output of the trail were zero. It led us to choose a multi-output differential characteristic instead of a single-output for our purpose: We allowed the 8 highest nibbles of the output to be every differences. The value of the probability of this multi-output difference characteristic was  $2^{-6}$  which was very greater than  $2^{-22}$  (Figure 4). On the other hand, because of being zero the values of the 8 lowest nibble of the output differences of the characteristic, we decided to consider the structure of MixColumns and MixRows layer to find an algebraic reason for it. After considering these two linear parts of  $\Gamma_{32}$ , we found an interesting fact: There existed a lot of similar multi-output characteristics for  $\Gamma_{32}$ , which the probabilities of them were at most  $2^{-6}$  and at least  $2^{-9}$ . We explain these differential characteristics in more detail in the following.

#### 4.1.1. The differential characteristics for the $\Gamma_{32}$

As we explained before, we found a multi-output trail of  $\Gamma_{32}$  which its probability was  $2^{-6}$  (see Figure 4). As you can see in it, the differences before *MixRows* and after *MixColumns* are  $S^2 = (000030009000B000)$  and  $S^4 = (FD49EF2D00000000)$ , respectively. We define a  $4 \times 4$  matrix *M* and denote the *i*th differential state with a  $4 \times 4$  matrix  $S^i$ , so in the trail of Figure 4:

$S^2$	=	$\begin{bmatrix} 0\\ 3\\ 9\\ B\end{bmatrix}$	0 0 0 0	0 0 0 0	$\begin{bmatrix} 0\\0\\0\\0\end{bmatrix},$	$S^4 =$	$\begin{bmatrix} F \\ E \\ 0 \\ 0 \end{bmatrix}$	$egin{array}{c} D \ F \ 0 \ 0 \end{array}$	4 2 0 0	$\begin{bmatrix} 9\\D\\0\\0\end{bmatrix}$	,
M	=	$\begin{bmatrix} 1\\ 2\\ 6\\ 4 \end{bmatrix}$	$2 \\ 1 \\ 4 \\ 6$	$     \begin{array}{c}       6 \\       4 \\       1 \\       2     \end{array} $	$\begin{bmatrix} 4\\6\\2\\1 \end{bmatrix}$						

It is easily seen the 8 high-value nibbles of  $S^4$  are zero. The *MixRows* and *MixColumns* layer at *i*th round are a multiplication of the above matrix M to the state matrix, from the right and left side respectively, so:

$$S^3 = S^2 M \Rightarrow S^4 = M S^3 \Rightarrow S^4 = M S^2 M.$$

After this observation we suppose instead of 3, 9, B in the first column of  $S^2$  we put x, y, z and find them such that all of the elements of the third and fourth row of  $S^4$  to be zero, are shown in Box I, where the sign "\*" can be every difference. These equations are equivalent with two below equations in  $GF_2^4$ :

$$4x + y + 2z = 0, \ 6x + 2y + z = 0 \Leftrightarrow$$

$$y = 7x, \ z = 8x, \ x \in GF_2^4.$$
 (2)

So there exist 15 nonzero solution for triple (x, y, z)when x varies from 1 to F. As it is seen the three nonzero input differences x, y and z at  $S^2$  in the characteristic of Figure 4 are in the fourth column of the Table 1. In fact, there are a lot of other similar characteristics that their differences  $S^2$  in them are like (0000x000y000z000) and the nonzero differences x, y and z can be chosen from every column of the Table 1. On the other hand in a characteristic of this kind, if  $S^0 = (i000j000000k000)$  then the differential nibbles i, j and k are corresponded to y, z and x (Figure 5), i.e., they must be such that they can become y, z and x after passing the  $S_1$ -box, by positive probabilities. So if in a characteristic of this kind  $S^2$  is fixed then  $S^0$  can varies.

If  $S^2 = (000030009000B000)$  and  $S^0 = (i000j0000000k000)$ , then by considering the DDT of  $S_1$ -box, the differential nibbles i, j and k can vary while  $i \in \{2, 3, 5, 8, 9, B, C\}, j \in \{4, 7, 8, 9, B, D, F\}$  and  $k \in \{4, 6, 7, 8, 9, D, F\}$ . The reason is: e.g. i must be a difference that has a positive probability for going to 9 after passing  $S_1$ -box. So by using ninth column of the DDT of  $S_1$ -box (Table 2) i has to be in the set  $\{2, 3, 5, 8, 9, B, C\}$ .

The almost same situation exists for j or k. With a similar way if in a characteristic of this kind the values of i, j or k at  $S^0$  are fixed then the values of x, y and zat  $S^2$  can vary. Suppose  $S^0 = (300070000004000)$  and  $S^2 = (0000x000y000z000)$  then the nonzero difference x, y or z must be one of differences which the differences 4,3 or 7 can go to them after passing the  $S_1$ -box with positive probability respectively. So from the DDT of  $S_1$ -box  $x \in \{1, 2, 3, 4, 5, 8, B\}, y \in \{4, 6, 7, 8, 9, D, F\}$ and  $z \in \{3, 5, 6, B, D, E\}$ . But by considering these three sets and the Table 1, we conclude there exist



Figure 5. The first three state of a similar multi-outputs differential characteristic to the trail of Figure 4 for  $\Gamma_{32}$ .

only three cases for x, y and z, i.e.,  $(x, y, z) \in \{(3, 9, B), (4, F, 6), (5, 8, E)\}$ . The other values for x, y and z can not occur, e.g., x does not be 1: if x = 1 then by Table 1, the differences y and z must be 7 and 8 respectively (the value of the second and third row of the first column of Table 1), but in the set of values for z, there is not the value 8, so it is not possible that x = 1.

It may be possible that there exists only one solution for  $S^2$  when the  $S^0$  is fixed, e.g., if  $S^0 =$ (2000B0000006000) then there is only one case for x, y and z, i.e. (x, y, z) = (3, 9, B), therefore  $S^2$  must be (000030009000B000). In this case the probability of the characteristic is equal to the multiplication of three probabilities  $\Pr_{S_1}(2 \to 9) \times \Pr_{S_1}(B \to B) \times \Pr_{S_1}(6 \to 3) = \frac{4}{16} \times \frac{4}{16} \times \frac{4}{16} = 2^{-6}$ . By these method we collected some characteristics of this kind and their probabilities, they can be seen in Table 3. On the other hand, if in Equality (1) we change all the elements of the column 1 and elements of columns 2, 3 or 4 of the middle matrix with each other, then two Eqs. (2) stay the same without any changes. We explain the reasons for the case of column 2, the two other columns are the same. For column 2 Relations (1) is changed as it can be seen in Eq. (3) in Box II, these equality show the two previous Eq. (2) are still valid. With these properties it is straightforward that one can conclude in a multi-outputs trail of this kind, it is possible to rotate the input difference nibbles of  $S^0$  by 1, 2 or 3 nibbles from the low-value nibbles to the high-value ones (see Table 4). At this table, the numbers in the fourth column show the number of nibbles for the rotation at the input of characteristics. It should be noted we considered the most left bit as the LSB.

