

# An application of energy efficiency programs on multi-stage transmission network expansion and reactive power planning

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**Abstract.** Energy efficiency programs as an energy source with multiple advantages (low cost, more reliable and better clean) are considered as one of the most effective solutions to meet future energy needs. In this paper, energy efficiency programs (EEPs) are modelled as virtual sources of power generation to investigate their impacts on expanding transmission network and reactive power planning (RPP). A multi-stage model based on AC power flow has been used to indicate the possibility of postponing the investment actions as the investment deferral in transmission expansion planning (TEP). Two groups of regulatory support schemes are considered as investor income to promote participation in EEPs, namely purchasing certified emission reductions (CERs) and shared saving model. In addition, two standard case studies (Garver & 46-bus Brazilian) are evaluated to demonstrate the promising potential of the proposed model in handling the planning problems of practical power systems. The simulation results show the effectiveness of the proposed model to solve such planning problems in the presence of EEPs.

**Key words.** Energy efficiency programs; Transmission expansion planning; Reactive power planning; Emission reductions; Multi stage planning.

## 1. Introduction

Energy efficiency policies have been adopted globally to address the public concern about energy supplies, rising energy prices, and the environmental impacts associated with energy usage [1]. Energy efficiency programs (EEPs) are one of the least-cost and leading resources available to utilities to reducing energy consumption, saving the primary energy resources, addressing the climate changes, and reducing pollution emitted by burning fossil fuels. Moreover, investing in EEPs is one-third to half of the cost of generating the same amount of electricity from traditional power sources and can provide significant energy savings to the society, which is also beneficial to the utility side [2]. Therefore, promoting EEPs in electricity usage are essential.

Due to the rapid growth of electric energy consumption, new transmission lines for transferring power from the supply centers to the load centers should be constructed that results in significant investment costs. Energy efficiency and demand response programs (DRs) as load management subsets play a vital role to reduce energy consumption and thus reduce environmental pollution, which can be adequately used in power systems planning. DRs change the load profile by shifting the peak-demand times to low-load times, while EEPs reduce the load level and can be more efficient in power system planning than the DRs [3]. EEPs have a high potential in postponing investment actions in transmission expansion planning (TEP). The scheduling horizon of the EEPs implementation is usually divided into long-term and mid-term. Since the impact of EEPs on electricity consumption is typically noticeable in later planning horizons, these options are more effective in long-term planning problems such as TEP problems.

In recent years, several types of researches have addressed the integration of EEPs as well as environmental issues in power systems scheduling and planning problems [4-5]. In [6], a model for energy efficiency market is

introduced, this model emphasises the basis for designing more efficient policies in energy efficiency market by examining and developing conventional models. An analytical approach to prioritizing a country's energy efficiency and formulating a practical plan to integrate energy efficiency as a resource for achieving a nation's energy access goals is described in [7]. A two-step approach to investigate the impact of improved energy efficiency on CO<sub>2</sub> emission at the macro level is proposed in [8], while an index decomposition analysis is used to obtain real energy efficiency by separating the impact of structural changes in the economic activities on energy intensity. In [9], a new model for simulating the effects of EEPs on the generation expansion planning is introduced, while a method for improving energy efficiency in a distribution system using reactive power sources in [10] is conferred. In [11], a two-stage model has been proposed to consider the impacts of DRs and EEPs in a smart grid environment. An overview of the potential of energy efficiency in reducing energy consumption as well as dropping the pollutants emission in the UK industry has been presented in [12]. Due to the nonlinear nature and complexity of an optimization problem, various innovative solution methods have been studied by researchers [13-15]. A comprehensive review of articles with the applications of heuristic methods to energy efficiency is presented in [16]. In [17], to accommodate the uncertainty and variability of wind power, an innovative scenario-based stochastic model that incorporates generation, transmission, and reactive power planning (RPP), based on relaxed AC optimal power flow is presented, this model seeks to balance investment and operation cost, while considering the spinning reserve, unit ramp rate, and current output of units. In [18], the impact of the integration of inverter-based distributed energy resources on the protection, control, operation and planning of power distribution network is investigated. A comprehensive review of recent studies on TEP from restructuring to renewable and distributed electricity markets and their challenges is presented in [19].

The high potential of EEPs on the TEP problems, on one hand, and the lack of a proper study in joint TEP and RPP problems simultaneously with EEPs, on the other hand, motivated the authors to provide an in-depth model to investigate the effects of combined EEPs on a joint TEP and RPP problems. The main contributions of this study are listed below:

- To propose an economic model for EEPs based on production function of electric energy consumption. To do so, EEPs are modeled as virtual sources of power generation.
- To introduce two groups of regulatory support schemes as investor income to promote participation in EEPs, namely purchasing certified emission reductions (CERs) and shared saving model.
- To propose a robust mixed-integer model for multi-stage planning to indicate the possibility of investment deferral.
- To use and extend AC model for multi-stage planning to assess the loss of real and reactive power to consider voltage constraints.

The rest of this paper is structured as follows. The proposed construction for the EEPs model in the TEP&RPP problem is investigated in Section 2. The solution methodology as well as solution algorithm principles for the proposed model are described in Section 3; the proposed model has been employed on test systems in Section 4. The conclusion is presented in Section 5.

## **2. EEPs associated with TEP&RPP**

### **2.1. EEPs**

Energy efficiency can be simply defined as using less energy to produce similar or better products, services or facilities. Energy efficiency can be implemented by replacing out-of-date appliances, practices, and technologies with new ones that consume less energy [20]. Energy efficiency improvements can be offered at several critical points of an energy system. In homes and offices, it can be considered as tightening building envelopes to prevent wasting the energy used for heating, ventilation and air conditioning, replacing incandescent light bulbs with LEDs, swapping out old appliances with new ones, etc [21]. On the generation side, a power plant can be upgraded to burn less natural gas or coal while still generating the same amount of electricity, if not more. Cars can be designed to go further on a gallon

of gases [22], or hybrid electric vehicles can use a management system to optimally manage the fuel consumption [23].

Implementation of EEPs in the electricity generation, transmission and consumption sectors can noticeably reduce electricity demand in the grid, which can enhance the reliability of the electricity system. It also saves money and can be more efficient and cost effective than alternative investments to strengthen the power system and production, transmission and distribution infrastructure. Therefore, energy efficiency can be called as the best medicine to meet the future needs of power system developments. Today, energy efficiency is considered as a great potential in power systems that can reduce greenhouse gas emissions, save money and create jobs in addition to reducing peak load, and these advantages in response to economic worries and climate change have led lawmakers and regulators to strongly support energy efficiency through financial and technical incentives.

