Design and analysis of solar photovoltaic-fed Z-source inverter-based dynamic voltage restorer

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Dynamic voltage restorer; Perturb \& observe; Maximum power point tracking.

Abstract. Z-Source Inverter (ZSI) is a new topology of power converter, especially a DC-AC converter, at a very interesting power level. For instance, it only uses a single-stage power converter with a buck-boost characteristic. This work introduced a combination of a solar system and a ZSI-based dynamic voltage restorer to reduce the voltage swell and harmonics under sudden addition of an unbalanced three-phase nonlinear load. This paper focused on Perturb and Observe (P\&O) algorithm to automatically determine the operating voltage of PV systems that would produce maximum power output. The proposed ZSI-based dynamic voltage restorer was designed and modeled by using MATLAB/SIMULINK. The outcomes were compared with those of conventional dynamic voltage restorers equipped with voltage and current source inverters.

1. Introduction

Presently, in addition to quality problems, electric power systems face voltage waveforms including swells and sags as major constraints [1,2]. The performance of power systems can be enhanced by incorporating some controllable custom power devices such as dynamic voltage restorers equipped with voltage source, current source, and Z-Source Inverters (ZSI) [3–5]. The disadvantages of conventional dynamic voltage restorer with voltage and current source inverters were enumerated in [6–8]. ZSI can be used to enhance the boost operation for the inverter AC output voltage and therefore, inverters can operate in the shoot-through mode [9]. Unlike conventional inverters such as voltage and current sources, the short-circuit mode is not destructive and has been truly used in the ZSI [5]. Solar energy is one of the most reliable sources of renewable energy power generation [10]. Energy from sunlight is converted through the power conversion process so that the generated power can be transferred to an existing electrical network. The circuit of conventional PV power converters requires two-stage converters: first, it steps up the solar voltage and then, changes direct current input back into alternator current before it can be fed into the existing electrical grid [11,12]. However, a ZSI uses a single-stage power converter with buck-boost characteristic [13]. Since ZSI is a new inverter type, it has received much academic spotlight. However, these techniques could not function well if the Perturb and Observe (P\&O) algorithm has not been modified in advance to obtain greater voltage and current from the solar system and maintain the voltage at the DC-link of the inverter input [14–16]. This work introduces a combination of a solar system and

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a dynamic voltage restorer with ZSI for ameliorating distorted voltage and current waveforms in the process of switching a three-phase balanced nonlinear load. In this paper, the Maximum Power Point Tracking (MPPT) method such as P&O is applied to acquiring optimum power from the solar system. The proposed dynamic voltage restorer equipped with ZSI is validated in MATLAB/SIMULINK software and obtained outcomes are compared with the classical dynamic voltage restorer with voltage and current source inverters.

2. Dynamic voltage restorer with ZSI

Figure 1 shows the proposed Dynamic Voltage Restorer with a ZSI. The proposed system consists of a three-phase ZSI, interfacing inductance \( L_f \), a unit vector control technique, a DC source, and a solar photovoltaic system. A solar system is used to give DC supply to the DVR-based ZSI. The DVR with Z-source converts this DC supply to AC and ameliorates the voltage-related issues including voltage sags/swells in a distribution system under sudden switching of balanced three-phase nonlinear load.

3. Working principle of ZSI [6,8]

The working principle of ZSI can be explained in three different states such as active, zero, and shoot-through states, as highlighted in Figure 2(a)-(c). A detailed explanation of various working states of ZSI was given in [6-8]. The active state is additionally known as a non-shoot-through state, as given in Figure 2(c). In the shoot-through state, ZSI is working in one of the forty-one distinctive modes as shown in Figures 2(b) and 3 and Insulated-Gate Bipolar Transistor (IGBT) switches are short-circuited.