Remark 1: We built a Mixed Integer Linear Programming (MILP) [11,12], model for  $\Gamma_{32}$  and by using it, we looked for a characteristic from  $C_1$  to  $C_0$  such that its input differential to be  $S^0 = (2000B00000006000)$  and at its output differential the 8 low-value nibbles to be zero. After that we found that there is not any such characteristic from  $C_1$  to  $C_0$  whit positive probability.

$$\begin{bmatrix} * & * & * & * \\ * & * & * & * \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} M \cdot \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & x & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & z & 0 & 0 \end{bmatrix} \cdot M = M \cdot \begin{bmatrix} 0 & 0 & 0 & 0 \\ 2x & x & 4x & 6x \\ 2y & y & 4y & 6y \\ 2z & z & 4z & 6z \end{bmatrix}$$

$$= \begin{bmatrix} 2(2x + 6y + 4z) & 2x + 6y + 4z & 4(2x + 6y + 4z) & 6(2x + 6y + 4z) \\ 2(x + 4y + 6z) & x + 4y + 6z & 4(x + 4y + 6z) & 6(x + 4y + 6z) \\ 2(4x + y + 2z) & 4x + y + 2z & 4(4x + y + 2z) & 6(4x + y + 2z) \\ 2(6x + 2y + z) & 6x + 2y + z & 4(6x + 2y + z) & 6(6x + 2y + z) \end{bmatrix}$$
(3)

										(			1			
x/y	0	1	2	3	4	5	6	7	8	9	A	В	C	D	E	F
0	16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	2	4	0	2	2	2	0	2	0	0	0	0	0	2	0
2	0	4	0	0	4	0	0	0	0	4	0	0	4	0	0	0
3	0	0	0	0	2	0	4	2	2	2	0	0	0	2	0	2
4	0	2	4	2	2	2	0	0	2	0	0	2	0	0	0	0
5	0	2	0	0	2	0	0	4	0	2	4	0	2	0	0	0
6	0	2	0	4	0	0	0	2	2	0	0	0	2	2	0	2
7	0	0	0	2	0	4	2	0	0	0	0	2	0	4	2	0
8	0	2	0	2	2	0	2	0	0	2	0	2	2	0	2	0
9	0	0	4	2	0	2	0	0	2	2	0	2	2	0	0	0
A	0	0	0	0	0	4	0	0	0	0	4	0	0	4	0	4
B	0	0	0	0	2	0	0	2	2	2	0	4	0	2	0	2
C	0	0	4	0	0	2	2	0	2	2	0	0	2	0	2	0
D	0	0	0	2	0	0	2	4	0	0	4	2	0	0	2	0
E	0	2	0	0	0	0	0	2	2	0	0	0	2	2	4	2
F	0	0	0	2	0	0	2	0	0	0	4	2	0	0	2	4

**Table 2.** Differential Distribution Table (DDT) of the  $S_1$ -box

Table 3. Some multi-output characteristics for  $\Gamma_{32}$ , where PS and PT respectively denote the probability of a single trail and the sum of the probabilities of all trails as a total probability.

No.	$S^0$	$S^2$	$\#S^2$	PS	PT
1	(2000B0000006000)	(000030009000B000)	1	$2^{-6}$	$2^{-6}$
2	(300040000007000)	(000030009000B000)	1	$2^{-9}$	$2^{-9}$
3	(300040000004000)	$egin{array}{llllllllllllllllllllllllllllllllllll$	2	$2^{-9}$ $2^{-9}$	$2^{-8}$
4	(2000B0000004000)	$egin{array}{l} (000030009000B000)\ (000040007000B000) \end{array}$	2	$2^{-9}$ $2^{-9}$	$2^{-8}$
5	(3000700000004000)	$egin{array}{l} (000030009000B000)\ (00004000F0006000)\ (000050008000E000) \end{array}$	3	$2^{-9}$ $2^{-9}$ $2^{-9}$	$2^{-7.41}$

By using this property we find the control signal bits of CK, for more details refer to Subsection 4.2.

#### 4.2. Second key recovery procedure

In this section, we show that by decryption different ciphertext and encrypting the results again under related keys, the 96 bits of the main secret key can be extracted with the time complexity of  $2^{20}$  and data complexity  $2^{17.92}$ . In the attack the adversary has access to an oracle, say O-RL, and for an arbitrary plaintext P or for an arbitrary ciphertext C she or he can receive from the oracle:

- 1. The ciphertext Enc(P, Ck).
- 2. The ciphertext  $Enc(P, \overline{Ck})$ , while the hamming weight of  $Ck \oplus \overline{Ck}$  is 1.
- 3. The plaintext Dec(C, Ck).
- 4. The plaintext  $Dec(C, \overline{Ck})$ , while the hamming weight of  $Ck \oplus Ck$  is 1.

To the best of our knowledge this kind of attack, in related key mode, which applies chosen-plaintext

- The 96 bits of main key  $\leftarrow$  Algorithm 2
- 1)  $CK_{31} \leftarrow Algorithm 3$
- 2)for  $j \in \{0, 1, 2, 3\}$  do
  - $((K_0)_j, (K_0)_{4+j}, (K_0)_{12+j}) \leftarrow$
- algorithm  $4(j, CK_{31})$
- $\begin{array}{l} 1 & (K_0)_{8,1}(K_0)_{9,1}(K_0)_{10}, (K_0)_{11}) \leftarrow Algorithm \ 5 \\ ((K_0)_l, \ l \in (GF_2^4 \{8, 9, 10, 11\}) \\ 4) \ RK^{31} \leftarrow K_0 \quad \triangleright \ \text{By using the } K_0 \ \text{and with the} \end{array}$
- Feistel structure in backward direction at  $\Gamma_{32}$  get the  $RK^3$ . 5) for  $l \in \{30, \cdots, 0\}$  do
- a)  $CK_l \leftarrow Algorithm6 \ (l, CK_i, RK^i(l+1 \le i \le 31));$ b)  $RK^l \leftarrow RK^{l+1};$  $\triangleright$  By using the  $RK^{l+1}$ and with the Feistel structure or the SP structure in backward direction get the  $RK^{l}$
- when  $CK_l = 0$  or 1. 6) Return  $RK^0 \parallel CK_0 \parallel \cdots \parallel CK_{31}$  as the secret key of the SFN cipher.

