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Sustainability assessment of supply chains by inverse network dynamic data envelopment analysis

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KEYWORDS Sustainable Supply Chain Management (SSCM); Data Envelopment Analysis (DEA); Range Adjusted Measure (RAM); Inverse data envelopment analysis; Network DEA; Dynamic DEA. **Abstract.** This paper focuses on assessing sustainability of supply chains. This paper, at first, proposes network dynamic Range Adjusted Measure (RAM) model. Then, an inverse version of network dynamic RAM model is proposed. The proposed inverse network dynamic Data Envelopment Analysis (DEA) model changes both inputs and outputs of Decision-Making Units (DMUs) so that existing efficiency scores of DMUs remain unchanged. We change inputs and outputs without any modification in efficiency score of DMU under evaluation, while inputs and outputs may have a large range. A case study shows the efficacy of the proposed model.

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1. Introduction

Nowadays, our earth encounters a number of difficulties such as air pollution, little or lack of water resources, energy inefficiency, destruction of forests, etc. For this reason, supply chains should be responsible for environmental issues. Mentzer et al. [1] defined Supply Chain Management (SCM) as "the systemic, strategic coordination of traditional business functions and the tactics across these business functions within a particular company and across businesses within the supply chain, for the purposes of improving the longterm performance of the individual companies and the supply chain as a whole". Drumwright [2] and Murphy et al. [3] introduced Sustainable Supply Chain Management (SSCM). Carter and Rogers [4] defined SSCM as "the strategic, transparent integration and achievement of an organization's social, environmental, and economic goals in the systemic coordination of key inter-organizational business processes for improving the long-term economic performance of the individual company and its supply chains". At the moment, sustainability considerations are not just a symbolic action; however, they are reactive to pressures of Non-Governmental Organizations (NGOs), media, and green political parties [5]. Many firms have established tough evaluations for suppliers in their supply chain to ensure that the sustainability considerations are addressed seriously [6-8].

Charnes et al. [9] proposed Data Envelopment Analysis (DEA). DEA is a proper tool for assessing relative efficiency of supply chains [10]. In classical DEA models, Decision-Making Units (DMUs) are considered as a black box. Lewis and Sexton [11] proposed a network DEA model to deal with divisions in each DMU. In addition, most of other traditional DEA models measure efficiency score just in a specific

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period. For the first time, Färe and Grosskopf [12] proposed dynamic DEA model. Tone and Tsutsui [13] considered the network DEA model dynamically and, then, proposed a network dynamic DEA model based on Slacks-Based Measure (SBM) approach. They named efficiencies of each period and each division as "term" and "divisional" efficiencies, respectively.

This paper proposes input-oriented Range Adjusted Measure (RAM) model and clarifies the reason for using this model. Then, an inverse model of network dynamic input/output-oriented RAM is proposed. To the best of our knowledge, the inverse RAM model with network and dynamic structure has not been proposed so far. This paper has the following contributions: the following topics are proposed in this paper for the first time:

- Input/output-oriented RAM model with dynamic and network structure is developed;
- The inverse model of dynamic-network input/ output-oriented RAM model is developed;
- Both inputs and outputs of Decision-Making Units (DMUs) can be changed in our inverse DEA model;
- The proposed model is applied to the assessment of the sustainability of supply chains;
- To demonstrate the applicability of our model, a case study is given.

The main objective of this paper is to develop network-dynamic input-oriented RAM model and its inverse for assessing sustainability of supply chains.

The structure of this paper is organized as follows. Literature review is presented in Section 2. The proposed models are given in Section 3. A case study is given in Section 4. Managerial implications and conclusions are explained in Sections 5 and 6, respectively.

2. Literature review

2.1. Sustainable SCM

As mentioned earlier, environmental and social responsibilities in SCM started to receive attention in 1994 and continued through researches such as greening supply chain [14], greening product [15,16], and greening supply chain from product design to end user [17,18].

Liu et al. [19] focused on eco-friendly competition between substitutable products and retail stores. They found that eco-friendly manufacturers earned more profits because of customers' environmental awareness. Zhang et al. [20] studied impact of customers' environmental awareness on companies. Ghosh and Shah [21] discussed greening costs and impact of greening sensitivity of customers on profit. Xie [22] studied the role of policy-makers in energy saving.

Assessing sustainability of supply chains is an important topic. Genovese et al. [23] proposed an environmentally extended Multi-Regional Input-Output (MRIO) hybrid model and Life Cycle Assessment (LCA) that can be used for emissions assessment of supply chains. They evaluated supply chains based Su et al. [24] addressed improving on emissions. sustainability of supply chain management in situations with incomplete information. They proposed a hierarchical grey-DEMATEL approach. Dubey et al. [25] focused on dynamic nature of SSCM. They addressed both quantitative and qualitative approaches. Kumar et al. [26] assessed suppliers based on SSCM criteria. They applied fuzzy multi-criteria decisionmaking model. Azadi et al. [27] developed a fuzzy model for assessing sustainability of suppliers in terms of economic, environmental, and social factors. Li and Cui [28] proposed network range adjusted measure model to evaluate sustainability of supply chains. Table 1 summarizes previous researches on sustainable SCM criteria and used techniques.

This paper proposes inverse network dynamic input-oriented RAM model to assess sustainability of supply chains as well as given economic, environmental, and social criteria.

2.2. Data Envelopment Analysis (DEA) 2.2.1. Inverse DEA

Wei et al. [37], for the first time, proposed inverse DEA model. The main purpose of the inverse DEA model is to analyze sensitivity of a DEA model to changes in inputs/outputs of DMU_o (DMU under evaluation) without any change in DMU_o efficiency score. In other words, after changes in inputs/outputs, Production Possibility Set (PPS) changes; however, efficient frontier should not be changed dramatically [38].

Yan et al. [38] introduced an inverse DEA model for resource planning, given decision-makers' preferences. Jahanshahloo et al. [39] developed the inverse model of Yan et al. [38] and presented inverse DEA model to estimate outputs, given changes in inputs. Jahanshahloo et al. [40] developed an inverse DEA model to estimate inputs, given outputs increase and improvements in efficiency score. Furthermore, they estimated maximum reduction in inputs without changing efficiency scores. Jahanshahloo et al. [41] ran a sensitivity analysis by inverse DEA model. They determined upper and lower bounds for inputs and outputs by two multi-objective linear programming problems and converted multi-objective linear programme to a linear program. Jahanshahloo et al. [42] addressed intertemporal dependency among efficiencies of a DMU_{o} in multiple periods. They proposed inverse dynamic DEA model. Furthermore, they introduced a periodic weak Pareto solution in multiple-objective linear programming. Lertworasirikul et al. [43] proposed inverse

Authors	Approaches and techniques	Sustainable SCM criteria
Awasthi et al. [29]	Fuzzy Multi-Criteria Decision Making (MCDM)	Environmental criteria
Büyüközkan et al. [30]	Fuzzy MCDM in the presence of incomplete information	Environmental and economic criteria
Erol et al. $[31]$	Fuzzy MCDM	Environmental criteria
Govindan et al. [32]	Fuzzy MCDM based on triple bottom line approach	Environmental and economic criteria
Kuo et al. $[33]$	Artificial neural network and MADM	Environmental, social, and economic criteria
Punniyamoorthy et al. [34]	Structural equation modeling in fuzzy context	Economic criteria
Amindoust et al. [35]	Fuzzy inference system ranking model	Environmental, social, and economic criteria
Yeh and Chuang [36]	MCDM by use of Genetic Algorithm	Environmental and economic criteria
Azadi et al. [27]	Enhanced Russell measure DEA model in fuzzy context	Environmental, social, and economic criteria

Table 1. Sustainable SCM criteria and different approaches for assessing sustainability.