Let the impedance network elements have similar values \( L_1 = L_2 = L \) and \( C_1 = C_1 = C \). Therefore, the Z-network inductor and capacitor voltage can be obtained using Eq. (1) [6,8]:

\[
\begin{align*}
 v_{l1} &= v_{l2} = v_l \\
 v_{c1} &= v_{c2} = v_c 
\end{align*}
\]  

(1)

where \( v_c \) is the capacitor voltage and \( v_l \) is the inductor voltage of the ZSI. In the Shoot-Through (ST) state, \( t_0 \) is the time period and the relation between \( v_c \) and \( v_l \) is obtained through Eq. (2) [6,8]:

\[
\begin{align*}
 v_l &= v_c \\
 v_{dis} &= 2v_c \\
 v_{in} &= 0 \quad \text{(ST state)}
\end{align*}
\]  

(2)

where \( v_{in} \) and \( v_{dis} \) are the dc-link input voltage of the inverter and diode voltage. In active and zero states, the relation between \( v_c \) and \( v_l \) is obtained using Eq. (3) and \( t_1 \) is the time interval:

\[
\begin{align*}
 v_l &\neq v_c \\
 v_{dis} &= v_{pv} = v_l + v_c \\
 v_l &= v_{pv} - v_c = v_c - v_{in} \\
 v_{in} &= v_c - v_l = 2v_c - v_{pv}
\end{align*}
\]  

(3)

where \( v_{pv} \) is the output voltage of PV system. The

![Figure 1. Combination of dynamic voltage restorers with Z-source inverters.](image-url)
mean voltage of the Z-network inductor \( (v_{\text{mean}}) \) at
time \( t \) is expressed in Eq. (4) [6,8]:

\[
v_{\text{mean}} = v_c + (v_{pr} - v_c) \cdot t_1 = 0,
\]

\[
v_c = v_{pr} \left( \frac{t_1}{t_1 - t_0} \right).
\]  

The mean input dc-link of the inverter is obtained through Eq. (5) \( (v_{in}) \):

\[
v_{in} = t_0 \ast 0 + t_1 \cdot (2v_c - v_{pr}) \quad \text{using Eq. (4)},
\]

\[
v_{in} = \left( \frac{t_1}{t_1 - t_0} \right) v_{pr} = v_c.
\]  

The input dc-link voltage of the inverter in active and zero states is expressed through Eq. (6):

\[
v_{in}^\wedge = (v_c - v_l) = v_c - (v_{pr} - v_c),
\]

\[
v_{in}^\wedge = (2v_c - v_{pr}).
\]  

By comparing Eqs. (4) and (6), Eq. (7) is obtained:

\[
v_{in}^\wedge = \left( \frac{t}{t_1 - t_0} \right) v_{pr},
\]

\[
v_{in}^\wedge = b v_{pr},
\]

where ‘b’ denotes the boost factor and is also obtained through Eq. (8):

\[
b = \left( \frac{t}{t_1 - t_0} \right) = \frac{1}{1 - \left( \frac{t_1}{t} \right)} \geq 1, \quad t = t_0 + t_1.
\]

The converter output voltage can be calculated using Eq. (9) [6,8]:

\[
v_{ac} = \frac{m v_{in}^\wedge}{2} = \left( \frac{m b v_{pr}}{2} \right),
\]

where \( m \) is the modulation index whose value should be less than or equal to one. The Z-network capacitor voltage can be obtained through Eqs. (10) and (11) [6,8]. From Eq. (4), we obtain the following:

\[
v_c = \left( \frac{t_1}{t_1 - t_0} \right) v_{pr},
\]

\[
v_c = \left( \frac{t_1}{t} \right) \left( \frac{t}{t_1 - t_0} \right) v_{pr},
\]

\[
v_c = \left( \frac{1 - \left( \frac{t_0}{t} \right)}{1 - \left( \frac{t_0}{t_1} \right)} \right) v_{pr},
\]

\[
v_c = \frac{b + 1}{b} v_{pr} = \left( \frac{b + 1}{2} \right) v_{pr}.
\]

4. Impedance source inverter design

4.1. Z-network inductor design

In active and zero modes, a mean current passing through the inductor is reduced, as expressed in Eq. (12) [6,8]:

\[
i_{\text{mean}} = \left( \frac{p_{in}}{v_{pr}} \right),
\]

For designing ZSI parameters such as inductor and capacitor, the 30% current ripples are taken.

The maximum current flowing through the inductor [6,8] is:

\[
i_{\text{max}} = i_{\text{mean}} + 30\% \text{ of } i_{\text{mean}}.
\]
The minimum current flowing through the inductor [6,8] is given below:

\[ i_{\text{min}} = i_{\text{min,max}} - 30\% \text{ of } i_{\text{max,max}}. \]

In ST state, \( v_t = v_c = v \), \( v_t = v_c = v = \left( \frac{b+1}{2} \right) v_{pu} \), use the value of \( v_c \) from Eq. (11).