Since 1990, energy efficiency has become the third largest electricity supplier in the United States. Regardless of energy efficiency plans, more than 300 additional large power plants are needed to meet US energy needs. It is anticipated that if energy productivity standards, applications, and energy efficiency codes in buildings reach their full potential, energy efficiency will become the largest US electricity supplier by 2030 and will have many benefits. Figure 1 shows the share of each US power generation resource in 2030 with the increased energy efficiency policies [24].

Energy efficiency can also perform the same function of transmission and distribution sources in power systems and reduce power through transmission lines and equipments. These reductions can delay the need for upgrading traditional network infrastructure or even prevent new equipment from being installed. Hence, in this paper, the significant impacts of energy efficiency on transmission network development planning will be examined.

Energy efficiency improvements decrease fossil fuel consumption and thereby mitigate emissions, and consequently, result in increasing social welfare and substantial health benefits [25]. Industrial EEPs can provide significant energy savings to society and the utility system at a lower cost than most programs targeted at other sectors [26]. The amount of electricity saved by industrial programs directly displaces the requirement to invest in expensive power plants or transmission and distribution system upgrades. The surcharges due to the investing in these assets will be on the shoulder of the customers and keeping the electricity bills high, therefore not investing or postponing the investment is a remedy to prevent increasing the bills [27].

## 2.2. EEPs model

In this paper, the introduction of a comprehensive model of EEPs associated with TEP&RPP is considered as one of the important issues. Therefore, this section presents a comprehensive mathematical formulation of the EEPs and TEP&RPP model. In this paper, virtual power plants, due to their effectiveness, are considered as the EEPs. These power plants are installed at the load centers and participate in providing electricity according to their characteristics.

In order to model the effects of energy efficiency investment costs on the demand side, a production function is used for electricity consumption as the EEP supply curve [9]. The proposed model of electricity consumption in the presence of EEPs depends on the price elasticity of electricity consumption and the elasticity of electricity consumption by considering EEP investment ( $EEI$ ). It is worth mentioning that for the sake of simplicity, only the self-elasticity of electricity consumption concerning the energy efficiency investment is taken into account and other elasticities are neglected.

This function is as follows:

$$E_t = D(EEI_t) \quad (1)$$

The EEPs is assumed to be divided into  $k$  types in terms of profit/cost ratio. The electricity consumption function in the presence of EEPs can be approximately linearized at  $k$  points by a Taylor series, while for the sake of simplicity, the second and higher orders of the partial derivatives are ignored. This function is linearized as follows:

$$D(EEI_t) = D(EEI_{0i}) + \frac{\partial D(EEI_{0i})}{\partial EEI_t} \times (EEI_t - EEI_{0i}); i = 1, \dots, d \quad (2)$$

The difference in power consumption after the presence of EEPs indicates the amount of power savings, as follows:

$$ES_{i,t} = D(EEI_t) - D(EEI_{0i}) \quad (3)$$

The electricity consumption sensitivity with respect to the investment of EEPs is defined as energy efficiency elasticity, which is expressed as the following equation:

$$\delta_{i,t} = \frac{\partial D(EEI_{0i})}{\partial EEI_t} \quad (4)$$

It should be noted that electricity consumption elasticity with energy efficiency investment,  $\delta_{i,t}$ , is negative because of the positive effects of EEPs on reducing the consumption and also for each EEPs can be numerically different. By putting Equations 2 and 4 in Equation 3, Equation 5 is obtained.

$$ES_{i,t} = \delta_{i,t} \times (EEI_t - EEI_{0i}) \quad (5)$$

The real assumption is that the priority of using EEPs is based on the lowest investment cost. Therefore, the cumulative saving of electricity can be achieved by collecting the amount of power savings from the implementation of previous EEPs as follows:

$$CES_{i,t} = \sum_{m=1}^{i-1} ES_{m,t}^{\max} - ES_{i,t} \quad (6)$$

Substituting Equation 5 in Equation 6, Equation 7 is obtained.

$$CES_{i,t} = \sum_{m=1}^{i-1} ES_{m,t}^{\max} - \delta_{i,t} \times (EEI_t - EEI_{0i}) \quad (7)$$

The cumulative saving of electricity due to investing in EEPs is illustrated by this equation. The energy efficiency investment function is obtained by presenting Equation 7 as Equation 8.

$$EEI_t = \frac{1}{\delta_{i,t}} \left( \sum_{m=1}^{i-1} ES_{m,t}^{\max} - CES_{i,t} \right) + EEI_{0i} \quad (8)$$

The total investment curve of EEPs is shown in Figure 2 as the investment function of cumulative electricity saving for all EEPs. Each section of this curve refers to a specific type of EEPs, e.g., the section between points X and the Y stands for the cost-saving function for the  $i^{th}$  type of EEP. From this curve, the marginal cost of energy savings for EEPs is obtained as Equation 9.

$$MC_{i,t} = -\frac{1}{\delta_{i,t}} \quad (9)$$

In this section of the paper, it is assumed that there are enough economic incentives to encourage investors to participate in EEPs. If the incentive is lower than a sufficient value, the investor will have no incentive to invest in these resources. Multifarious incentive-based support schemes have been designed to increase the penetration rate of the EEPs in the electricity system. Moreover, two groups of regulatory support schemes are considered as the income of EEP investors for promoting participation in EEPs, namely purchasing *CERs* and shared saving model.

*CERs* are a type of emissions unit (or carbon credits) issued by the Clean Development Mechanism (CDM) executive board for emission reductions achieved by CDM projects and verified by a Designated Operational Entity (DOE) under the rules of the Protocol. Purchasing *CERs* is one of the income sources for investors in EEPs [28]. This function is as follows:

$$f^{CER} = \sum_{t \in T} \lambda^{CER} \sum_{i=1}^k (EMF_{CO_2}) \times CES_{i,t} \quad (10)$$

Where the  $\lambda^{CER}$  is the *CERs* price (\$/ton),  $EMF_{CO_2}$  is the amount of carbon dioxide reduction due to reduced energy consumption (ton/MWh), and  $f^{CER}$  is the function of purchasing *CER* from EEPs. Moreover, a shared saving model is used to promote investors to participate in EEPs.