DEA model based on linear programming and Pareto optimal solution. Their main DEA model is based upon BCC (Banker-Charnes-Cooper) model [44].

Amin et al. [45] merged a couple of DMUs and studied whether or not the merged DMU could affect efficiency frontier. Amin et al. [46] used inverse DEA model to recommend higher operational efficiency. Eyni et al. [47] divided inputs/outputs into desirable and undesirable inputs/outputs and applied inverse DEA model to increase desirable outputs and decrease undesirable outputs.

2.2.2. RAM model

In real world, there are differences in measurement unit of variables. In addition, in some cases, there might be big ranges in inputs and outputs. Some DEA models can cope with different measurement units, which are called unit invariant models [48]. For instance, CCR [9] and BCC [44] models are considered as unit invariant models. On the other hand, there might be zero and negative values in datasets [49]. Some of DEA models can deal with negative and zero values called translation invariant, i.e., translation of values does not affect results [50]. Additive (ADD) model and BCC model are translation invariant, although the input-oriented BCC is invariant under output translation, and vice versa [51]. RAM is an extension of the ADD model, which is both unit and translation invariant [52].

In this paper, a new extension of RAM model is introduced, which is called input/output oriented-RAM model (oriented-RAM). Moreover, the inverse oriented-RAM model with network and dynamic structure is proposed.

2.2.3. Network and dynamic DEA models

Tone and Tsutsui [53] argued that traditional DEA models dealt with DMUs as black boxes and could not address network structure of DMUs. They proposed a network SBM model and calculated "divisional efficiency" of each division in each DMU. Färe and Grosskopf [54], for the first time, addressed intermediate products and, then, extended their work and developed network DEA model [55]. Sexton and Lewis [56] proposed a two-stage DEA model and extended their work to multi-stage networks. Mirhedayatian et al. [57] proposed a network DEA model to assess green supply chains.

Färe and Grosskopf [12] first introduced dynamic DEA. Tone and Tsutsui [58] proposed a dynamic SBM measure and calculated "term efficiency" for each DMU

in each period. Chen [59] proposed a network DEA model with dynamic effects on network. Park and Park [60] expanded Debreu-Farrell technical efficiency and applied their multi-period model to cable TV service units. Shabanpour et al. [61] utilized dynamic DEA and artificial neural networks to evaluate past, present, and future efficiencies of green supply chains. Tone and Tsutsui [13] combined network and dynamic DEA models and proposed network dynamic DEA model.

3. The proposed models

3.1. Oriented-RAM model

Basic RAM model proposed by Cooper et al. [52] is as follows:

$$\max \quad \theta = \frac{1}{m+p} \left(\sum_{i=1}^{m} R_i^x s_i^x + \sum_{r=1}^{p} R_r^y s_r^y \right),\,$$

s.t.:

$$\sum_{j}^{n} x_{ij}\lambda_{j} + s_{i}^{x} = x_{io}, \qquad i = 1, \cdots, m,$$

$$\sum_{j}^{n} y_{rj}\lambda_{j} - s_{r}^{y} = y_{ro}, \qquad r = 1, \cdots, p,$$

$$\lambda_{j}, s_{i}^{x}, s_{r}^{y} \ge 0, \qquad \forall i, j, r, \qquad (1)$$

where s_i^x and s_r^y are distances of DMU_o from efficient frontier. R_i^x and R_r^y denote ranges of inputs and outputs calculated as $1/(x_i^U - x_i^L)$ and $1/(y_r^U - y_r^L)$, respectively. Upper and lower bounds are specified by $x_i^U = \max_j \{x_{ij}\}, y_r^U = \max_j \{y_{rj}\}$ as well as $x_i^L = \min_j \{x_{ij}\}, y_r^L = \min_j \{y_{rj}\}$, respectively. Objective function measures inefficiency of DMU_o. Efficiency score is calculated by $\theta^* = 1 - (1/m + p) (\sum_{i=1}^m R_i^x s_i^{x*} + \sum_{r=1}^p R_r^y s_r^{y*})$. A DMU_o (supply chain) is efficient if the objective function of Model (1) is zero, i.e., $s_i^{x*} = s_r^{y*} = 0$. Our new input-oriented RAM model is as follows:

$$\max \quad \frac{1}{m} \sum_{i=1}^{m} R_i^x s_i^x,$$

s.t.:

$$\sum_{j}^{n} x_{ij}\lambda_{j} + s_{i}^{x} = x_{io}, \qquad i = 1, \cdots, m,$$
$$\sum_{j}^{n} y_{rj}\lambda_{j} \ge y_{ro}, \qquad r = 1, \cdots, p,$$
$$\sum_{j}^{n} \lambda_{j} = 1,$$

$$\lambda_j, s_i^x \ge 0, \qquad \forall \ i, j, r, \tag{2}$$

where R_i^x is $1/(x_i^U - x_i^L)$.

The reason for proposing the oriented-RAM model is that, in real world, some cases exist in which there might be very a high range of inputs or outputs. On the other hand, in some cases, such as production plants, divisions produce intermediate measures delivered to next divisions. Thus, except for the last division, other divisions cannot deliver outputs to outside of the network (e.g., water refinery). Therefore, ordinary RAM model cannot be utilized. There is a significant difference between our model and the other unit and translation invariant DEA models. Our idea originates from input (output) oriented SBM model proposed by Cooper et al. [51].

Theorem 1. In optimal solution, efficiency score is $0 \le \theta^* \le 1$.

Proof. According to Aida et al. [62], in an optimal solution, there is:

$$0 \le -\sum_{j}^{n} x_{ij} \lambda_{j}^{*} + x_{io} = s_{i}^{x^{*}} \le x_{i}^{U} - x_{i}^{L}.$$
 (3)

Eq. (3) comes from condition $\sum_{j=1}^{n} \lambda_{j} = 1$. Therefore, we have:

$$0 \le R_i^x s_i^{x^*} \le 1. \tag{4}$$

Theorem 2. The RAM model is translation invariant. This theorem can be generalized for input-oriented RAM model. Suppose that there are n DMUs with one input and one output. Changes after translation are depicted in Figures 1, 2, and 3.

As is observed, in Figures 1, 2, and 3, translation cannot change direction or amount of efficiency improvement.