Algorithm 2. Recovering the main key of the SFN.

and ciphertext simultaneously is introduced for the first time, so we call it "chosen-plaintext-ciphertext" related key attack. Algorithm 2 is for recovering the main key of the SFN and it has some steps as follows:

**Table 4.** It is possible to rotate the input differences  $S^0$  at the multi-output characteristics for  $\Gamma_{32}$  by 1, 2 or 3 nibbles from the low-value nibbles to the high-value ones. At first column, numbers 10 to 13, ..., 50 to 53 show the characteristic number 1, ..., 5 of Table 3 and their rotations with 1, 2 or 3 nibbles at their inputs respectively.

No.	$S^{0}$	$S^2$	# nibbles	PS	PT
10	(2000B0000006000)	(000030009000B000)	0	$2^{-6}$	$2^{-6}$
11	(02000B000000600)	(0000030009000B00)	1	$2^{-6}$	$2^{-6}$
12	(002000B00000060)	(00000030009000B0)	2	$2^{-6}$	$2^{-6}$
13	(0002000B0000006)	(000000030009000B)	3	$2^{-6}$	$2^{-6}$
20	(300040000007000)	(000030009000B000)	0	$2^{-9}$	$2^{-9}$
21	(030004000000700)	(0000030009000B00)	1	$2^{-9}$	$2^{-9}$
22	(003000400000070)	(00000030009000B0)	2	$2^{-9}$	$2^{-9}$
23	(000300040000007)	(000000030009000B)	3	$2^{-9}$	$2^{-9}$
50	(300070000004000)	$egin{array}{llllllllllllllllllllllllllllllllllll$	0	$2^{-9}$ $2^{-9}$ $2^{-9}$	$2^{-7.4150}$
51	(0300070000000400)	$egin{array}{llllllllllllllllllllllllllllllllllll$	1	$2^{-9}$ $2^{-9}$ $2^{-9}$	$2^{-7.4150}$
52	(003000700000040)	$egin{array}{llllllllllllllllllllllllllllllllllll$	2	$2^{-9}$ $2^{-9}$ $2^{-9}$	$2^{-7.4150}$
53	(0003000700000004)	$egin{array}{llllllllllllllllllllllllllllllllllll$	3	$2^{-9}$ $2^{-9}$ $2^{-9}$	2-7.4150

•  $CK_{31} \leftarrow algorithm \ 3$ 1) n = 900,  $S^0 = (2000B0000006000),$   $CK_{31} = 1;$ 2)  $\overline{CK} = CK \oplus \alpha(31);$ 3) for  $i \in \{1, 2, \dots, n\}$  do (a)  $C(i) \stackrel{\$}{\leftarrow} \{0, 1\}^{64};$ (b)  $C'(i) = C(i) \oplus S^0;$ (c)  $\overline{C(i)} = Enc(Dec(C(i), CK), \overline{CK});$ (d)  $\overline{C'(i)} = Enc(Dec(C'(i), CK), \overline{CK});$ (e)  $\Delta(i) = \overline{C(i)} \oplus \overline{C'(i)};$ f) if 8 low-value nibbles of  $\Delta(i)$  are zero then (b)  $\sum_{i=n;}^{1} \operatorname{return} CK_{31}.$ 

Algorithm 3. Recovering the control signal bit  $CK_{31}$ .

- Recovering the control signal bit  $CK_{31}$  by Algorithm 3.
- Recovering the round key  $K_0$  by running four times Algorithm 4 and one time Algorithm 5. In this step, Algorithm 6 is called inside Algorithm 4.

 Recovering the control signal bit CK<sub>l</sub> and after that the round key RK<sup>l</sup>, by running Algorithm 7, 31 times for l ∈ {30, · · · , 0} respectively.

Then it returns the  $K = RK^0 \parallel CK_0 \parallel \cdots \parallel CK_{31}$  as the main key of the SFN cipher. An overview of the second key recovery attack on SFN as schematically is shown in Figure 6.

#### Extracting the $CK_{31}$ (Algorithm 3)

Suppose  $S^0$  is the input difference of characteristic No. 1 in Table 3. For  $i = 1, \dots, n$  where n is a natural number greater than 64, choose a random ciphertext C(i) and put  $C'(i) = C(i) \oplus$  $S^0$  and quarry from the oracle O-RK to produce Dec(C(i), CK) and Dec(C'(i), CK), and then we quarry for  $\overline{C(i)} = Enc(Dec(C(i), CK), CK \oplus \alpha(31))$ and  $\overline{C'(i)} = Enc(Dec(C', CK), CK \oplus \alpha(31))$  and define  $\Delta(i) = \overline{C(i)} \oplus \overline{C'(i)}$ . The probability of characteristic No. 1 is  $2^{-6}$ , so we expected that the values of the 8 low-value nibbles of  $\Delta(i)$  to be zero •  $(K_0)_j, (K_0)_{(4+j)}, (K_0)_{(12+j)} \leftarrow algorithm \ 4 \ (j, CK_{31})$ 1)  $J_0 = J_1 = J_2 = GF_2^4$  $CTR_0[16] = CTR_1[16] = CTR_2[16] =$  $\{0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0\},$  $MS_0 = MS_1 = MS_2 = \phi,$  $flag = 0, \quad n = 30;$ 2) if  $CK_{31} = 0$  then CK' = CK;else  $CK' = CK \oplus \alpha(31);$ 3)  $a_0 = j, a_1 = 4 + j, a_2 = 12 + j,$  $b_0 = 8, b_1 = 12, b_2 = 4;$ 4) for  $Rep \in \{1, 2, \dots, n\}$  do for  $m \in \{1, 2\}$  do | a)  $(CTR_r, r \in \{0, 1, 2\}) \leftarrow Algorithm 6$  $(m, j, CK', CTR_r, J_r, r \in \{0, 1, 2\});$ b) for  $r \in \{0, 1, 2\}$  do \* if  $|J_r| > 1$  then 1) put  $MS_r$  equal to the set of all k which the value of  $CTR_r[k]$  is equal to the maximum value of all values of 16 elements of  $CTR_r$ ; 2)  $J_r = J_r \cap MS_r$ ; c) if  $|J0| = |J_1| = |J_2| = 1$  then flag = 1, m = 2, n = 30; \* return the value of flag and for  $r \in \{0, 1, 2\}$  the unique element of  $J_r$  as the nibble  $(K_0)_{a_r}$ . 5) if flag = 0 then print: "The three nibbles of  $K_0$  can not be found with these values of parameters: the value of m, Rep, or both of them have to be increased", and then return the value of the flag.