The value of inductor is determined through Eq. (13):

\[ L = \left( \frac{v \times f_0}{\Delta i} \right), \]

where \( \Delta i = (i_{\text{max}} - i_{\text{min}}) \).
4.2. Z-source capacitor design
The capacitor value is obtained through Eq. (14) [6,8]:

\[ C = \left( \frac{i_{\text{avg}} \cdot t_0}{\Delta v_c} \right), \quad \Delta v_c = v \cdot 3\% . \]  \hspace{1cm} (14)

In the ST state, the value of inductor and capacitor can be calculated by Eqs. (11) and (14) [6,8]:

\[ L = \left( \frac{v \cdot t_0}{\Delta i} \right) = \left( \frac{167.75 \cdot 9.83}{2.57} \right) = 0.6 \text{ mH}, \]

\[ C = \left( \frac{i_{\text{mean}} \cdot t_0}{\Delta v_c} \right) = \left( \frac{4.28 \cdot 9.83}{844.20} \right) = 0.05 \mu\text{F}. \]

4.3. Voltage gain
The voltage gain can be expressed in Eq. (15) [8]:

\[ G = m \cdot b = \left( \frac{n}{m} \right) \sqrt{3m} - 1. \]  \hspace{1cm} (15)

\[ G = \left[ \frac{1}{2} D (1 - D) \right]_0^D D - D (1 - D) - 1. \]  \hspace{1cm} (15)

4.4. Switching losses [8]
The switching loss of each IGBT in active and ST states \( P_{SW-act} \) and \( P_{SW-st} \) is calculated through Eqs. (16) and (17).

\[ P_{SW-st} = \frac{1}{2} \frac{T_{SW}}{2} (E_{SW-act} + E_{SW-off}) \]

\[ P_{SW-act} = \frac{1}{2} T_{SW} (E_{SW-act} + E_{SW-off}). \]  \hspace{1cm} (17)

\( E_{SW-act} \) and \( E_{SW-off} \) are the switch-on and switch-off energy losses of the IGBT at peak current, respectively. \( E_{SW-act} \) and \( E_{SW-off} \) are the switch-on and switch-off energy losses corresponding to the mean turn on current of the shoot-through states, which is \( \frac{2}{3} I_L \).

4.5. Voltage stress across the devices [8]
According to Eq. (7), the voltage stress, \( S_S \), can be expressed in Eq. (18):

\[ S_S = v_{in} = b v_{pe}. \]  \hspace{1cm} (18)

5. Modulation algorithm with timing diagram of the ZSI

Figure 3 outlines the structure of the eighty-three IGBT switching modes of the proposed ZSI including forty active modes, two zero modes, and forty-one ST modes. In active and zero modes, two IGBT switches with one, two, three, five, or six modes complement each other, similar to the commonly used traditional inverters and the proposed ZSI. However, forty-one ST modes with one (E1 to E6), two (E7 to E21), three (E22 to E31), four (E32 to E37), five (E38 to E40), or six legs (E41) are short circuited which are specific to ZSI. The switching states for the DVR with ZSI are shown in Table 1.

6. Unit Vector Template (UVT) control technique [17]

In UVT technique, first, three-phase supply voltages are measured and multiplied by \( g = \frac{1}{V_{mag}} \), as shown in Figure 4, where \( V_{mag} \) is the input voltage obtained through Eq. (19) [17].
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<th>State (00000)</th>
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Table 1. Switching states of the proposed DVR with Z-Source Inverter (ZSI) ((SWY is the complement of SWY, where Y = 1, 3, 5, 7, 9, or 11)).