Figure 1. Basic RAM.



Figure 2. Output oriented-RAM model.



Figure 3. Input oriented-RAM model.

Proof. For proof, see Cooper et al. [63]. \blacksquare

Theorem 3. The input-oriented RAM model is unit invariant in inputs. In addition, output-oriented RAM model is unit invariant in outputs, corresponding to the objective function of input (output)-oriented RAM model (Model 2). As is seen, there are only inputs' (outputs') slacks in the objective function.

Now, output-oriented RAM model is proposed. Model (5) has characteristics similar to those of Model (2):

$$\max \quad \frac{1}{p} \sum_{r=1}^{p} R_{r}^{y} s_{r}^{y},$$

s.t.:
$$\sum_{j}^{n} x_{ij} \lambda_{j} \leq x_{io}, \qquad i = 1, \cdots, m,$$
$$\sum_{j}^{n} y_{rj} \lambda_{j} - s_{r}^{y} = y_{ro}, \qquad r = 1, \cdots, p,$$

$$\sum_{j}^{n} \lambda_{j} = 1,$$

$$\lambda_{j}, s_{r}^{y} \ge 0, \qquad \forall i, j, r.$$
(5)

p,

Proof. For proof, see Cooper et al. [63]. ■

3.2. Network-dynamic input-oriented RAM (NDIO-RAM) model

In this subsection, we extend the input-oriented RAM model to a network dynamic model. Suppose that there are *n* DMUs $(j = 1, \dots, n)$ with *k* divisions (k = $1, \dots, K$ in each t period $(t = 1, \dots, T)$. Notations are as follows:

- x_{ijk}^t The *i*th input of the *j*th DMU in the kth division in term t;
- y_{rjk}^t The *r*th output of the *j*th DMU in the kth division in term t;
- $l_{wi(k-h)}^t$ The wth $(w = 1, \cdots, W)$ intermediate measure of the jth DMU sent from the kth division to the hth division in term t;
- $c_{ujk}^{t,t+1}$ The *u*th $(u = 1, \dots, U)$ carry-over of the jth DMU in the kth division from term t to term t + 1;
- λ_{jk}^t Intensity vector of the jth DMU in the kth division in term t.

At this juncture, the NDIO-RAM model is proposed as follows:

$$\max \quad \frac{1}{T} \sum_{t=1}^{T} \frac{1}{K} \sum_{k=1}^{K} \frac{1}{m} \sum_{i=1}^{m} R_{iok}^{x^{t}} s_{iok}^{x^{t}},$$

s.t.:

$$\begin{split} \sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + s_{iok}^{x^{t}} &= x_{iok}^{t}, \\ i &= 1, \cdots, m, \quad \forall K, T, \\ \sum_{j}^{n} y_{rjk}^{t} \lambda_{jk}^{t} &\geq y_{rok}^{t}, \qquad r = 1, \cdots, p, \quad \forall K, T \\ \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} &= \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t}, \\ w &= 1, \cdots, W, \quad \forall K, T, \\ \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} &= \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1}, \\ u &= 1, \cdots, U, \quad t = 1, \cdots, T - 1, \quad \forall K, \\ \sum_{j}^{n} \lambda_{jk}^{t} &= 1, \qquad \forall K, T, \end{split}$$

$$\lambda_{jk}^t, s_{iok}^{x^t} \ge 0, \qquad \forall \ i, j, r.$$
(6)

Model (6) is a general model in which there is no preference for divisions, inputs, and terms. Intermediate measures and carry-overs have indirect impact on objective function.

3.3. Inverse oriented-RAM model

For the first time, Wei et al. [37] introduced the following inverse (Models (7) and (8)). Their inverse model was derived from a general radial output-oriented DEA model.

 $\max z_0,$

$$\sum_{j}^{n} x_{ij} \lambda_{j} \leq x_{io}, \qquad i = 1, \cdots, m,$$

$$\sum_{j}^{n} y_{rj} \lambda_{j} \geq y_{ro} z_{0}, \qquad r = 1, \cdots, p,$$

$$\delta_{1} \left(\sum_{j}^{N} \lambda_{j} + \delta_{2} (-1)^{\delta_{3}} v \right) = \delta_{1},$$

$$\lambda_{j}, v \geq 0, \qquad \forall i, j, r. \qquad (7)$$

Parameters δ_1 , δ_2 , and δ_3 can have only 0 or 1 values:

- If $\delta_1 = 0$, then Model (7) is a CCR model;
- If $\delta_1 = 1$ and $\delta_2 = 0$, then Model (7) is a BCC model;
- If $\delta_1 = \delta_2 = 1$ and $\delta_3 = 0$, then Model (7) is a non-increasing model;
- If $\delta_1 = \delta_2 = \delta_3 = 1$, then Model (7) is a non-decreasing model.

Wei et al. [37] supposed that inputs of DMU_o (x_{io}) increased to a given value, i.e., a_i . Then, they tried to determine proper values for β_r given that objective function values of Models (7) and (8) are equal, i.e., $z_o^* = z_{inv}^*$. Wei et al. [37] proposed a new dummy DMU_{n+1} with input vector a_{io} and output vector β_{ro} , where $a_{io} = x_{io} + \Delta x_{io}$ and $\beta_{ro} = y_{ro} + \Delta y_{ro}$.

$$\begin{array}{ll} \max & z_{inv}, \\ \text{s.t.:} \\ & \sum_{j}^{n} x_{ij}\lambda_{j} + \alpha_{i0}\lambda_{n+1} \leq \alpha_{i0}, \\ & \sum_{j}^{n} y_{rj}\lambda_{j} + \beta_{ro}\lambda_{n+1} \geq \beta_{ro}z_{inv}, \\ & r = 1, \cdots, p, \end{array}$$

$$\delta_1\left(\sum_{j}^N \lambda_j + \lambda_{n+1} + \delta_2(-1)^{\delta_3} v\right) = \delta_1,$$

$$\lambda_j, v \ge 0, \qquad \forall \ i, j = 1, 2, \cdots, n+1, r.$$
(8)

In our proposed model, there are not any given predetermined values for neither a_{io} nor β_{ro} . Model (13) is a multi-objective linear programme that determines a_{io} and β_{ro} .