Energy service companies (ESCOs) develop, design, build, and fund EEPs that save energy, reduce energy costs and decrease operations and maintenance costs at their customers' facilities. In general, ESCOs act as project developers for a comprehensive range of energy conservation measures and take into account the technical and performance risks associated with a project [29]. In this case, ESCOs will invest in energy efficiency projects and

based on a predetermined percentage for several years, the cost savings are shared with consumers [30]. The following function is used:

$$f^{SSC} = \sum_{t \in T} SSC \times EEI_t \quad (11)$$

Where  $SSC$  is the sharing coefficient and  $f^{SSC}$  is the sharing function. The objective function of EEPs can be obtained as follows:

$$f^{EEP}(\mathbf{P}^{EEP}, \mathbf{u}_e) = \sum_{t \in T} EEI_t - f^{CER} - f^{SSC} \quad (12)$$

This objective function is used to find the best set of solution for EEPs model. The binary variable  $u_e$  shows the connection or disconnection of the virtual power plant to a demand bus;  $P^{EEP}$  is the amount of power that the EEPs can reduce in a given period and can be obtained by Equation 13.

$$P^{EEP} = \sum_{t \in T} CES_{i,t} \quad (13)$$

### 2.3. Multi-stage TEP & RPP model

Generally, there are two types of TEP problems, namely static and dynamic. The static TEP problem is the simplest model that considers the whole planning horizon in one stage and the lines that can be optimally used to reinforce the network are determined out of the candidate lines at one stage only. Investment is being carried out at the beginning of the planning horizon. The dynamic or multiple-year planning approaches define not only the optimal locations and types of the equipments but also the most appropriate times for making such investment. In the dynamic TEP problem, it is required to consider multi-time periods as well as the possible transmission reinforcements at each time. Investments are carried out at the beginning of each stage. In multi-stages TEP problems, the objective function is the minimization of the present value of the investment decisions carried out throughout the horizon.

From the mathematics perspective, multi-stage TEP problems are mixed-integer non-linear problems, and consequently, the problem is very complicated since, besides the number of circuits that must be added to the system, the development timeline should be considered too. By increasing the number of variables and constraints, the planning problem requires a lot of computational effort. Some useful examples of multi-stage models have been addressed in [31-34]. In this work, an AC model for multi-stage TEP is used to assess the loss of real and reactive power accurately. This model can provide the most economical TEP based on the scheduling development of power grids. In this model, one year is considered as the base year that TEP begins with. Concerning the annual interest rate  $I$ , the current value of investment costs for the base year  $t_0$  with the horizon of steps  $T$  is as follows:

$$\begin{aligned} c(x) &= c_1(x) + (1-I)^{t_1-t_0} c_2(x) + \dots + (1-I)^{t_T-t_0} c_T(x) \\ &= \sum_{i=1}^T (1-I)^{t_i-t_0} c_i(x) = \sum_{i=1}^T \delta_{inv}^i c_i(x) \end{aligned} \quad (14)$$

In Equation 14 all the financial terms are converted by an appropriate term to take into account the time value of financial investments. Where  $\delta_{inv}^i$  is the factor used to calculate the present investment value at stage  $t$  as follows:

$$\delta_{inv}^i = (1-I)^{t_i-t_0} \quad (15)$$

The mathematical model for multi-stage TEP and RPP problem can be formulated as follows:

**Objective function:** The objective function of this problem is to minimize the total cost of the system, including development planning costs as well as the investment on reactive power resources in a given planning horizon. The objective function can be calculated by Equation 16.

$$v_1 = \sum_{t=1}^T \delta_{inv}^t \left[ \sum_{(i,j)} c_{ij} \cdot n_{ij}^t + f(Q_G^t, \mathbf{u}_q) \right] \quad (16)$$

The first term of Equation 16 stands for the investment costs of transmission lines, and the second term represents the investment costs of reactive power resources. In the present work, to avoid the complexity of the model, the optimal planning of Var sources is done with shunt capacitors, assuming that these equipments are installed at high voltage

side and a portion of the reactive power consumption of the network is provided by them. The investment cost of reactive resources is presented as follows:

$$f(Q'_G, u_q) = \sum_{k \in \Omega_d} (c_{0d} + c_{1d} Q'_{Gd}) u_d \quad (17)$$

**Equality constraint:** active and reactive power should be adequately generated to satisfy the corresponding demands via Equation 18 and Equation 19, respectively.

$$P(V, \theta, n) - P_G + P_D = 0 \quad (18)$$

$$Q(V, \theta, n) - Q_G - Q_{G_0} + Q_D = 0 \quad (19)$$

Where  $n$  is the number of circuits (lines and transformers).

**Inequality Constraints:** The TEP&RPP problem is subject to several inequality constraints during the planning horizon [35], as Equation 20- Equation 26. The active and reactive generation is bounded within the lower and upper limits.

$$\underline{P}_G \leq P_G \leq \overline{P}_G \quad (20)$$

$$\underline{Q}_G \leq Q_G \leq \overline{Q}_G \quad (21)$$

$$\underline{Q}_G^0 \leq Q_G^0 \leq \overline{Q}_G^0 \quad (22)$$

$$\underline{V} \leq V \leq \overline{V} \quad (23)$$

$$(N + N^0) S^{\text{from}} \leq (N + N^0) \overline{S} \quad (24)$$

$$(N + N^0) S^{\text{to}} \leq (N + N^0) \overline{S} \quad (25)$$

$$0 \leq n \leq \overline{n} \quad (26)$$

Where Equation 20 stand for the upper and lower limits of active power generation, while Equation 21 and Equation 22 show the reactive power limitations of the new and existing sources, respectively; the voltage level is limited by Equation 23; transmission line MVA limits are enforced by Equation 24, Equation and 25, for sending and receiving points, respectively; and Equation 26 shows the maximum number of candidate lines to be installed. The elements of vectors P and Q are represented by Equation 27 and Equation 28, respectively.

$$P_i(V, \theta, n) = V_i \sum_{j \in N_B} V_j [G_{ij}(n) \cos \theta_{ij} + B_{ij}(n) \sin \theta_{ij}] \quad (27)$$

$$Q_i(V, \theta, n) = V_i \sum_{j \in N_B} V_j [G_{ij}(n) \sin \theta_{ij} - B_{ij}(n) \cos \theta_{ij}] \quad (28)$$

Where the admittance matrix elements G and B are represented by Equation 29 and Equation 30, respectively.

$$G = \left\{ \begin{array}{l} G_{ij}(n) = -(n_{ij} g_{ij} + n_{ij}^0 g_{ij}^0) \\ G_{ii}(n) = \sum_{j \in \Omega_d} (n_{ij} g_{ij} + n_{ij}^0 g_{ij}^0) \end{array} \right\} \quad (29)$$

$$B = \left\{ \begin{array}{l} B_{ij}(n) = -(n_{ij} b_{ij} + n_{ij}^0 b_{ij}^0) \\ B_{ii}(n) = b_i^{\text{sh}} + \sum_{j \in \Omega_d} [n_{ij} (b_{ij} + b_{ij}^{\text{sh}}) \\ + n_{ij}^0 (b_{ij}^0 + (b_{ij}^{\text{sh}})^0)] \end{array} \right\} \quad (30)$$