Shoot-through E1 (0V) 1 1 SW3 !SW3 !SW5 SW5 !SW5 SW7 !SW7 SW9 !SW9 SW9 SW11 !SW11
Shoot-through E2 (0V) SW1 !SW1 1 1 S5 !S5 S7 !S7 S9 !S9 S11 !S11
Shoot-through E3 (0V) SW1 !SW1 SW3 !SW3 1 1 SW7 !SW7 SW9 !SW9 SW9 SW11 !SW11
Shoot-through E4 (0V) SW1 !SW1 SW3 !SW3 SW5 !SW5 1 1 SW9 !SW9 SW9 SW11 !SW11
Shoot-through E5 (0V) SW1 !SW1 SW3 !SW3 SW5 !SW5 SW7 !SW7 1 1 SW9 !SW9 SW9 SW11 !SW11
Shoot-through E6 (0V) SW1 !SW1 SW3 !SW3 SW5 !SW5 SW7 !SW7 SW9 !SW9 1 1
Shoot-through E7 (0V) 1 1 1 1 SW5 !SW5 SW7 !SW7 SW9 !SW9 SW9 SW11 !SW11
Shoot-through E8 (0V) 1 1 SW3 !SW3 1 1 SW7 !SW7 SW9 !SW9 SW9 SW11 !SW11
Table 1. Switching states of the proposed DVR with Z-Source Inverter (ZSI) ([SYW] is the complement of SWY, where Y = 1, 3, 5, 7, 9, or 11) (continued).

<table>
<thead>
<tr>
<th>Shoot-through E9 (OV)</th>
<th>1</th>
<th>1</th>
<th>SW3</th>
<th>!SW3</th>
<th>SW5</th>
<th>!SW5</th>
<th>1</th>
<th>1</th>
<th>SW9</th>
<th>!SW9</th>
<th>SW11</th>
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<td>SW3</td>
<td>!SW3</td>
<td>SW5</td>
<td>!SW5</td>
<td>SW7</td>
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<td>SW3</td>
<td>!SW3</td>
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<td>Shoot-through E19 (OV)</td>
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<td>Shoot-through E20 (OV)</td>
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<td>SW5</td>
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<td>!SW11</td>
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<tr>
<td>Shoot-through E41 (OV)</td>
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</tr>
</tbody>
</table>

\[ V_{mag} = \sqrt{\frac{2}{3}}(V_{sa}^2 + V_{sb}^2 + V_{sc}^2). \]  

(19)

The voltage signals are given as an input into a Phase-Locked Loop (PLL). After receiving input signals, the PLL used to create unit vectors \( U_a, U_b, \) and \( U_c \) is calculated using Eq. (20) [17]:

\[
\begin{align*}
U_a &= \sin (\theta) \\
U_b &= \sin (\theta - 120) \\
U_c &= \sin (\theta + 120)
\end{align*}
\]  

(20)

\[ V_{Ld}, V_{Lb}, \text{ and } V_{Lc} \text{ are obtained by Eq. (21) [17]:} \]

\[
\begin{bmatrix}
V_{La}^* \\
V_{Lb}^* \\
V_{Lc}^*
\end{bmatrix} = [\varphi] \begin{bmatrix}
U_a \\
U_b \\
U_c
\end{bmatrix}.
\]  

(21)

The three-phase supply voltages are compared with \( V_{La}^*, V_{Lb}^*, \text{ and } V_{Lc}^* \) and the reference compensator voltage \( V_{Cabc}^* \) is generated. The Pulse Width Modulation (PWM) generator produces switching pulses after
comparing the reference compensator voltages and used compensator voltages.

7. Perturb and Observe (P&O) algorithm [18–20]

The P&O technique is commonly known for hunting down the MPPT because it is straightforward and requires only an estimation of the voltage ($v_{pp}$) and current ($i_{pp}$) of the PV system [21]. P&O works by perturbing (increasing or decreasing) the measured photovoltaic voltage ($v_{pp}$) and comparing the instantaneous powers before and after perturbation [18–21]. The P&O algorithm is given in Figure 5.

8. Results and discussion

The proposed dynamic voltage restorer-based ZSI system in Figure 1 is modulated using MATLAB/SIMULINK under sudden switching of a balanced three-phase nonlinear load. Figure 6(a)-(c) shows different characteristics of the solar cell under sun irradiations. As the irradiation increases, the open-circuit voltage and the short-circuit current increase, as shown in Figure 6(a) and (b). Consequently, the P&O algorithm is used to obtain the highest amount of power from solar cells, as highlighted in Figure 7. The simulation specifications are shown in Table 2.