Definition 1. Let the optimal solution for the following input-oriented RAM model be $(z_0^*, \lambda_i^*, s_i^{x^*})$:

$$\max \quad z_{0} = \frac{1}{m} \sum_{i=1}^{m} R_{i}^{x} s_{i}^{x},$$

s.t.:
$$\sum_{j}^{n} x_{ij} \lambda_{j} + s_{i}^{x} = x_{io}, \qquad i = 1, \cdots, m,$$

$$\sum_{j}^{n} y_{rj} \lambda_{j} \ge y_{ro}, \qquad r = 1, \cdots, p,$$

$$\sum_{j}^{n} \lambda_{j} = 1,$$

$$\lambda_{j}, s_{i}^{x} \ge 0, \qquad \forall i, j, r. \qquad (9)$$

Definition 2. The input-oriented RAM inverse model can be formulated as Model (10), and its optimal solution is $(z_{inv}^*, \lambda_i^*, \lambda_{i+1}^*, s_i^{\bar{a}^*})$:

$$\max \quad z_{inv} = \frac{1}{m} \sum_{i=1}^m R_i^x s_i^{\bar{\alpha}},$$

s.t.:

$$\sum_{j}^{n} x_{ij}\lambda_{j} + \bar{\alpha}_{io}\lambda_{n+1} + s_{i}^{\bar{\alpha}} = \bar{\alpha}_{io},$$

$$i = 1, \cdots, m,$$

$$\sum_{j}^{n} y_{rj}\lambda_{j} + (y_{ro} + \Delta \bar{y}_{ro})\lambda_{n+1} \ge y_{ro} + \Delta \bar{y}_{ro},$$

$$r = 1, \cdots, p,$$

$$\sum_{j}^{n} \lambda_{j} + \lambda_{n+1} = 1,$$

$$\lambda_{j}, \lambda_{n+1}, s_{i}^{\bar{\alpha}} \ge 0, \quad \forall i, j, r.$$
(10)

Given the assumption, z_0^* from Model (9) and z_{inv}^* from Model (10) have similar values. In addition,

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 R_i^x is assumed constant as we want to keep efficiency frontier unchanged. Therefore, the following equation is considered:

$$\frac{1}{m}\sum_{i=1}^{m}R_{i}^{x}s_{i}^{x^{*}} = \frac{1}{m}\sum_{i=1}^{m}R_{i}^{x}s_{i}^{\bar{\alpha}^{*}}.$$
(11)

As a result:

$$s_i^{x^*} = s_i^{\tilde{\alpha}^*}.$$
 (12)

Now, a multi-objective linear programme (13) is utilized that determines α_{io} and Δy_{ro} , simultaneously, where $\alpha_{io} = x_{io} + \Delta x_{io}$:

min
$$\alpha_{io}$$
,
s.t.:

$$\sum_{j}^{n} x_{ij} \lambda_{j} + s_{i}^{x^{*}} = \alpha_{io}, \qquad i = 1, \cdots, m,$$

$$\sum_{j}^{n} y_{rj} \lambda_{j} = y_{ro} + \Delta y_{ro}, \qquad r = 1, \cdots, p,$$

$$\alpha_{io} \ge x_{io},$$

$$\lambda_{j} \ge 0, \qquad \forall i, j, r,$$

$$\Delta y_{ro} : \text{free.} \qquad (13)$$

In the first constraint of Model (13), s_i^{α} is replaced by $s_i^{x^*}$. R_i^x is assumed to be constant. The last condition of Model (13) guarantees that purpose.

Definition 3. Suppose that $\bar{\alpha}_{io}$, $\Delta \bar{y}_{ro}$, and $\bar{\lambda}_i$ are feasible solutions. If there is no feasible solution such as $\alpha_i < \bar{\alpha}_{io}, (\bar{\alpha}_{io}, \Delta \bar{y}_{ro}, \bar{\lambda}_i)$ can be a weak Pareto solution for Model (13).

Theorem 4. $(\bar{\alpha}_{io}, \Delta \bar{y}_{ro}, \bar{\lambda}_j)$ is a weak Pareto solution for Model (13) and z_o^* is the optimal objective function value for Model (9). z_{RA}^* is the optimal objective function value for Model (14):

 $\cdot , p,$

$$\max \quad z_{RA} = \frac{1}{m} \sum_{i=1}^{m} R_i^x s_i^{\alpha},$$

s.t.:
$$\sum_j^n x_{ij} \lambda_j + s_i^{\alpha} = \bar{\alpha}_{io}, \qquad i = 1, \cdots, m,$$

$$\sum_j^n y_{rj} \lambda_j \ge y_{ro} + \Delta \bar{y}_{ro}, \qquad r = 1, \cdots, p,$$

$$\sum_j^n \lambda_j = 1,$$

$$\lambda_j, s_i^{\alpha} \ge 0, \qquad \qquad \forall \ i, j, r. \tag{14}$$

Proof. Model (14) has an optimal solution $(z_{RA}^*, \lambda_i^{\alpha})$ $s_i^{\alpha^*}$). The optimal solution of Model (13) is embedded in its first constraint and that of Model (14) in its first constraints. Therefore, given Model (13), we have:

$$\sum_{j}^{n} x_{ij} \bar{\lambda}_j + s_i^{x^*} = \bar{\alpha}_{io}.$$
(15)

In addition, given Model (14), we have:

$$\sum_{j}^{n} x_{ij} \lambda_j^{\alpha} + s_i^{\alpha^*} = \bar{\alpha}_{io}.$$
⁽¹⁶⁾

Consequently:

$$\sum_{j}^{n} x_{ij} \lambda_{j}^{\alpha} + s_{i}^{\alpha^{*}} = \sum_{j}^{n} x_{ij} \bar{\lambda}_{j} + s_{i}^{x^{*}}.$$
 (17)

Furthermore, given Definition 3 and Model (14), we know the optimal solution of Model (13), and $(\bar{\alpha}_{io})$, $\Delta \bar{y}_{ro}, \bar{\lambda}_i$ is a feasible solution for Model (14). Given Models (9) and (14) and Definition 3, we have:

$$z_{RA}^* \ge z_o^*. \tag{18}$$

As mentioned earlier, R_i^x remains constant. Therefore:

$$s_i^{\alpha^*} \ge s_i^{x^*}. \tag{19}$$

If $z_{RA}^* > z_o^*$, then:

$$s_i^{\alpha^*} > s_i^{x^*}.$$
 (20)

By Eqs. (17) and (20), we have:

$$\sum_{j}^{n} x_{ij} \lambda_{j}^{\alpha} < \sum_{j}^{n} x_{ij} \bar{\lambda}_{j}.$$
(21)

To convert Expression (21) to an equation, h > 0 is added to left-hand side of Expression (21).

$$\sum_{j}^{n} x_{ij} \lambda_j^{\alpha} + h = \sum_{j}^{n} x_{ij} \bar{\lambda}_j.$$
(22)

Now, we substitute $\sum_{j}^{n} x_{ij} \lambda_{j}^{\alpha} + h$ by $\sum_{j}^{n} x_{ij} \overline{\lambda}_{j}$ in the first constrain of Model (13).

$$\sum_{j}^{n} x_{ij} \lambda_j^{\alpha} + s_i^{x^*} = \alpha_{io} - h.$$
(23)

Therefore, we have a feasible solution $(\lambda_i^{\alpha}, \bar{\alpha}_{io} - \bar{h})$ for Model (13), while we know that Model (13) has a weak Pareto solution $(\bar{\alpha}_{io}, \bar{\lambda}_j)$. Therefore, we have $z_{RA}^* = z_o^*$. Then, h = 0. By Theorem 4, the relationship between Models (14) and (13) is examined.