The elements  $ij$  of vectors  $S^{\text{from}}$  and  $S^{\text{to}}$  and the required definitions are given by Equation 31-36.

$$S_{ij}^{\text{from}} = \sqrt{(P_{ij}^{\text{from}})^2 + (Q_{ij}^{\text{from}})^2} \quad (31)$$

$$P_{ij}^{\text{from}} = V_i^2 g_{ij} - V_i V_j (g_{ij} \cos \theta_{ij} + b_{ij} \sin \theta_{ij}) \quad (32)$$

$$Q_{ij}^{\text{from}} = -V_i^2 (b_{ij}^{\text{sh}} + b_{ij}) - V_i V_j (g_{ij} \sin \theta_{ij} - b_{ij} \cos \theta_{ij}) \quad (33)$$

$$S_{ij}^{\text{to}} = \sqrt{(P_{ij}^{\text{to}})^2 + (Q_{ij}^{\text{to}})^2} \quad (34)$$

$$P_{ij}^{ro} = V_j^2 g_{ij} - V_i V_j (g_{ij} \cos \theta_{ij} - b_{ij} \sin \theta_{ij}) \quad (35)$$

$$Q_{ij}^{ro} = -V_j^2 (b_{ij}^{sh} + b_{ij}) + V_i V_j (g_{ij} \sin \theta_{ij} + b_{ij} \cos \theta_{ij}) \quad (36)$$

### 3. Solution methodology

In this paper, due to the complexity of the proposed multi-stage joint TEP and RPP in the presence of EEPs, a heuristic-based approach is used. The heuristic approach determines the required number of lines to be installed, Var compensators, and EEPs, while several iterations are conducted to obtain a high-quality solution that satisfies all the operational constraints.

#### 3.1. Solving process

The overall procedure for solving TEP&RPP associated with EEPs is as follows.

1. An initial set of solution is generated where each individual solution is randomly chosen.
2. At this stage, each solution is checked for cost. Those individual solutions whose investments costs are very high will be cut off.
3. The information of each individual solution is read out, and the new network based on this information is constructed. This information includes the number and location of new lines, and the location and size of VAR resources as well as features of EEP.
4. In this section, the TEP problem is formulated based on the AC OPF equations [35] and are solved for each individual solution according to the following objectives:

$$\min v = \sum_{i=1}^n (f_{1i}(P_{Gi}) + f_{2i}(Q_{Gi})) + f^{EEP}(P^{EEP}, u_e) + v_1 \quad (37)$$

$$P(V, \theta) - P_G + P_D - P^{EEP} = 0 \quad (38)$$

$$Q(V, \theta) - Q_G - q + Q_D = 0 \quad (39)$$

$$\underline{P}_G \leq P_G \leq \bar{P}_G \quad (40)$$

$$\underline{Q}_G \leq Q_G \leq \bar{Q}_G \quad (41)$$

$$\underline{q} \leq q \leq \bar{q} \quad (42)$$

$$\underline{P}^{EEP} \leq P^{EEP} \leq \bar{P}^{EEP} \quad (43)$$

$$S^{from} \leq \bar{S} \quad (44)$$

$$S^{from} \leq \bar{S} \quad (45)$$

$$S^{to} \leq \bar{S} \quad (46)$$

where  $v_1$  is the total investment cost of the system, including the costs of network expansion planning as well as the financial burden of reactive resources over a given horizon;  $f_{1i}$  and  $f_{2i}$  show the cost of active and reactive power generation by the generator  $i$ , respectively.

5. The fitness function for all individuals is calculated according to the results obtained in the previous step.
6. When the OPF problem is solved for the entire individual solutions, and the values are calculated, the selection, recombination, and mutation are carried out and a new set of the individual solutions is generated. When all the individual solutions are the same, there is no new individual, and the process can be stopped, while another stopping criterion is the number of generation.
7. According to the measures introduced to stop the algorithm and the convergence of the approach, the trends will be stopped or continued by going back to the second stage.

#### 3.2. Solution Algorithm

Generally, heuristic-based algorithms can be considered as a method for solving both constrained and unconstrained optimization problems that are based on natural selection, the process that drives biological evolution. It is frequently

used to find optimal or near-optimal solutions among many locally optimal solutions. The heuristic-based algorithm consists of maintaining a population of individuals, which represent potential solutions to the problem to be solved, that is, the optimization of a function, generally very complex. The heuristic-based algorithm repeatedly modifies a set of individual solutions. At each step, the algorithm selects individuals at random from the current population to be parents and uses them to produce new solutions for the next generation. Over successive generations, the population "evolves" toward an optimal solution. Based on these evaluations, a new population is formed using a mechanism of selection and applying operators such as crossover and mutation. Encoding, selection, recombination, mutation, and fitness evaluation are the main stages of the proposed algorithm. Problem codification and fitness evaluation as the most important stages of heuristic-based algorithm are discussed in detail in the following section.

### 3.3. Problem Codification

One of the most important parts of the heuristic-based algorithms is the problem codification, which matters more in solving complex problems. Each individual introduces a developed network that includes added lines, reactive power sources installed on demand buses and EEPs.

Codification is a very important issue when a heuristic-based algorithm is designed to dealing with a combinatorial problem. A proper codification may prevent complexity in the implementation of the solution algorithm. The individual is a solution proposal for the planning problem or better saying is the topology made up of all transmission lines, VAR sources and EEPs characteristics added to the system corresponding to their investment proposal. In the TEP&RPP associated with EEPs, the individual of the solution algorithm is represented by a group of vectors. The range of variations of each member for the part related to the transmission lines is determined according to the limitations given by Equation 26. The limitations given by Equation 42 and 43 specify the range of member for the components of reactive power sources and EEPs (the capacity of the virtual power plant) respectively. Each member of this vector can vary from zero to the maximum value of the corresponding variables. Thus, a simple codification is shown in Figure 3.