8.1. Swell alleviation by dynamic voltage restorer with voltage source inverter

A 31% three-phase balanced voltage swell occurs on the supply side because of sudden switching of nonlinear load, as shown in Figure 8(a) and (b). At $t = 0.05$ to 0.15, a voltage source inverter-based DVR is connected to a distribution system and a compensated voltage is injected to compensate the three-phase balanced voltage swell, as shown in Figure 8(c). Figure 8(d) highlights the sinusoidal load voltage after minimizing the voltage swell effect. Figure 8(e) outlines the nature of the capacitor voltage of the dynamic voltage restorer equipped with source inverter.

8.2. Swell alleviation by dynamic voltage restorer with current source inverter

Figure 9(a) and (b) show the voltage swell with a magnitude of 31% under sudden switching of three-phase balanced nonlinear load. It begins at $t = 0.05$ s and terminates at $t = 0.15$ s. Figure 9(c) depicts the ability of dynamic voltage restorer with a current source inverter to ameliorate the three-phase balanced

![Figure 5. Perturb and observe algorithm.](image-url)
voltage swell by injecting the compensated voltage. Figure 9(d) highlights the sinusoidal load voltage after minimizing the voltage swell effect. Figure 9(e) shows the behavior of inductor current of the dynamic voltage restorer with a current source inverter under voltage swell.

8.3. Swell alleviation by dynamic voltage restorer with a ZSI

Figure 10(a) and (b) show the voltage swell with a magnitude of 31% under sudden switching of three-phase balanced nonlinear load in a distribution network. It begins at $t = 50$ milliseconds and terminates at $t = 150$ milliseconds. Figure 10(c) depicts the ability of the dynamic voltage restorer with a ZSI to alleviate voltage swell by injecting the compensated voltage. Figure 10(d) highlights the sinusoidal load voltage after minimizing the voltage swell effect. Figure 10(e)–(f) outlines the nature of capacitor voltage and inductor current of the proposed dynamic voltage restorer based on ZSI.

9. Comparison of dynamic voltage restorers with voltage, current, and ZSI

Figure 11 outlines the comparison in compensated voltages of conventional dynamic voltage restorers with voltage, current, and proposed ZSI. Regardless of what inverters have been used, voltage swell with a magnitude of 31% (98 V) at $t = 0.5$ s for a duration of 0.35 s is observed. Therefore, the dynamic voltage restorers with inverters are associated with the system and they generate voltages of 132 V, 66.65 V, and 95 V.
Table 2. DVR with Z-Source Inverter (ZSI) Specifications.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supply voltage (Vs)</td>
<td>380 V</td>
</tr>
<tr>
<td>Frequency (f)</td>
<td>50 Hz</td>
</tr>
<tr>
<td>Supply resistance (Rs)</td>
<td>0.05 Ω</td>
</tr>
<tr>
<td>Supply inductance (Ls)</td>
<td>3.5 μH</td>
</tr>
<tr>
<td>Linear load</td>
<td>Inductive reactive power (QL) = 10 kVAR</td>
</tr>
<tr>
<td>Nonlinear load</td>
<td>Diode rectifier, Rd = 10 Ω, Ld = 3 μH</td>
</tr>
<tr>
<td>Injection transformer</td>
<td>240/120 V</td>
</tr>
<tr>
<td>DC-bus voltage (Vdc)</td>
<td>150 V</td>
</tr>
</tbody>
</table>

\[ V_{OC} = 36.1 \text{ V} \]
\[ I_{SC} = 6 \text{ A} \]

Number of solar cells \((C) = 36 \)

\[ P_{\text{max}} = 151 \text{ W} \]
\[ V_{MPP} = 29.6 \text{ V} \]

Solar module

\[ I_{MPP} = 5.1 \text{ A} \]

Diode identity factor \((n) = 1 \)

\[ R_s = 0.18 \text{ Ω} \]
\[ R_p = 360.002 \text{ Ω} \]
\[ L_1 = L_2 = L = 0.6 \text{ mH} \]
\[ C_1 = C_2 = C = 0.05 \text{ μF} \]
\[ m = 0.5 \]
\[ i_0 = 9.83 \mu\text{s} \]
\[ i_{\text{avg}} = 4.28 \text{ A} \]
\[ i_{\text{max}} = 5.56 \text{ A} \]
\[ i_{\text{min}} = 2.99 \text{ A} \]
\[ \Delta i = 2.57 \text{ A} \]

Table 3. Comparison of supply current THD_i values.