Theorem 5. Models (9) and (14) have similar objective function values: $z_{RA}^* = z_o^*$.

Proof. Given Theorem 4, we know that $s_i^{\alpha^*} = s_i^{\alpha^*}$. Thus, there is $\frac{1}{m} \sum_{i=1}^m R_i^x s_i^{\alpha^*} = \frac{1}{m} \sum_{i=1}^m R_i^x s_i^{\alpha^*}$.

Theorem 6. Models (10) and (14) have similar objective function values: $z_{RA}^* = z_{inv}^* s$.

Proof. Let $(z_{inv}^*, \lambda_j^*, \lambda_{j+1}^*, s_i^{\bar{a}^*})$ be the optimal solution of Model (10) and $z_{inv}^* \ge 0$. We suppose that $z_{inv}^* > 0$. If $z_{inv}^* > 0$, then $\lambda_{n+1} = 0$. In this case, we add a new constraint $(\lambda_{n+1} = 0)$ to Model (10) so that it becomes similar to Model (14). We can prove it by another manner. The dual of Model (10) is as follows:

min
$$\sum_{i}^{m} v_i \bar{\alpha}_{iO} - \sum_{r}^{p} u_r \left(\bar{y} + \Delta \bar{y}_{ro} \right) + \theta,$$

s.t.:

$$\sum_{i}^{m} v_{i} x_{iO} - \sum_{r}^{p} u_{r} y_{rj} + \theta \ge 0, \quad \forall j,$$

$$\sum_{i}^{m} v_{i} \bar{\alpha}_{iO} - \sum_{r}^{p} u_{r} \left(\bar{y} + \Delta \bar{y}_{ro} \right) + \theta \ge 0,$$

$$v_{i} \ge \frac{1}{mR_{i}^{x}}, \quad \forall i,$$

$$v_i, \theta$$
: free, $u_r \ge 0, \quad j = 1, 2, \cdots, n.$ (24)

Given the relationship between primal and dual problems [64], objective function value of Model (24) is similar to that of Model (10). Therefore, the second constraint of Model (24) should be an inequality. Thus, this constraint is redundant. Consequently, Model (24) is similar to Model (25). The only difference between Model (24) and Model (25) is the second constraint of Model (24).

min
$$\sum_{i}^{m} v_i \bar{\alpha}_{iO} - \sum_{r}^{p} u_r \left(\bar{y} + \Delta \bar{y}_{ro} \right) + \theta,$$

s.t.:

$$\sum_{i}^{m} v_{i} x_{iO} - \sum_{r}^{p} u_{r} y_{rj} + \theta \ge 0, \quad \forall j,$$

$$v_{i} \ge \frac{1}{m R_{i}^{x}}, \quad \forall i,$$

$$v_{i}, \theta : \text{free}, \quad u_{r} > 0, \quad j = 1, 2, \cdots, n. \quad (25)$$

Note that Model (25) is the dual of Model (10). In Model (10), the first set of constraints has equity sign. Therefore, the related dual variable (v_i) is free in sign.

Theorem 7. Let $(z_o^*, \lambda_i^*, \text{ and } s_i^{x^*})$ be the optimal

solution of Model (9) and $(z_{inv}^*, \lambda_j^*, \lambda_{j+1}^*, \text{ and } s_i^{\bar{a}^*})$ be the optimal solution of Model (10). Then, $z_{inv}^* = z_o^*$.

Proof. Given Theorems 4 and 5, it is proved that Models (9) and (14) have similar objective function values. Furthermore, in Theorem 6, we proved that Models (14) and (10) have similar objective function values. As a result, given Theorems 4, 5, and 6, Models (9) and (10) have similar objective function values. \blacksquare

3.4. Numeric example

Suppose that there are 8 DMUs, and each DMU has 2 inputs (x1 and x2) and 2 outputs (y1 and y2). Data are shown in Table 2.

Given input-oriented RAM model (Model 9), Table 3 demonstrates efficiency scores of DMUs and distances of DMU_o from efficient frontier, where $s_1^{x^*}$ and $s_2^{x^*}$ are distances of DMU_o from efficient frontier for input 1 and input 2, respectively.

Now, Model (13) is utilized and $s_1^{x^*}$ and $s_2^{x^*}$ are considered to determine α_{io} and Δy_{ro} , where $\alpha_{io} = x_{io} + \Delta x_{io}$. Results are shown in Table 4. Given Model (14) and Table 4, efficiency scores of inverse models are shown in Table 5.

As is seen, the efficiency scores in Tables 3 and 5 are similar, although some outputs have changed, yet inputs remain unchanged.

3.5. The inverse network-dynamic input-oriented RAM model

In a classical approach, a decision-maker changes outputs (inputs) and solves Model (8) for calculating a new set of inputs (outputs). Herein, for the first time, two approaches are proposed:

Approach 1. Given the presented theorems, here, we extend the inverse input-oriented RAM Model (10) to inverse network-dynamic input-oriented RAM model, proposed as follows:

$$\max \quad \frac{1}{T} \sum_{t=1}^{T} \frac{1}{K} \sum_{k=1}^{K} \frac{1}{m} \sum_{i=1}^{m} R_{iok}^{x^{t}} s_{iok}^{x^{t}},$$

Table 2. Numeric example dataset.

DMIIs	Inp	uts	Out	puts
DIVIOS	x_1	x_2	y_1	y_2
А	3	5	13	13
В	2	4	12	13
\mathbf{C}	5	7	15	15
D	4	6	14	15
Ε	8	10	18	13
F	9	13	19	17
G	1	2	20	15
Н	14	10	11	10

DMUs	\mathbf{A}	в	С	D	\mathbf{E}	\mathbf{F}	\mathbf{G}	Η
Efficiency scores	0.7867	0.8706	0.6189	0.7028	0.3672	1	1	0.1363
$S_{1}^{x^{*}}$	2	1	4	3	7	0	0	13
$S_{2}^{x^{*}}$	3	2	5	4	8	0	0	8

Table 3. Efficiency scores of DMUs.