### 3.4. Fitness Evaluation

The fitness of an individual in a heuristic-based algorithm is the value of an objective function. For calculating fitness, the possible solution has to be first decoded and the objective function has to be evaluated. Finally, the algorithm must evaluate the fitness level of the new solutions in order to select the following candidates whose members will be recombined. It is worth mentioning that the fitness not only indicates how good the solution is but also corresponds to how close the set of solution is to the optimal one. The objective function provided in this article is to seek to achieve the following objectives:

1. Deviation from the limitation of constraints.
2. Cost of TEP.
3. Cost of RPP.
4. Investment in EEPs.

The objective function can be used in the following equation:

$$objective\ function = w_1(v_1) + w_2(v_2) + w_3(v_3) + w_4(d_v) + w_5(d_G) + w_6(d_S) \quad (47)$$

Where  $v_1$  is the cost of TEP,  $v_2$  is the Cost of RPP,  $v_3$  is the investment of EEPs,  $d_v$  is the sum of deviations from voltage limitations,  $d_G$  is the sum of deviations from power generation limitations and  $d_S$  is the sum of deviations from power flow limitation of branches.

Moreover,  $w_1$ - $w_6$  are the weight coefficients that can be chosen by the decision maker; these coefficients must be selected in such a way as to satisfy the following equation.

$$\sum_{i=1}^6 w_i = 1 \quad (48)$$

## 4. Illustrative tests

For the illustrative test, two systems are studied, namely a well known Garver system and the practical south Brazilian 46-bus system. The main objectives of the tests are to show the effectiveness of the presented multi-stage TEP&RPP



model along with EEPs in declining the investment costs and mitigating the greenhouse gas comparison with other planning models. In this study, the EEPs cost curve and EEPs marginal cost are derived from historical data of Iran Energy Efficiency Organization (IEEO) [9] as shown in Table 1. The historical data includes the cumulative energy saving (CES) and its corresponding cost. In this table, EEPs are divided into three levels such as low, medium, and high costs. The energy savings and marginal costs associated with each group of EEPs are ranked in the second and third column, respectively. The proposed algorithm is implemented in a programming-based language, AMPL [36], The AMPL code is run on a computer with Intel core™ i7 processor clocking at 2.5GHz RAM and with installed memory of 8.00GB.

#### 4.1. Garver system

To show the potential of EEPs in TEP problems, the model is investigated via a well-known example namely the Garver system that considers a small electricity system. This system has six buses and fifteen branch candidates, the total demand is 760 MW, 152 MVar and a maximum 5 lines can be added to each branch, where the Garver system data is given in [9]. Six different tests have been implemented; while three different cases have been used:

**Case 1.** TEP without reactive planning.

**Case 2.** TEP&RPP without considering EEPs.

**Case 3.** TEP&RPP with considering EEPs.

For each case two tests are managed: single-stage planning and multi-stage planning.

The assumptions of the problem are as follows:

The annual interest value  $I = 10\%$

The VAr-plant fixed costs  $c_0 = 10000\$$

The VAr-plant variable costs  $c_1 = 30\$/\text{kVAr}$

The shared saving model = 50% for ten years

The emission factor = 0.735 ton/MWh

The CER price is assumed to be 15\$.

##### *Test-1: Single-Stage TEP:*

In this test a single stage TEP has been implemented on the Garver system. The planning process resulted in a line investment of \$160 million and the following lines are added:  $n_{2-6}=2$ ,  $n_{3-5}=2$ ,  $n_{4-6}=2$ . Active power losses is 11.68 MW. Figure 4 shows the complete results of Test1. In Figure 4 the lines added to the base system are shown as dashed lines, the line loading rate is also expressed as a percentage, for example, the line loading between buses 2 and 3 is about 72.9%. As can be seen in the Figure 4, all constraints related to power flow such as bus voltage constraints, generator power limitations, and transmission line power are fully respected.

##### *Test-2: Single-Stage TEP&RPP:*

In this test a single-stage TEP and RPP has been implemented simultaneously on the Garver system. The planning process resulted in a line investment of \$130 million and the following lines are added:  $n_{2-6}=1$ ,  $n_{3-5}=2$ ,  $n_{4-6}=2$ . Active power losses is 12.77 MW and a total 45 MVar reactive power source must be installed at bus 2 and bus 5. Figure 5 shows the result of this test. In Figure 5, the lines added to the base system are shown as dashed lines, Compared to Test # 1, simultaneous problem solving for transmission line development and reactive resources has prevented the construction of a single line between buses 2 and 6, and the cost of developing the transmission network has been reduced by \$ 28.63 million. In this test, reactive power is provided locally at buses 2 and 5 thus the capacity of the transmission lines is released substantially.

##### *Test-3: Single-Stage TEP&RPP in the presence of EEPs:*

In this test, it is assumed that EEPs have been implemented in the Garver system .The planning process resulted in line investment of \$110 million and the following lines are added:  $n_{2-6}=1$ ,  $n_{3-5}=1$ ,  $n_{4-6}=2$ . Active power losses is

14.81MW. The capacity of reactive power compensators in buses 2 and 5 are 16 and 25 MVar, respectively. In this system, EEPs have been implemented in buses 2, 4 and 5, and these programs have reduced the consumption of each bus by 1.2, 1.6, and 1.8 percent, respectively. Figure 6 shows the complete results of the test. Compared with results of test 2, implementation of EEPs avoids building a line between buses 2 and 6 and also the cost of the transmission lines planning will be reduced by \$ 20 million. Table 2 summarizes the results of Tests 1 to 3. Columns 2-4 show the planning results of each test and columns 5-7 show the cost of each program, as can be seen from the results, the investment cost has been reduced by taking into account energy efficiency plans, and in addition the pollution caused by carbon dioxide gas has decreased by more than 180 million kg.

*Test-4: Mutli-Stage TEP:*

The test runs a multi-stage TEP on the Garver system. In this case, the three 5-year stages of  $P1$ ,  $P2$ , and  $P3$  are considered as the planning stages. Stage  $P1$  is the period from 2020 to 2025 where 2020 is considered as the base year for this stage. In the  $P2$  stage, 2025 is the base year with duration of 5 years from 2025 to 2030. The last planning stage is  $P3$ , starting from 2030 to 2035 with the year 2030. It should be noted that all investments should be discounted to the base year 2020. The following lines are added for the first stage  $P1$  (2020-2025):  $n_{2-6}=1$ ,  $n_{3-5}=2$ ,  $n_{4-6}=1$ , in the second stage  $P2$  (2025-2030) one branch must be installed between bus 4 and 6 and in the last stage  $P3$  (2030-2035) one line added in  $n_{2-6}=1$  route. In this case, the investment costs of lines is about M\$US128.4. However, in test 1, for a single stage planning model, the investment costs of lines was about M\$US160, which shows 20% higher costs. As multi-stage investment planning is carried out at different intervals, the final investment cost will be noticeably reduced by considering a 10% interest rate.