**Algorithm 4.** Recovering three nibbles of  $K_0$  in  $\Gamma_{32}$ .

```
• (K_0)_l (l \in \{8, 9, 10, 11\}) \leftarrow
  algorithm 5(CK_{31}, (K_0)_l (l \in (GF_2^4 - \{8, 9, 10, 11\}))
1) C_0 \xleftarrow{\$} \{0,1\}^{64};
2) if CK_{31} = 0 then
     CK' = CK;
else
    CK' = CK \oplus \alpha(31);
3) \overline{CK'} = CK' \oplus \alpha(31);
4) C_1 = Enc(Dec(C_0, CK'), \overline{CK'});

5) for i \in \{0, \dots, 2^{16} - 1\} do

a) K'_0 = ((K_0)_0 \parallel \dots \parallel (K_0)_7 \parallel i \parallel (K_0)_{12} \parallel \dots \parallel K_0)
        (K_0)_{15});
      b) Find \overline{RK^{31}};
                                        \triangleright By the Feistel structure in
        backward direction at \Gamma_{32} cipher and using the
        value of K'_0 find \overline{RK^{31}};
                              \triangleright At \Gamma_{32} cipher, for plaintext C_0
      c) Find C'_1;
        and main key \overline{RK^{31}} find the corresponding
        ciphertext: C'_1;
      d) if C'_1 = C_1 then
             Return the value of i as
               (K_0)_8 \parallel \cdots \parallel (K_0)_{11}.
```

**Algorithm 5.** Recovering four nibbles of  $RK^{31}$ , exhaustive search.

(suitable case) in at least  $n/64 \ge 1$  times out of these n cases. If for one i the  $\Delta(i)$  satisfies the condition, then conclude  $CK_{31} = 0$ , the reason for this conclusion is the Remark 1, and otherwise conclude  $CK_{31} = 1$ . For n = 900 the probability of the case in which

•  $CTR_r (r \in \{0, 1, 2\}) \leftarrow$ algorithm 6  $(m, j, CK', CTR_r, J_r (r \in \{0, 1, 2\}))$ 1) n = 900,  $\overline{CK'} = CK' \oplus \alpha(31);$ 2)  $a_0 = j$ ,  $a_1 = 4 + j$ ,  $a_2 = 12 + j$ ,  $b_0 = 8$ ,  $b_1 = 12$ ,  $b_2 = 4$ ; 3) for  $i \in \{1, \dots, n\}$  do a) Initialize  $S^0, S^2;$  $\triangleright$  put them equal to the inputs differential of characteristic number mwith j nibbles rotation of table 4. b)  $C_0(i) \xleftarrow{\$} \{0,1\}^{64};$ c)  $C'_0(i) = C_0(i) \oplus S^0;$ d)  $C_1(i) = Enc(Dec(C_0(i), CK'), \overline{CK'});$ e)  $C'_1(i) = Enc(Dec(C'_0(i), CK'), \overline{CK'});$ f)  $\Delta(i) = C_1(i) \oplus C'_1(i);$ g) if 8 low-value nibbles of  $\Delta(i)$  are zero then for  $r \in \{0, 1, 2\}$  do if  $|J_r| > 1$  then for  $k \in \{0, 1, \cdots, 15\}$  do if  $S_1((C_0(i))_{a_r} \oplus k) \oplus$  $S_1((C'_0(i))_{a_r} \oplus k) = (S^2)_{b_r}$ then \* add  $CTR_r[k]$  one unit; return  $CTR_0$ ,  $CTR_1$  and  $CTR_2$ .



```
• CK_l \leftarrow Algorithm 7
 (l, CK_i, RK^i(l+1 \le i \le 31))
1) n = 900,
   S^0 = (2000B0000006000),
   CK_l = 1;
2) \overline{CK} = CK \oplus \alpha(l);
3) for i \in \{1, 2, \cdots, n\} do
     a) C_{(l+1)}(i) \xleftarrow{\$} \{0,1\}^{64};
     b) C'_{(l+1)}(i) = C_{(l+1)}(i) \oplus S^0;
     c) C(i) =
       Enc(C_{(l+1)}(i), RK^{(l+1)\sim 31}, CK_{(l+1)\sim 31}, l+1),
         C'(i):
       Enc(C'_{(l+1)}(i), RK^{(l+1)\sim 31}, CK_{(l+1)\sim 31}, l+1);
     d) \overline{C(i)} = Enc(Dec(C(i), CK), \overline{CK});
     e) \overline{C'(i)} = Enc(Dec(C'(i), CK), \overline{CK});
     f) C_{(l+1)}(i) =
         Dec(\overline{C(i)}, RK^{(l+1)\sim 31}, CK_{(l+1)\sim 31}, l+1),
         \overline{C'_{(l+1)}(i)} =
         Dec(\overline{C'(i)}, RK^{(l+1)\sim 31}, CK_{(l+1)\sim 31}, l+1);
     g) \Delta_{(l+1)}(i) = \overline{C_{(l+1)}(i)} \oplus \overline{C'_{(l+1)}(i)};
     h) if 8 low-value nibbles of \Delta_{(l+1)}(i) are zero
       then
       | CK_{(l)} = 0 \ i = n;
4) Return CK_{(l)} as the signal bit CK_l.
```

**Algorithm 7.** Recovering the control signal bit  $CK_l$  for a l in the set  $\{0, ..., 30\}$ .

 $CK_{31} = 0$  and there is not any suitable case for i, so the program returns an incorrect value for  $CK_{31}$ , is equal to  $(1 - 2^{-6})^{900} \simeq 7 \times 10^{-7}$ . It is obvious by choosing larger n, we can make the previous probability smaller and smaller. Therefore we expect the program



Figure 6. Framework of the second key recovery attack of SFN cipher.

to return the correct value for  $CK_{31}$  when we choose a value sufficiently large for n. We examined it for ten million random cases when we had chosen n = 900: the program returned the correct value in all cases, so we choose this value for n in the program.