<table>
<thead>
<tr>
<th>Before compensation</th>
<th>DVR with VSI (%)</th>
<th>DVR with CSI (%)</th>
<th>Proposed DVR with ZSI (%)</th>
<th>Enhancement in THD_i (%)</th>
<th>Enhancement in THD_i (%)</th>
<th>Enhancement in THD_i (%)</th>
</tr>
</thead>
<tbody>
<tr>
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<tr>
<td>7.97</td>
<td>0.65</td>
<td>91.8</td>
<td>0.75</td>
<td>90.58</td>
<td>0.5</td>
<td>93.72</td>
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</table>

V, respectively. The proposed dynamic voltage restorer with ZSI is characterized by better implementation than those with voltage and current source inverters, as highlighted in Figure 11.

Tables 3 and 4 show the capability of voltage, current, and proposed dynamic voltage restorers with ZSIs to eliminate current and voltage harmonics.

Total Harmonic Distortion (THD) of supply current without dynamic voltage restorers with voltage, current, and ZSIs connected to the system is measured as 7.97%; however, when they are connected to the system, the THD_i values will be 0.65%, 0.75%, and 0.6%, as shown in Table 3. Therefore, a 93.72% decrease in THD_i has been accomplished by the proposed dynamic voltage restorer with ZSI, compared with 91.8% and 90.58% decreases in THD_i of voltage and current source inverters.

In Table 4, load voltage THD_v is 18.62% when the
dynamic voltage restorers with voltage, current, and proposed ZSBs are not connected to the system. In contrast, when they are connected, the THDv values will be 3.5%, 2.48%, and 1.8%, as shown in Table 4. Therefore, a 90.33% decrease in THDv has been accomplished by the proposed dynamic voltage restorer with ZSI, compared with 81.2% and 86.68% decreases in THDv of voltage and current source inverters.

10. Conclusion
This work introduced a combination of a solar system
and a dynamic voltage restorer with Z-source inverter for ameliorating voltage swell and harmonics under sudden addition of balanced three-phase nonlinear load. Results showed that in the swell condition, the proposed restorer could reduce possible voltage variations by injecting an exact magnitude of compensated voltage as compared to the conventional dynamic voltage restorers with voltage and current source inverters.

Furthermore, results demonstrated the ability of the proposed restorer to eliminate current and voltage harmonics in the process of switching three-phase balanced nonlinear load, compared to the conventional dynamic voltage restorers with voltage and current source inverters. This study focused on Perturb and Observe (P&O) algorithm to automatically find the operating voltage of PV systems producing maximum power output.

**References**


Biographies

Miska Prasad was born in India and received BE in Electrical & Electronics Engineering from GITAM University, Andhra Pradesh, India, and M.Tech in Power Systems from NIT Jamshedpur, Jharkhand, India in 2010 and 2013, respectively. Currently, he is pursuing PhD degree at Electrical Engineering Department, NIT Jamshedpur, India. His main research interests are power quality, custom power devices, and power electronics.

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Almoataz Y. Abdelaziz received the BSc and MSc degrees in Electrical Engineering from Ain Shams University, Cairo, Egypt in 1985 and 1990, respectively and PhD degree in Electrical Engineering according to the channel system between Ain Shams University, Egypt, and Brunel University, U.K., in 1996. He is currently a Professor of Electrical Power Engineering at Ain Shams University. Dr. Abdelaziz is the Chair of IEEE Education Society chapter in Egypt, a senior editor of Ain Shams Engineering Journal, an editor of Electric Power Components & Systems Journal, a member of editorial board, and a reviewer of technical papers in several international journals and conferences. He is a senior member in IEEE, a member in IET, and a part of Egyptian Sub-Committees of IEC and CIGRE. He has been awarded many prizes for distinct research and for international publishing from Ain Shams University, Egypt. He has authored or coauthored more than 300 refereed journal and conference papers in his research areas, which include the applications of artificial intelligence as well as evolutionary and heuristic optimization techniques to power system operation, planning, and control.