*Test-5: Mutli-Stage TEP&RPP:*

In this test, a mutli-stage with RPP is implemented on the Garver system. The planning horizons of this test are similar to Test 4. The following lines are added for the first stage  $P1$  (2020-2025):  $n_{2-6}=1$ ,  $n_{3-5}=2$ ,  $n_{4-6}=1$  and According to the simulation results, the system does not need reactive power sources at this stage, In the second time horizon  $P2$  (2025-2030), there is no need to add new transmission lines to the grid and only reactive power resources must be added to the network as following:  $Q_2=5$  MVar,  $Q_5=25$  MVar. In the last stage  $P3$  (2030-2035) one line must be added in  $n_{4-6}=1$  route. In this case, the investment costs of TEP&RPP is about M\$US110.9. However, in test 2, for a single stage planning model, the investment costs of planning was about M\$US130, which shows The cost of investment has decreased by M\$US 19.1 .

*Test-6: Mutli-Stage TEP&RPP in the presence of EEPs:*

In this test, a mutli-stage TEP with RPP is implemented on the Garver system. In this test, it is assumed that EEPs have been implemented in the Garver system .The planning horizons of this test are similar to that mentioned in Test 4. Table 3 shows the complete results of Test 6. In this case, the investment costs of TEP&RPP in the presence of EEPs is about M\$US99.63. However, in test 3, for a single stage planning model, the investment costs of planning was about M\$US127.42, which shows the cost of investment has decreased by M\$US 27.8.

*4.2. 46-Buses System (Southern Brazilian Network)*

Southern Brazilian 46-bus system is used to show the effectiveness of the proposed model in dealing with practical cases. The single mode diagram of 46-bus system can be found in [37]. The system consists of 46 buses, and 79 circuits, while the active and reactive demands for the entire planning horizon are 6880 MW and 1032 MVar [35], respectively. The maximum number of parallel transmission lines that can be added between two buses is limited to four. In this case, the four stages of  $P1$ ,  $P2$ ,  $P3$  and  $P4$  are considered. The period of Stage  $P1$  is from 2020 to 2025 where 2020 is considered as the base year. In the  $P2$  stage, 2025 is the base year with duration of 5 years from 2025 to 2030. The 3rd stage is  $P3$ , with duration of 2030 to 2035 where 2030 is considered as the base year. The last planning stage is  $P4$  with the duration from the year 2035 until 2040 and the base year is 2035. The annual interest rate value is set to 10%. The details of results derived through the implementation of TEP&RPP along with EEPs for

this system are given in Table 4. In Table 4, the first column outlines the planning time periods; the second column presents the results of the TEP and presents the lines added for Reinforcement the network. The results for RPP are shown in the third column of the table; this column shows the amount of reactive power installed in each bus. The percentages of participation in EEPs are outlined in the next column. The last column of Table 4 shows the CO<sub>2</sub> reduction at each stage of the planning, for example in the first stage *P1*, by implementing the proposed approach, results show that seven reactive sources should be installed at load buses with total 1627MVar capacity, and also one line in path 20-21 is added to the existing network, and also The following buses participate in energy efficiency programs; 5, 13, 20, 24, and 42. In this case, the investment costs of lines and reactive resources are about M\$US31.62 and M\$US12.81, respectively, and in addition the pollution caused by carbon dioxide gas has decreased by more than 1.288 million tons. Since it is a multistage planning solution, the lines and reactive resources are added in *P1* participated in the objective function with their true values whereas those added in *P2*, *P3* and *P4* are multiplied by their corresponding factors 0.59, 0.35 and 0.206, respectively. However, in [35], for a single stage planning model, the investment costs of lines and reactive sources were about M\$US47.48 and M\$US14.136, respectively, which shows 28% higher costs.

## 5. Conclusion

In this paper, a robust mixed-integer structure for multi-stage TEP&RPP problems is modelled to indicate the possibility of postponing the investment costs in planning problems. In the proposed methodology, an AC model for multi-stage planning is used to assess the loss of real and reactive powers properly. In addition, purchasing CERs and shared saving model are proposed as incentive-based support schemes to increase the penetration rate of the EEPs in the electricity system. Regarding incentive policies, investors are encouraged to invest in such resources. One of the major achievements through study is showing that solving TEP and RPP simultaneously in the presence of EEP provides better technical and economical solutions than the existing traditional planning models. The proposed multi-stage TEP&RPP algorithm is tested on a commonly used test system, the so-called Garver system, and a practical power system: 46-bus south Brazilian system. It has been concluded that by investing in EEPs, not only the total investment on transmission network expansion has been decreased but also a significant reduction in the emission has been achieved. It can be also deduced that simultaneous consideration of EEPs and multi-stage TEP&RPP problems has considerably declined the total TEP&RPP investment costs by preventing or postponing the construction of unnecessary lines. All in all, the results of various case studies, compared with the results presented in one of the most prominent sources in this field, indicate the effectiveness of the proposed methodology. On the other hand, the robustness of the performance of the proposed approach has been verified by solving a practical large-scale system.

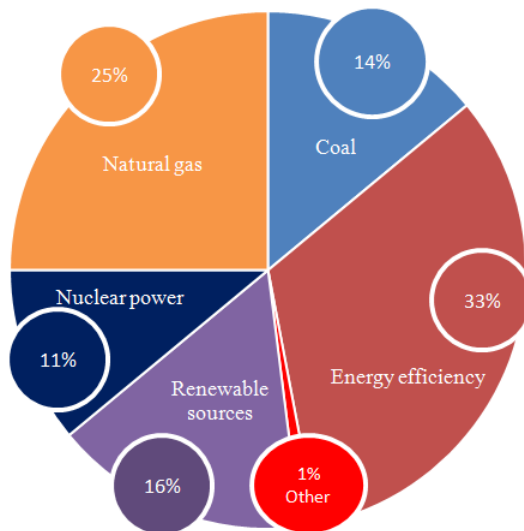
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- **Figure 1.** Share of US electricity generation by resource in 2030.
- **Figure 2.** Total investment curve of energy efficiency programs (EEPs).
- **Figure 3.** Simple codification
- **Figure 4.** Planning result of test 1
- **Figure 5.** Planning result of test 2
- **Figure 6.** Planning result of test 3
- **Table 1.** The marginal cost of energy efficiency programs (EEPs)
- **Table 2.** Results of single-stage planning - Garver system
- **Table 3.** Expansion results of test 6 - Garver system
- **Table 4.** Expansion results of 46 bus system



**Figure 2.**

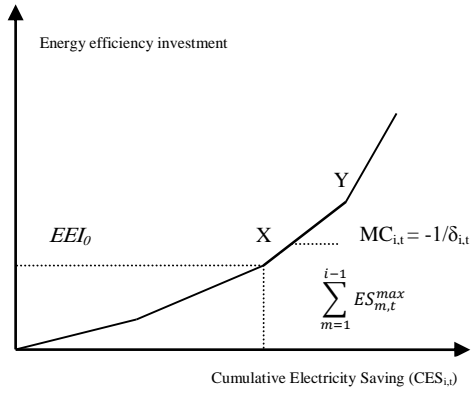


Figure 2.