## Extracting three nibbles of the $RK^{31}$ (Algorithms 4 and 6)

We want to explain Algorithm 4 and a little about Algorithm 6 which is called by it, here. Suppose  $K_0 = ((K_0)_0 \cdots (K_0)_{15})$  and  $j \in \{0, 1, 2, 3\}$ . Inputs of Algorithm 4 are a value j and the signal bit  $CK_{31}$ and its output is nibbles  $(K_0)_j, (K_0)_{j+4}, (K_0)_{j+12}$ . In "3" we define  $a_0 = j$ ,  $a_1 = j + 4$ ,  $a_2 = j + 12$ : The indexes of nibbles of  $K_0$  which we want to recover them, and  $b_0 = 8$ ,  $b_1 = 12$ ,  $b_2 = 4$ : Which the nibble with index  $a_i - j$  in the differential  $S^0$  after swapping and passing from  $S_1$ -box goes to the nibble with index  $b_i$  in the differential  $S^2$  (Figure 5). Also we introduce for  $r \in \{0, 1, 2\}$ , the sets  $J_r$  which we want to choose the values of  $(K_0)_{a_r}$  from their elements. At the first in "1" we put  $J_r = GF_2^4$  and step by step they are updated (in "4.(b)\*(2)") and become smaller until all of them have only one element. Then if the conditions are satisfied in "(c)", we choose and return the unique element of  $J_r$  as the nibble  $(K_0)_{a_r}$  in "(c)\*". We introduce and initialize three 16 elements vectors  $CTR_0, CTR_1, CTR_2$  in "1". Algorithm 6 updates three vectors  $CTR_0$ ,  $CTR_1$ ,  $CTR_2$  and Algorithm 4 calls it several times (in "4.(a)"). For  $k \in \{0, 1, \dots, 15\}$ the element  $CTR_r[k]$  counts how many times the value k satisfies the conditions for  $(K_0)_{a_r}$ : in "3.(g)" at Algorithm 6 when k satisfies the conditions, the value of  $CTR_r[k]$  is added one unit.

Also we define three sets  $MS_r$  such that the set  $MS_r$  has all k which the value of  $CTR_r[k]$  is the maximum value between all 16 elements of vector  $CTR_r$  (in "4.(b)\*(1)"). These three sets are initialized to  $\phi$  at the first (in "1."), and they are applied for updating the sets  $J_r$ : for  $r \in \{0, 1, 2\}$  we update the sets  $J_r$  by intersecting them by  $MS_r$  (in "4.(b)\*(2)").

For m = 1 after updating the sets  $J_r$ , if each one of them have one element, the program return their unique element as the nibbles  $(K_0)_{a_r}$  in "4.(c)\*", if not it tries m = 2. After that if some of the sets  $J_r$  have more than one elements, the program adds one unit to *Rep* and repeats the previous steps again. If for all values of m and *Rep* the program can not find the three nibbles of  $K_0$ , then it print: "The three nibbles of  $K_0$  can not be found with these values of parameters: The number of m or the value of *Rep*, or both of them should be increased" and then return the value of flag. In our experiments with  $m \in \{1, 2\}$  the maximum value for *Rep* was 12 and by notice the maximum value of *Rep* in the program, i.e., 30, this case will not occur in real experiments.

#### Extracting the bits of $CK_l$ (Algorithm 7)

In Algorithm 7 we denote a ciphertext which encrypted l rounds at the SFN by  $C_{(l)}$ , so the plaintext is equal to  $C_{(0)}$  and the complete ciphertext which encrypted 32 rounds is equal to  $C_{(32)}$ , that usually we denote it by C. Suppose l is a fixed value in the set  $\{0, 1, \dots, 30\}$  and given the values of  $CK_i$ ,  $RK^{j}$  for every  $j = l + 1, \dots, 31$ . For recovering  $CK_{l}$ the same as Algorithm 3, suppose  $S^0$  is the input differential of characteristic No.1 in Table 3:  $S^0$  is initialized at "1.". In "2." define  $\overline{CK} = CK \oplus \alpha(l)$ and in "3.(a)" for  $i = 1, \dots, n$ , where n = 900, choose a random 64 bits string  $C_{(l+1)}(i)$  and at "3.(b)" put  $C'_{(l+1)}(i) = C_{(l+1)}(i) \oplus S^0.$  Consider both of  $C_{(l+1)}(i)$ and  $C'_{(l+1)}(i)$  as ciphertexts which encrypted l+1rounds with the signal string CK. In "3.(c)" by using the control signal bits  $CK_i$  and round keys  $RK^i$  for  $i \ge l+1$ , encrypt  $C_{(l+1)}(i)$  and  $C'_{(l+1)}(i)$  for 31-l rounds encryption more, to reach the complete ciphertexts  $C_{(32)}(i) = C(i)$  and  $C'_{(32)}(i) = C'(i)$ . In "(3.(d), 3.(e))" request from the oracle O-RKto give the Dec(C(i), CK), Dec(C'(i), CK) and  $Enc(Dec(C(i), CK), \overline{CK}), Enc(Dec(C'(i), CK), \overline{CK}))$ which we denote them by  $\overline{C(i)}, \overline{C'(i)}$  respectively. In "3.(f)" by using the control signal bits  $CK_i$  and round keys  $RK^i$  for  $i \geq l+1$ , decrypt C(i), C'(i) for 31 - l rounds, to reach two l + 1 encrypted ciphertexts  $\overline{C_{(l+1)}(i)}$  and  $\overline{C'_{(l+1)}(i)}$ . In "3.(g)" define  $\Delta_{(l+1)}(i)$ and in "3.(h)" if 8 low-value nibbles of  $\Delta_{(l+1)}(i)$  are zero, then put  $CK_{(l)} = 0$  and return it as the signal bit  $CK_l$ , and otherwise go to next *i*. If there is not any *i* which for it the condition at "3.(h)" satisfies, then return  $CK_{(l)}$  which is initialized at "1." to 1, as the signal bit  $CK_l$ . For the probability of correctness of obtained  $CK_l$  refer to Remark 1 is not any such characteristic and extracting the  $CK_{31}$  at 4.2.