Ta	able 4. F	Results of N	Model (13)	
	Cha	nges	Cha	nges
DMUs	in in	puts	in ou	$_{ m tputs}$
Diffes	Δx_{1o}	Δx_{2o}	Δy_{1o}	Δy_{2o}
А	0	0	7	2
В	0	0	8	2
С	0	0	5	0
D	0	0	6	0
Е	0	0	2	2
F	0	0	0	0
G	0	0	0	0
Н	0	0	9	5

s.t.:

$$\begin{split} \sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + s_{iok}^{x^{t}} &= x_{iok}^{t}, \qquad i = 1, \cdots, m, \\ \forall K, T, \\ \sum_{j}^{n} y_{rjk}^{t} \lambda_{jk}^{t} &\geq y_{rok}^{t}, \qquad r = 1, \cdots, p, \\ \forall K, T, \\ \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} &= \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t}, \\ w &= 1, \cdots, W, \qquad \forall K, T, \\ \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} &\geq c_{uok}^{t,t+1}, \\ u &= 1, \cdots, U, \qquad t = 1, \cdots, T-1, \qquad \forall K, \\ \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} &= \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1}, \\ u &= 1, \cdots, U, \qquad t = 1, \cdots, T-1, \qquad \forall K, \end{split}$$

$$\sum_{j}^{n} \lambda_{jk}^{t} = 1, \qquad \forall K, T,$$
$$\lambda_{jk}^{t}, s_{iok}^{x^{t}} \ge 0, \qquad \forall i, j, r.$$
(26)

Tone and Tsutsui [13] classified intermediate measures into four categories: free, fixed (nondiscretionary), input intermediate, and output intermediates. In addition, they classified carry-overs into four categories: good, bad, free, and fixed carryovers. Model (26) demonstrates a case with fixed intermediate measures and good carry-overs. The third set of constraints of Model (26) connects two divisions. Moreover, the fifth set of constraints of Model (26) links two consecutive terms. Given Tone and Tsutsui [13] classification, good carry-overs play a role of outputs. As a result, in Model (26), we have good carry-overs addressed in the fourth set of constraints.

Model (27) is a multi-objective linear programme. It determines α_{iok}^t , Δy_{rok}^t , and $\Delta c_{uok}^{t,t+1}$, where ($\alpha_{iok}^t = x_{iok}^t + \Delta x_{iok}^t$). The optimal solution of Model (27) is ($\alpha_{iok}^{t^*}$, $\Delta y_{rok}^{t^*}$, $\Delta c_{uok}^{t,t+1^*}$, and, $\lambda_{jk}^{t^*}$).

min α_{iok}^t ,

s.t.:

$$\sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + s_{iok}^{x^{t^{*}}} = \alpha_{iok}^{t}, \qquad i = 1, \cdots, m,$$

$$\forall K, T,$$

$$\sum_{j}^{n} y_{rjk}^{t} \lambda_{jk}^{t} = y_{rok}^{t} + \Delta y_{rok}^{t}, \qquad r = 1, \cdots, p,$$

$$\forall K, T,$$

$$\sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} = \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t},$$

$$w = 1, \cdots, W, \qquad \forall K, T,$$

Table 5.	Efficiency	\mathbf{scores}	of	inverse	models
----------	------------	-------------------	----	---------	--------

\mathbf{DMUs}	А	в	С	D	\mathbf{E}	F	G	н
Efficiency scores	0.7867	0.8706	0.6189	0.7028	0.3672	1	1	0.1363

$$\sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} = c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1},$$

$$u = 1, \cdots, U, \qquad t = 1, \cdots, T - 1, \qquad \forall K,$$

$$\sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} = \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1},$$

$$u = 1, \cdots, U, \qquad t = 1, \cdots, T - 1, \qquad \forall K,$$

$$\alpha_{iok}^{t} \ge x_{iok}^{t}, \qquad i = 1, \cdots, m, \qquad \forall K, T,$$

$$\sum_{j}^{n} \lambda_{jk}^{t} = 1, \qquad \forall K, T,$$

$$\lambda_{jk}^{t} \ge 0, \qquad \Delta y_{rok}^{t}, \Delta c_{uok}^{t,t+1} : \text{free}, \quad \forall i, j, r, t. \quad (27)$$

Model (27) minimizes inputs and determines changes of normal outputs, intermediate outputs, and good carry-overs. Expression $\alpha_{iok}^t \geq x_{iok}^t$ does not let the inputs be decreased to less than original inputs. Thus, Models (26) and (28) have similar input ranges $(R_{iok}^{x^t} = R_{iok}^{{\alpha^t}^*})$. Finally, inverse network-dynamic input-oriented RAM model is as follows:

$$\max \quad \frac{1}{T} \sum_{t=1}^{T} \frac{1}{K} \sum_{k=1}^{K} \frac{1}{m} \sum_{i=1}^{m} R_{iok}^{\alpha^{t^{*}}} s_{iok}^{\alpha^{t}},$$

s.t.:

$$\begin{split} \sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + \alpha_{iok}^{t^{*}} \lambda_{(n+1)k}^{t} + s_{iok}^{\alpha^{t}} &= \alpha_{iok}^{t^{*}}, \\ i &= 1, \cdots, m, \qquad \forall K, T, \\ \sum_{j}^{n} y_{rjk}^{t} \lambda_{jk}^{t} + \left(y_{rok}^{t} + \Delta \bar{y}_{rok}^{t}\right) \lambda_{(n+1)k}^{t} \geq y_{rok}^{t} + \Delta y_{rok}^{t^{*}}, \\ r &= 1, \cdots, p, \qquad \forall K, T, \\ \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} + l_{wj(k-h)}^{t} \lambda_{(n+1)k}^{t} = \sum_{j}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t} \\ &+ l_{wj(k-h)}^{t} \lambda_{(n+1)h}^{t}, \\ w &= 1, \cdots, W, \qquad \forall K, T, \\ \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} + \left(c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1^{*}}\right) \lambda_{(n+1)k}^{t} \\ &\geq c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1^{*}}, \\ u &= 1, \cdots, U, \qquad t = 1, \cdots, T - 1, \qquad \forall K, \end{split}$$

$$\sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} + \left(c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1*}\right) \lambda_{(n+1)k}^{t}$$

$$= \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1} + \left(c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1*}\right) \lambda_{(n+1)k}^{t+1},$$

$$u = 1, \cdots, U, \qquad t = 1, \cdots, T-1, \qquad \forall K,$$

$$\sum_{j}^{n} \lambda_{jk}^{t} + \lambda_{(n+1)k}^{t} = 1, \qquad \forall K, T,$$

$$\lambda_{jk}^{t}, \lambda_{(n+1)k}^{t}, s_{iok}^{\alpha^{t}} \ge 0, \qquad \forall i, j, r. \qquad (28)$$

Given the inverse oriented-RAM (Model (10)), only two types of variables, including intermediate measures and carry-overs, are added to Model (28). Intermediate measures and carry-overs do not have direct impact on objective function.