	Set of solutions								
	Line Codification			VARs Codification			EEPs Codification		
	$n_{1,2}$	$n_{1,3}$	...	$Q_2$	$Q_3$	...	EEP <sub>1</sub>	EEP <sub>2</sub>	...
Stage 1	1	2	...	120	100	...	2%	4%	...
...	...	...	...	...	...	...	...	...	...
Stage $n$	0	1	...	52	15	...	3%	1%	...
Overall Planning	1	4	...	350	230	...	6%	7%	...

Figure 3.

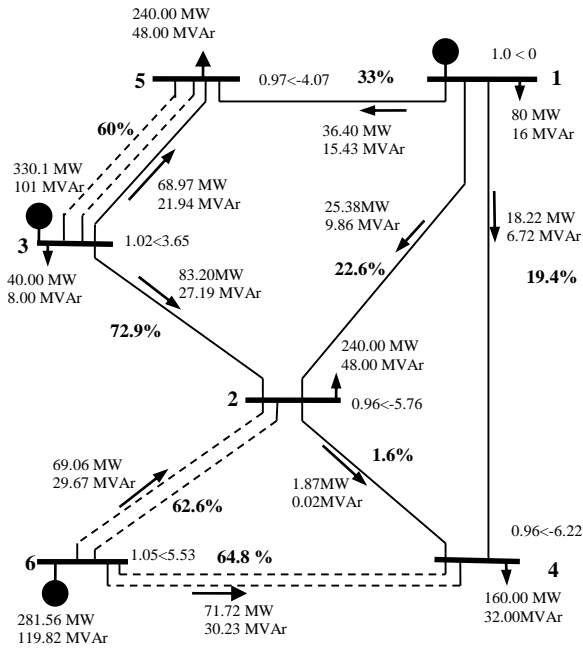


Figure 4.

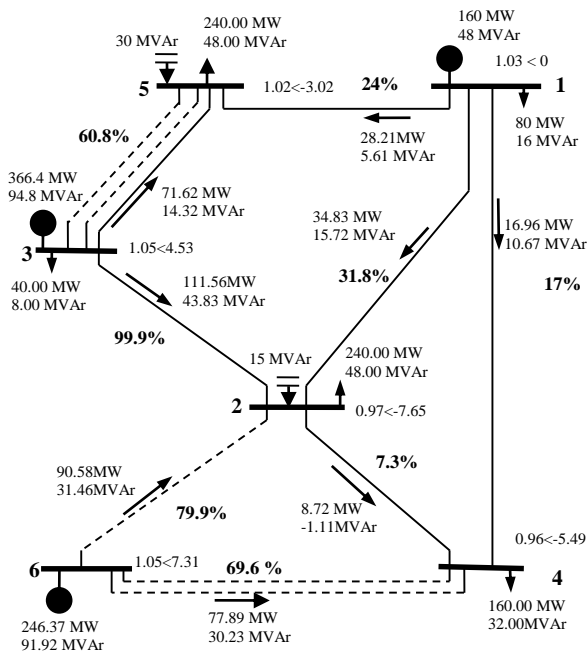


Figure 5.

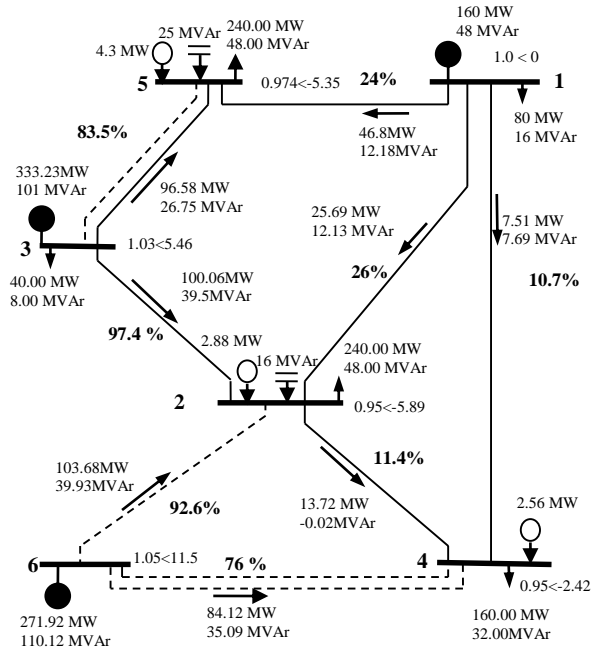


Figure 6.



**Table.1**

Classification	Cumulative energy saving (%)	The marginal cost of EEPs (\$/MWh)
Low cost EEPs	0.4	6
	0.6	7.7
	0.8	9.8
	1	12.6
	1.2	16.1
	1.4	20.6
Medium Cost EEPs	1.6	26.4
	1.8	30.7
	2	43.19
	2.2	55.2
High cost EEPs	2.4	70.7
	2.6	90.3
	2.8	115.5
	3.0	147.5

**Table 2.**

Tests	TEP Results	RPP Results (MVA <sub>r</sub> )	EEP Results	Line Investment (M\$)	VAR Investment (M\$)	EEP Investment (M\$)	Total Investment (M\$)	Co2 Emission Reduction (10 <sup>6</sup> kg)
Test 1: TEP	$n_{2-6}=2$ $n_{3-5}=2$ $n_{4-6}=2$	-	-	160	-	-	160	-
Test 2: TEP&RPP	$n_{2-6}=1$ $n_{3-5}=2$ $n_{4-6}=2$	$Q_2=15$ $Q_5=30$	-	130	1.37	-	131.37	-
Test 3: TEP&RPP EEP	$n_{2-6}=1$ $n_{3-5}=1$ $n_{4-6}=2$	$Q_2=16$ $Q_5=25$	EEP <sub>2</sub> =1.4% EEP <sub>4</sub> =1.6% EEP <sub>5</sub> =1.8%	110	1.25	16.17	127.42	180.5