#### Extracting the main key (Algorithm 2)

For recovering the main key of the SFN cipher, one can apply the Algorithm 2. First in "1." by calling Algorithm 3 recover the signal bit  $CK_{31}$ . Then in "2." assume the number j, as the number for nibbles rotation at the input of the characteristics of Table 3, and by calling 4 times Algorithm 4, recover the nibbles with indexes  $\{0, 1, 2, 3, 4, 5, 6, 7, 12, 13, 14, 15\}$  and after that in "3." by calling Algorithm 5, by exhaustive search, recover the nibbles with indexes  $\{8, 9, 10, 11\}$ of the key  $K_0$  at the new scheme  $\Gamma_{32}$ . By knowing the value of  $K_0$  and with notice to the structure of the new scheme  $\Gamma_{32}$ , in "4." with Feistel structure in backward direction, get the value of round key  $RK^{31}$ . Then at "5." for  $l \in \{30, \dots, 0\}$ , in 31 steps and at each step, by calling the Algorithm 7 and recovering the signal bit  $CK_l$ , with Feistel or SP structure in backward direction (if  $CK_l$  is equal to 0 or 1 respectively), recover the round key  $RK^{l}$ . Finally in "6." return the value  $RK^0 \parallel CK_0 \parallel \cdots \parallel CK_{31}$  as the secret key of the SFN block cipher.

#### Complexity of the second recovery attack

Suppose we consider the maximum time of encryption or decryption for a 64 bits plaintext or ciphertext, as a unit of time. Hear we want to compute an upper bound of the computational time complexity in the term of this unit for the second key recovery attack or related key with chosen-plaintext-ciphertext attack for recovering the 96 bits main key of the SFN block cipher. For this purpose we should compute the time for running Algorithm 2. First we compute the time complexity for Algorithms 3,4,5,7 and then we compute the time complexity of Algorithm 2 which calls these algorithm inside itself. In each case we also compute the data complexity:

- 1. The time for running Algorithm 3 is dominated by the rows "3.(c)" and "3.(d)". At each row there are one decryption and one encryption, so the time complexity of this algorithm is upper bonded to  $2 \times 2 \times n = 2 \times 2 \times 900 = 3600 \le 2^{11.82}$ . At this algorithm in "3.(a)" a ciphertext is chosen randomly and it is repeated almost 900 times, so its data complexity is upper bounded to  $900 \times 1 = 2^{9.82}$ ciphertexts.
- 2. First we compute the time complexity of Algorithm 6 which is called inside of Algorithm 4. The run-time of Algorithm 6 is dominated by the rows "3.(d)" and "3.(e)", and at each row there are one encryption and one decryption. These two row are done 900 times, so its run-time as same as Algorithm 3, is upper bounded to 2<sup>11.82</sup>. The data complexity of Algorithm 6 is similar to the Algorithm 3 and is upper bounded to 2<sup>9.82</sup>. The run-time at Algorithm 4 is dominated by the row

"4.(a)". This row is done at most  $2n = 2 \times 30 = 60$ times, therefore its run-time is upper bounded to  $60 \times 2^{11.82} \leq 2^{17.73}$ . The data complexity of Algorithm 4 is related to calling Algorithm 6, and this algorithm is called at most  $2 \times 30 = 60$ , by considering the data complexity of the Algorithm 6, we can conclude the data complexity of Algorithm 4 is upper bounded to  $60 \times 2^{9.82} \leq 2^{15.73}$ .

- 3. The run-time of Algorithm 5 is related to rows "4.", "5.(b)" and "5.(c)". At "4." there are one decryption and one encryption. The run-time for each row of two rows "5.(b)" and "5.(c)" is less than  $\frac{1}{32}$  of the run-time for one round of the SFN cipher, so the total run-time for Algorithm 5 can be computed as follows:  $2+2^{16} \times (2 \times \frac{1}{32}) \leq 2^{12.01}$ . The data complexity of Algorithm 5 is one ciphertext which is chosen randomly at "1.".
- 4. The rows "3.(c)", "3.(d)", "3.(e)" and "3.(f)" are the main role at the run-time of Algorithm 7. The run-times of rows "3.(c)" or "3.(f)" are less than one encryption or decryption respectively which both are less than one unit. The run-time of rows "3.(d)" or "3.(e)" are 2 units. These 4 rows are done at most 900 times, so the time complexity of Algorithm 7 is upper bounded to 900 × (1 + 2 + 2 + 1) ≤ 900 × 6 ≤ 2<sup>12.40</sup>. The data complexity of Algorithm 7 is dominated by "3.(a)". This row is done 900 times at most, so the data complexity of this algorithm is equal to 900 × 1 = 900 ≤ 2<sup>9.82</sup>.
- 5. The run-time of Algorithm 2 is related to two sources:first, calling other algorithms at row "1." one time (Algorithm 2), at row "2." 4 times (Algorithm 4), at row "3." one time (Algorithm 5), at row "5.(a)" 31 times (Algorithm 6) which the runtime of all these algorithms have been computed before, and second the computing rounds key at "4." one time, "5.(b)" 31 times, which their runtime are less than one round decryption or  $\frac{1}{32}$  unit of time. Therefore the total time complexity of Algorithm 2 is upper bounded to  $2^{11.82} + 4 \times 2^{17.73} + 2^{12.01} + 31 \times 2^{12.40} + \frac{1}{32} + 31 \times \frac{1}{32} \leq 2^{20}$ . The data complexity of Algorithm 2 by noticing the data complexities of other algorithm which it calls them is as follows:  $2^{9.82} + 4 \times 2^{15.73} + 1 + 31 \times 2^{9.82} \leq 2^{17.92}$ .

#### 4.3. Experimental results

By noticing the small time complexity of the second key recovery attack on the SFN block cipher, i.e.,  $2^{20}$ , a practical experiment was possible. So we decided to make a program to check it experimentally. Algorithms 3, 4, 5 and 7 are the main role at Algorithm 2. Algorithm 7 is almost similar to Algorithm 3 and Algorithm 5 is an exhaustive search, so we made a program by C++ language (https://github.com/MajidMNiknam/

SFN-cipher/commit/8688ecaaed83e49633d94217

6c40c22154b879ac) for checking experimentally Algorithms 3 and 4: First program for recovering the signal bit  $CK_{31}$  and the second one for recovering the nibbles  $\{0, 1, \dots, 7, 12, 13, 14, 15\}$ of the round key  $K_0$  at new scheme  $\Gamma_{32}$ . Our program can find both of  $CK_{31}$  and nibbles  $(K_0)_k$ for  $k \in \{0, 1, \dots, 7, 12, 13, 14, 15\}$  separately and it is based on Algorithms 3, 6 and 4. It has been checked 10 billion times for recovering the signal bit  $CK_{31}$  and the nibbles  $\{(K_0)_0, (K_0)_4, (K_0)_{12}\},\$  $\{(K_0)_1, (K_0)_5, (K_0)_{13}\}, \{(K_0)_2, (K_0)_6, (K_0)_{14}\}, \text{ and }$ than  $\{(K_0)_3, (K_0)_7, (K_0)_{15}\}$ , and it always returned the correct values for them. The program ran on a laptop with below specifications in less than one second:

Intel(R) Core(TM) i7-6500U CPU,@ 2.50GHz 2.59 GHz, RAM 8.00 GB (7.87 GB usable), 64-bit operating system, x64-based processor.