Approach 2. Given Model (27), we propose Model (29). Inputs and outputs are changed simultaneously. In Model (29), despite Model (27), inputs can be reduced to their lower bounds and be increased to their upper bounds. Expression $\underline{x}_{iok}^t \leq x_{iok}^t + \Delta x_{iok}^t \leq \bar{x}_{iok}^t$ guarantees input ranges to remain unchanged. Also \underline{x}_{iok}^t and \bar{x}_{iok}^t are lower and upper bounds of inputs, respectively.

$$\begin{split} \min & \Delta x_{iok}^t, \\ \text{s.t.:} \\ \sum_j^n x_{ijk}^t \lambda_{jk}^t + s_{iok}^{xt^*} = x_{iok}^t + \Delta x_{iok}^t, \quad i = 1, \cdots, m, \\ & \forall K, T, \\ \sum_j^n y_{rjk}^t \lambda_{jk}^t = y_{rok}^t + \Delta y_{rok}^t, \quad r = 1, \cdots, p, \\ & \forall K, T, \\ \sum_j^n l_{wj(k-h)}^t \lambda_{jk}^t = \sum_j^n l_{wj(k-h)}^t \lambda_{jh}^t, \\ & w = 1, \cdots, W, \quad \forall K, T, \\ \sum_j^n c_{ujk}^{t,t+1} \lambda_{jk}^t = c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1}, \\ & u = 1, \cdots, U, \quad t = 1, \cdots, T - 1, \quad \forall K, \\ \sum_j^n c_{ujk}^{t,t+1} \lambda_{jk}^t = \sum_j^n c_{ujk}^{t,t+1} \lambda_{jk}^{t+1}, \end{split}$$

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 $u = 1, \cdots, U, \qquad t = 1, \cdots, T - 1, \qquad \forall K,$ $\underline{x}_{iok}^{t} \leq x_{iok}^{t} + \Delta x_{iok}^{t} \leq \bar{x}_{iok}^{t},$ $i = 1, \cdots, m, \qquad \forall K, T,$ $\sum_{j}^{n} \lambda_{jk}^{t} = 1, \qquad \forall K, T,$ $\lambda_{jk}^{t} \geq 0, \quad \Delta x_{iok}^{t}, \Delta y_{rok}^{t}, \Delta c_{uok}^{t,t+1} : \text{free}, \quad \forall i, j, r, t.$ (29)

4. Case study

Nirou Moharekeh Industrial Co. (NMI) is an Iranian manufacturer that manufactures spare parts such as different types of gear boxes, splines, and shafts. NMI delivers them to Iran Khodro (an Iranian automaker). NMI has 12 suppliers that provide gear boxes. Dataset is shown in Table 6, which dates back to 2010-2015. Suppliers provide required spare parts of NMI Co. Figure 4 shows the structure of supply chain.

In this paper, we focus on suppliers of NMI Co. Each supplier of NMI has three divisions (see Figure 5). Each division has three inputs (including wage cost, energy cost, and material cost (economic factors)), two good carry-overs (including green programs and ISO



Figure 4. Overall structure of supply chain of NMI.



Figure 5. Internal structure of each supplier of NMI.

TS (environmental factor)), and human care programs (social factor). In addition, each division has one fixed intermediate measure (intermediate product) (see Figure 6). First, divisions have only two inputs including wage cost and energy cost.

Figure 6 depicts divisions, inputs, carry-overs, and intermediate measure of the jth supplier of NMI during 6 years. The following notations are defined:

- x_{ijk}^t The *i*th input of the *j*th DMU in the kth division in term t;
- $l_{wj(k-h)}^{t}$ The wth $(w = 1, \dots, W)$ intermediate measure of the *j*th DMU which is sent from the *k*th division to the *h*th division in term *t*;
- $c_{ujk}^{t,t+1}$ The *u*th $(u = 1, \dots, U)$ carry-over of the *j*th DMU in the *k*th division from term *t* to term t + 1.

First, DMUs' efficiency scores are calculated in 6 years (terms). Given Table 6, there are huge differences between the smallest and biggest values in inputs (big ranges). Thus, our new (Model (30)) can be used.

$$\max \quad \frac{1}{T} \sum_{t=1}^{T} \frac{1}{K} \sum_{k=1}^{K} \frac{1}{m} \sum_{i=1}^{m} R_{iok}^{x^{t}} s_{iok}^{x^{t}},$$

s.t.:

$$\sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + s_{iok}^{x^{t}} = x_{iok}^{t}, \qquad i = 1, \cdots, m,$$
$$\forall K, T,$$

$$\sum_{j=1}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} = \sum_{j=1}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t},$$
$$w = 1, \cdots, W, \qquad \forall K, T,$$
$$\sum_{j=1}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} \ge c_{uok}^{t,t+1}, \qquad u = 1, \cdots$$

$$j \qquad \qquad t = 1, \cdots, T - 1, \qquad \forall K.$$

$$\sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} = \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1}, \qquad u = 1, \cdots, U,$$
$$t = 1, \cdots, T - 1 \qquad \forall K$$

, U,

$$\sum_{i}^{n} \lambda_{jk}^{t} = 1, \qquad \forall K, T,$$

 $\lambda_{jk}^{t}, s_{iok}^{x^{t}} \ge 0, \qquad \qquad \forall \ i, j, r.$ (30)