**Table 3.**

The Stages of Planning	TEP Results	RPP Results (MVA <sub>r</sub> )	EEP Results (%)
<i>P1</i> (2020-2025)	$n_{3-5}=1$ $n_{4-6}=2$	---	EEP <sub>2</sub> =1.4 EEP <sub>4</sub> =1.6 EEP <sub>5</sub> =1.6
<i>P2</i> (2025-2030)	---	$Q_3=11$ $Q_5=15$	EEP <sub>2</sub> =1 EEP <sub>4</sub> =1.4 EEP <sub>5</sub> =1.8
<i>P3</i> (2030-2035)	$n_{2-6}=1$	$Q_3=15$ $Q_5=10$	EEP <sub>2</sub> =1.4 EEP <sub>4</sub> =1.2 EEP <sub>5</sub> =1.8

**Table 4.**

The Stages of Planning	TEP Results	RPP Results (MVA <sub>r</sub> )	EEP Results (%)	Co2 Emission Reduction (10 <sup>6</sup> kg)
<i>P1</i> (2020-2025)	$n_{20-21}=1$	$Q_2=59$ $Q_4=182$ $Q_5=138$ $Q_9=269$ $Q_{20}=458$ $Q_{21}=488$ $Q_{23}=133$	EEP <sub>5</sub> =1.0 EEP <sub>13</sub> =0.8 EEP <sub>20</sub> =1.8 EEP <sub>24</sub> =1.2 EEP <sub>42</sub> =0.6	1084.5
<i>P2</i> (2025-2030)	$n_{42-43}=1$	$Q_{40}=21$ $Q_{42}=155$ $Q_{43}=170$ $Q_{44}=50$ $Q_{45}=22$	EEP <sub>5</sub> =0.8 EEP <sub>13</sub> =0.6 EEP <sub>20</sub> =0.6 EEP <sub>24</sub> =1.6 EEP <sub>42</sub> =1.8	1288.7
<i>P3</i> (2030-2035)	$n_{9-14}=1$ $n_{5-11}=1$	$Q_5=90$ $Q_9=66$ $Q_{13}=60$ $Q_{18}=47$ $Q_{24}=16$ $Q_{33}=140$	EEP <sub>5</sub> =0.4 EEP <sub>13</sub> =0.6 EEP <sub>20</sub> =1.2 EEP <sub>24</sub> =1.6 EEP <sub>42</sub> =1.8	1443.3
<i>P4</i> (2035-2040)	$n_{13-18}=1$	$Q_5=146$ $Q_{13}=187$ $Q_{18}=320$ $Q_{20}=250$ $Q_{21}=130$ $Q_{23}=125$ $Q_{24}=30$ $Q_{33}=130$ $Q_{38}=40$	EEP <sub>5</sub> =0.6 EEP <sub>13</sub> =0.2 EEP <sub>20</sub> =0.4 EEP <sub>24</sub> =0.6 EEP <sub>42</sub> =1.0	699.9

## NOMENCLATURE

$V_0$	Transmission lines investment.	$V_G$	Vector of voltage at the generator buses.
$n$	New lines vector.	$I_G$	Vector Of Current at the generator buses.
$P_{Loss}$	Total real power loss.	$Q_G$	The size of new VAr plants.
$V$	Voltage magnitude of buses.	$Q_{Gd}$	The size of a VAr source installed at bus $d$ .
$\theta$	Voltage phase angle of buses.	$u_d$	Is a binary variable that indicates whether or not to install a reactive source at the bus $d$ .
$P_G$	Vector of active power generation.	$c_{0d}$	the reactive source Installation cost at the bus $d$ .
$P_D$	Vector of active power demand.	$c_{1d}$	Reactive source unit cost at the bus $d$ .
$Q_G^0$	Vector of reactive power of the existing generators.	$d$	Index of demand buses.
$Q_D$	Vector of reactive power demand.	$\underline{Q}_G$	The vector of VAr plants minimum limitation.
$\underline{P}_G$	Vector of lower bound of generators active power.	$\bar{Q}_G$	The vector of VAr plants maximum limitation.
$\bar{P}_G$	Vector of the upper bound of generators active power.	$\bar{Q}_G^0$	The vector of existing VAr plants minimum limitation.
$\underline{V}$	Minimum limit of buses voltage.	$\underline{Q}_G^0$	The vector of existing VAr plants maximum limitation.
$\bar{V}$	Maximum limit of buses voltage.	$u$	A binary vector that indicates whether or not to install reactive power sources at demand buses.
$S$	The vector of the (MVA) power flow.	$\delta_{mv}^T$	Present values factor of investment at stage $t$ .
$N$	Diagonal matrices containing vector $n$ .	$EEI_t$	The energy efficiency investment in year $t$ .
$N^0$	Diagonal matrices containing the existing lines.	$E_t$	The electricity consumption in year $t$ .
$S^{from}$	Vector of (MVA) power flow vector "from" bus.	$EEI_{0i}$	The initial energy efficiency investment from the $i$ -th program.
$S^{to}$	Vector of (MVA) power flow vector "to" bus.	$ES_{i,t}^{\max}$	The maximum limit of energy saving from the $i$ -th program in year $t$ .
$\bar{S}$	Vector of maximum (MVA) power flow.	$CES_{i,t}$	Cumulative energy saving from the $i$ -th program in year $t$ .
$\bar{n}$	Vector of the maximum number of candidate lines.	$\delta_{i,t}$	Energy efficiency investment elasticity.
$g_{ij}$	The conductance of the lines between buses $i$ and $j$ .	$MC_{i,t}$	Marginal cost of the $i$ -th program in year $t$ .
$\theta_{ij}$	The difference in phase angle between buses $i$ and $j$ .	$CER$	Certified emission reductions price.
$\Omega_d$	Set of demand buses.	$EMF_{CO_2}$	CO <sub>2</sub> emission reduction.
$N_B$	Number of all buses	$f^{CER}$	The function of Purchasing certified emission reductions from EEPs.
$b_{ij}$	Susceptance of the lines between buses $i$ and $j$	$SSC$	The sharing coefficient
$b_{ij}^{sh}$	Shunt susceptance of the lines between buses $i$ and $j$ .	$P^{EEP}$	The amount of power that the EEPs can reduce in a given period.

$b_i^{sh}$	Shunt susceptance at the bus $i$ .	$EEP_1$	The percentage of power that the EEPs can reduce at the bus $i$ .
$f^{CER}$	The function of Purchasing certified emission reductions from EEPs.		

## Biographies

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