The program works as follows: First, the signal bit  $CK_{31}$  and the 64 bits round key  $RK^{31}$  are chosen randomly. By the value of  $RK^{31}$ , the keys  $K_0$ , and  $K_1$  of  $\Gamma_{32}$  are made, and their value could be used only by oracle O-RK. The program recovers the signal bit  $CK_{31}$  first, and after that the value of three nibbles  $(K_0)_j, (K_0)_{j+4}, (K_0)_{j+12}$  where  $j \in \{0, 1, 2, 3\}$  is fixed. In the algorithm the number "Rep", as in Algorithm 4, is used for repetition, also at each repetition when the algorithm wants to choose a random ciphertext, for more randomness, "Rep" is used as a coefficient of the number which is generated by "rand" function of C++. The other notations are the same as ones at Algorithms 3 and 4.

The result related to recovering three nibbles  $(K_0)_0, (K_0)_4, (K_0)_{12}$  for 4 random cases one to four are shown at Table 5. The first column shows the number of characteristic at Table 3. The second column to seventh one show the sets  $J_0, MS_0, J_1, MS_1$  and  $J_2, MS_2$  respectively. The penultimate column shows the number of random ciphertexts used for recovering the nibbles, and the numbers of pairs with specified input/output differentials between them. The blue color are the recovered nibbles of  $K_0$  at last row, while they are red at the  $K_0$  in first row and other places in every recovering. In each row, for  $r \in \{0, 1, 2\}$  the set  $J_r$  is equal to intersection of the set  $MS_r$  at the same row with the set  $J_r$  at the previous row. When the number of elements in the set  $J_r$  becomes 1, then its element is  $(K_0)_{a_r}$  which  $a_r$  is 0, 4 or 12.

At this experiment for recovering the three nibbles  $(K_0)_0$ ,  $(K_0)_4$ ,  $(K_0)_{12}$ , the number of random ciphertexts that were used: in case one was equal to  $3(2 \times 900) = 5400$  (Rep=3), in case two to four was equal to  $2 \times 900 = 1800$  (Rep=1). Also for 10 billion repetitions for recovering these nibbles, the average and its maximum number of random ciphertexts that were used were equal to 2314.76 and 19800 in case one, 2173.90 and 12600 in case two, 2174.50 and 14400 in case three, 4045.47 and 21600 in case four, respectively. So the experimental data complexity of this algorithm on average was  $2^{11.98}$  and its maximum was  $2^{14.4}$ , while the theoretical data complexity for this algorithm has been computed before  $2^{15.73}$ .

#### 5. Meet in the middle attack

In MITM attack, the cipher is divided into two parts and the main idea is that the subkeys of key bits in both parts of the cipher can be guessed independently. In 2010, Bogdanov et al., introduced a new variant of MITM attack (3-subset MITM attack) on block ciphers [6]. Instead of considering two subsets of key bits, they considered three subsets as  $A_1$  that shows the key bits used only in the first part,  $A_2$  that shows the key bits used only in the second part, and  $A_0$  that shows the key bits used in two parts of the cipher.

Following the SFN's description, given the 96-bit main key K = RK|CK, the fraction  $RK \in \{0,1\}^{64}$  is used to generate the round keys, and  $CK \in \{0,1\}^{32}$ is used as the control signal to determine whether in each round key-expansion/round-function the Feistel structure is used or the SP one. Notice that each bit of the control signal is used in one and only one round of the SFN, hence, this block cipher will be an appropriate candidate for the 3-subset MITM attack. Therefore, inspired by [6], suppose  $A_1 = CK_{0 \sim 15}$ ,  $A_2 = CK_{16\sim31}$ , and  $A_0 = RK$ , are the three subsets of key bits used in SFN structures. The procedure of the key recovery of the SFN in the 3-subset meet in the middle attack is given in Algorithm 8. Now, if the adversary guesses are correct then the internal values should match, i.e.,  $P^{16} = P'^{16}$ . These happen for the correct guess of keys with the probability of 1 while for the wrong guess of keys the matching proba-

• $K \leftarrow algorithm \ 8(A_0, A_1, A_2)$
for a known $plaintext/ciphertext$ pair do
for each $2^{64}$ choice of key bits in $A_0$ do
<b>for</b> each $2^{16}$ choice of key bits in $A_1$ do
Encrypt 16 rounds SFN to calculate the
value of $P^{16}$ ;
for each $2^{16}$ choice of $A_2$ do Decrypt 16 rounds SFN to calculate the value of $P'^{16}$ ;
Execute matching between the values of $P^{16}$
and $P'^{16}$ on 64 bits;
if $P^{10} = P'^{10}$ then
Return the related key as correct round key.
else
Abort the related key.

Algorithm 8. The 3-subset MITM attack of the SFN.

**Table 5.** The experimental results for recovering  $CK_{31}$ , and three nibbles with indexes 0, 4 and 12 of  $K_0$  at  $\Gamma_{32}$  for 4 random keys: one to four. The blue color are the recovered nibbles of  $K_0$  at last row in every case, while they are red at the  $K_0$  in first row and other places.

One	$CK_{31} = 1$	$K_0 = 0x$	18be 6784 a	$484 \ ef{55}$	$RK^{31}=0x0029\;4823\;18be\;6784$					
No. of ch.	$J_0 = GF_2^4$	$MS_0$	$J_1 = GF_2^4$	$MS_1$	$J_2 = GF_2^4$	$MS_2$	# pair	Rep		
1	$\{5,7,c,e\}$	$\{5,7,c,e\}$	$\{4, 6, d, f\}$	$\{4, 6, d, f\}$	$\{8, a, c, {\color{red} {e}}\}$	$\{8, a, c, {\color{red} {e}}\}$	900, (18)	1		
2	$\{5,7,c,e\}$	$GF_2^4$	$\{4, 6, d, f\}$	$GF_2^4$	$\{8, a, c, {\color{red} {e}}\}$	$GF_2^4$	900, (0)	1		
1	$\{5,7,c,e\}$	$\{5,7,c,e\}$	$\{4, 6, d, f\}$	$\left\{ 4,6,d,f ight\}$	$\{8, a, c, {\color{red} {e}}\}$	$\{8, a, c, {\color{red} {\bf e}}\}$	900, (16)	2		
2	$\{5,7,c,e\}$	$GF_2^4$	$\{4, 6, d, f\}$	$GF_2^4$	$\{8, a, c, {\color{red} {e}}\}$	$GF_2^4$	900, (0)	4		
1	$\{5,7,c,e\}$	$\{5,7,c,e\}$	$\{4, 6, d, f\}$	$\{4, 6, d, f\}$	$\{8, a, c, {\color{red} {e}}\}$	$\{8, a, c, {\color{red} {e}}\}$	900, (13)	3		
2	$\{5\}$	$\{5, 6\}$	<b>{4}</b>	$\{0, 4\}$	$\{e\}$	$\{9, \boldsymbol{e}\}$	900, (5)	5		
Two	$CK_{31} = 0$	$K_0 = 0x$	x42da 718d de	cc <mark>0</mark> 40 <i>b</i> 9	$RK^{31} = 0x02a4\ 3024\ 42da\ 718d$					
No.	$J_0 = GF_2^4$	$MS_0$	$J_1 = GF_2^4$	$MS_1$	$J_2 = GF_2^4$	$MS_2$	# pair	$\operatorname{Rep}$		
1	$\{0,2,{\color{red}9},b\}$	$\{0,2,{\color{red}9},b\}$	$\{0, 2, 9, b\}$	$\{0, 2, 9, b\}$	$\{8, \mathbf{a}, c, e\}$	$\{8, \mathbf{a}, c, e\}$	900, (15)	1		
2	$\{9\}$	$\{9,a\}$	<b>{0}</b>	{ <mark>0</mark> , 4}	{ <b>a</b> }	$\{\mathbf{a}, d\}$	900, (2)	1		
Three	$CK_{31} = 1$	$K_0 = 0.2$	r284 <mark>c</mark> 4948 c3	$0c \ 6a77$	$RK^{31} =$	= 0x43c7 76j	fa 284c 4948	3		
No.	$J_0 = GF_2^4$	$MS_0$	$J_1 = GF_2^4$	$MS_1$	$J_2 = GF_2^4$	$MS_2$	# pair	$\operatorname{Rep}$		
1	$\{5, 7, c, e\}$	$\{5, 7, c, e\}$	$\{5,7,{\color{black}c},e\}$	$\{5,7,{\color{red}c},e\}$	$\{8, a, {\color{black} c}, e\}$	$\{8, a, \boldsymbol{c}, e\}$	900, (14)	1		
2	<b>{7</b> }	$\{4, 7\}$	$\{c\}$	$\{8, \boldsymbol{c}\}$	$\{c\}$	$\{b, {\color{black} {m c}}\}$	900, (2)	1		
Four	$CK_{31} = 0$	$K_0 = 0a$	$c67d4 \ 0097 \ 6e$	a0 d1d5	$RK^{31} =$	= 0x1db3 707	f 67d4 0097	7		
No.	$J_0 = GF_2^4$	$MS_0$	$J_1 = GF_2^4$	$MS_1$	$J_2 = GF_2^4$	$MS_2$	# pair	$\operatorname{Rep}$		
1	$\{5,7,c,e\}$	$\{5,7,c,e\}$	$\{0, 2, 9, b\}$	$\{0,2,9,b\}$	$\{0,2,{f 4},6\}$	$\{0, 2, 4, 6\}$	900, (11)	1		
2	$\{5\}$	$\{5, 6\}$	<b>{0}</b>	$\{0, 4\}$	$\{4\}$	$\{3, 4\}$	900,(2)			

bility would be  $2^{-|P^{16}|}$ . Therefore, with a probability of about  $2^{-|P^{16}|}$  this match would result in a false positive, but overall the number of key candidates is reduced to about  $2^{|K|} \times 2^{-|P^{16}|} = 2^{96-64} = 2^{32}$ after applying Algorithm 8. Thus, the number of key candidates is small enough that it has no effect on attack complexity. However, by considering another known plaintext/ciphertext (P', C') the number of key candidates can be reduced to about  $2^{32} \times 2^{-64} = 2^{-32}$ and thus the target key will be obtained.

Following the previous discussion, considering the cost of the decryption round the same as the cost of the encryption round, the time complexity of the provided attack would be equal to:

$$\underbrace{2^{|A_0|}(\frac{1}{2}(2^{|A_1|}+2^{|A_2|}))}_{\text{Algorithm 8}} + \underbrace{((2^{|K|-|P^{16}|}) + (2^{|K|-|P^{16}|} \times 2^{|C'|}) + \cdots)}_{\text{Key testing}}$$
$$= 2^{64}(\frac{1}{2}(2^{16}+2^{16})) + 2^{32} + 2^{-32} \simeq 2^{80},$$

calls to the SFN. Therefore, in total, we need only two known plaintext/ciphertext pairs (one for applying Algorithm 8 and one for the key testing step). which is at most  $2^{16} \times (80 + 80)$  bits,  $2^{20.32}$  bytes.

#### 6. Conclusion

This paper investigates the security level on the SFN against the related key attack. The encryption of the SFN involves an Substitution-Permutation (SP) network structure and a Feistel network structure. The SFN fixes a 64-bit block with a 96-bit key. We have proposed an attack, in the known-plaintext scenario, taking advantage of the related key distinguisher. With this attack, we have shown that FSN provides at most  $2^{60.58}$  encryptions security. We also proposed a chosenplaintext-ciphertext related key attack on the SFN with the complexity of  $2^{20}$ . In addition, in the single key mode, we presented a meet in the middle attack for which the time complexity was  $2^{80}$  and the memory complexity was  $2^{20.32}$  bytes. The attack complexity should be compared with the complexity of exhaustive key search which is  $2^{96}$ .

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#### **Conflicts of interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Authors contribution statement

Frist Author: Sadegh Sadeghi (Conceptualization; Data curation; Methodology; Formal analysis; Visualization; Writing-original draft; Writing-review and editing).

Second Author: Majid Mahmoudzadeh Niknam (Conceptualization; Data curation; Formal analysis; Investigation, Writing-original draft; Writing-review and editing).

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