							Table 6. I	$) at a set^*$.					
							Suppliers (I	OMUs)					
		TECH. A. T.	STEEL P.	D. L. KARAN	PARS HAM.	FARAZAN	SIRIN S. N.	PIROOZ	ALSAN	KARIN	TIR	BARAN	HAMRAH
	Division 1 Wage Energy Material	8,635,365,571 31,987,890 0	$\begin{array}{c} 1,999,707,195\\ 64,357,095\\ 0\end{array}$	794,951,857 33,108,240 0	$\begin{array}{c} 491,717,007\\ 12,245,228\\ 0\end{array}$	113,100,561 1,334,355 0	98,708,866 2,343,000 0	000	1,007,877,808 9,091,335 0	299,144,2858,311,875 0	238,468,076 4,686,000 0	259,199,894 6,619,635 0	000
	ISO Green	6,925,500	3,000,000	1,500,000	2,940,000	2,850,000	2,550,000	1,350,000	2,880,000	3,600,000	2,535,000	2,760,000	1,350,000
	Human care Intermediate	27,830,250 300 525	11,969,100 787 165	11,969,100 404 485	11,969,100 140 680	11,969,100 16.207	11,969,100 28 545	11,969,100 0	11,969,100 110,745	11,969,100 101 418	11,969,100 56 976	11,969,100 80 863	11,969,100 0
	measure Division 2				0 0 0 1 1			0	2 	0 4 4 5 5	5		2
	Wage Energy	20,075,290,095 511.806.240	5,937,128,890 1.029.713.520	$1,727,520,545\\529,731.840$	$1,123,924,587\\195,923,640$	296,569,872 21.349,680	258,832,276 37.488.000	00	2,048,884,342 145,461.360	719,541,969 132.990.000	614,515,373 74.976.000	612,914,666 $105,914,160$	00
c	Material ISO Green	6,197,503,577	10,336,941,152	11,344,526,256	2,551,443,820	0 000 000 0	682,685,080	0	5,044,580,800	3,915,134,424	682,685,080	760,085,600	0
5010	and ISO TS Human care	9,234,000 27,830.250	4,000,000 11.969.100	2,000,000 11.969.100	0,920,000 11.969.100	3,800,000 11.969.100	3,400,000 11.969.100	11.969.100	3,840,000 11.969.100	4,800,000	11.969.100	3,000,000 11.969.100	11.969.100
	Intermediate measure	390,252	786,795	404,161	149,585	16,282	28,539	0	110,661	101,334	56,948	80,848	0
	Division 3												
	Wage	10,642,369,874 OF 062 670	2,690,482,931	958,560,399	602,630,617 26 735 603	145,288,159	126,800,692	0 0	1,190,510,533	372,898,265 24.025.625	304,441,286	321,255,117	0 0
	Material	538,913,355	898,864,448	99,324,120 986,480,544	221,864,680	4,003,003 0	6,0283,920	0 0	438,659,200	24,939,029 $340,446,472$	14,006,000 59,363,920	19,000,900 66,094,400	0 0
	ISO Green and ISO TS	6,925,500	3,000,000	1,500,000	2,940,000	2,850,000	2,550,000	1,350,000	2,880,000	3,600,000	2,535,000	2,760,000	1,350,000
	Human care	27,830,250	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100	11,969,100
	Intermediate measure	387,732	780,086	401, 312	148,427	16,174	28,400	0	110,198	100,750	56,800	80,238	0
	Division 1												
	Wage	9,285,235,307	1,026,619,436	1,159,823,859	1,465,291,441	153,891,064	1,819,894,113	1,882,400	119,326,391 2 706 600	130,488,341	1,287,254,608	269,329,613	191,583,192
	Material	0 0	0	0 0	0	100(10±(*	0	0	0	100,100,1	TOT'CC1'07	0	0
	ISO Green and ISO TS	19, 170, 000	7,800,000	4,050,000	8,700,000	7,410,000	8,160,000	4,620,000	7,440,000	10,860,000	6,300,000	7,140,000	4,200,000
	Human care	379,052,000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000
	Intermediate measure	406,910	414,439	405,754	428,648	23,055	333,817	1,205	34,983	40,452	264,813	99,443	15,780
	Division 2												
	Wage Enerøv	21,223,394,988 705.346.848	2,837,657,375 716.872.944	2,520,428,786 701.387.968	3,293,142,713 $741.735.408$	389,752,272 39.953.296	4,530,282,732 579,510,272	4,767,460 2.094.544	255,004,534 60.747.008	298,259,064 70.154.144	3,375,411,495 460.722.944	615,610,543 172.305.456	460,821,597 27.314.528
г	Material	3,955,272,793	8,813,218,016	8,120,457,464	4,360,864,400	1,055,516,294	3,210,501,000	506,912,640	484,232,800	852,138,975	3,210,501,000	11,816,360,400	0
107	ISO Green and ISO TS	25,560,000	10,400,000	5,400,000	11,600,000	9,880,000	10,880,000	6,160,000	9,920,000	14,480,000	8,400,000	9,520,000	5,600,000
:	Human care	379,052,000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000
	Intermediate measure	406,666	414,257	405,389	428,369	23,037	333,717	1,205	34,961	40,423	264,704	99,431	15,767
	Division 3 Wage	11, 379, 649, 286	1,344,345,390	1,398,526,478	1,785,967,103	195,270,223	2,295,400,888	2,388,550	143, 129, 574	159,921,801	1,653,597,922	330,080,653	238,818,000
	Energy Material	132,252,534 $343,936,765$	134,413,677 766,366,784	131,510,244 706,126,736	139,075,389 379,205,600	7,491,243 91,784,026	108,658,176 279,174,000	392,727 44,079,360	11,390,064 42,107,200	13,153,902 74,099,041	86,385,552 279,174,000	32,307,273 1,027,509,600	5,121,474 0
	ISO Green and ISO TS	19,170,000	7,800,000	4,050,000	8,700,000	7,410,000	8,160,000	4,620,000	7,440,000	10,860,000	6,300,000	7,140,000	4,200,000
	Human care	379,052,000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000	16, 302, 000
	Intermediate measure	404,442	411,051	402,172	425,307	22,909	332,288	1,201	34,832	40,226	264, 176	98,799	15,662
*	All wage costs	enerav costs m	naterial costs	ISO Green and	ISO TS inve	stments and	human care c	Dete are in I	ranian Rial				

continued).
Dataset [*] (c
6.
Table

						l eranddne	U MI US)					
	TECH. A. T.	STEEL P.	D. L. KARAN	PARS HAM.	FARAZAN	SIRIN S. N.	PIROOZ	ALSAN	KARIN	TIR	BARAN	HAMRAH
ivision 1												
Tage	6,999,013,439	830,938,474	978, 581, 366	948, 546, 783	267, 313, 648	1, 139, 039, 553	148, 284, 869	0	69,927,244	1,356,621,486	393,955,586	0
nergy	48.644.232	44.163.912	45.044.064	43.508.868	5.966.844	33.415.200	10.464.168	0	3.427.788	36.535.200	8.060.676	0
Taterial	0	0	0	0	0	0	0	0	0	0	0	0
O Green	000 200 2	000 011 6	020 020 1	001 001 6	100 001	0 075 404	1 054 400	0 000 410	1 950 004	0 609 0000	000 200 0	000 200 1
AT OSI DA	000,000,1	0,100,040	T,040,010	001,401,0	110,110,7	101010	T,00/1,100	011,000,7	1,000,1004	4,040,040	000,000,2	1,000,000
uman care	30,922,500	13, 299, 000	13,299,000	13, 299, 000	13,299,000	13, 299, 000	13, 299, 000	13,299,000	13, 299, 000	13, 299, 000	13,299,000	13,299,000
termediate	313,507	285,116	291,634	280,988	38,440	215,078	67,232	0	22,070	234,633	51,950	0
easure												
ivision 2												
/age	16, 271, 138, 033	2,256,595,454	1,892,993,462	2,131,794,289	713, 307, 925	2,884,789,034	432, 393, 692	0	162, 565, 175	3,263,128,004	885, 388, 348	0
nergy	778,307,712	706, 622, 592	720, 705, 024	696, 141, 888	95,469,504	534, 643, 200	167, 426, 688	0	54,844,608	584, 563, 200	128,970,816	0
laterial	5, 149, 379, 165	5, 533, 809, 476	5,051,765,264	4,943,969,600	587,710,720	1,844,565,040	344, 196, 840	0	2,498,484,480	5, 245, 591, 600	3,419,851,600	0
O Green	10,260,000	4,174,560	2,167,560	4,656,240	3,965,832	4,367,232	2,472,624	3,981,888	5,812,272	3, 371, 760	3,821,328	2,247,840
S.I. OSI PI	000 000 00	10,000,000	19 000 000	12 200 000	10 000 000	000 000 11	10 000 000	12 000 000	12 200 000	000 000 11	10,000,000	000 000 01
uman care	30,922,500	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000	13,299,000
itermediate easure	313, 350	284,999	291, 343	280,827	38,413	215,035	67,212	0	22,056	234,551	51,945	0
ivision 3												
Tage	8.625.701.964	1.081.053.733	1.139.004.541	1.156.134.065	345.558.258	1.445.311.392	198.128.522	C	86.179.513	1.691.096.314	480.171.860	0
nerev	145.932.696	132.491.736	135.132.192	130.526.604	17.900.532	100.245.600	31.392.504	0 0	10,283.364	109.605.600	24.182.028	0 0
laterial	447,772,101	481,200,824	439,283,936	429,910,400	51,105,280	160,396,960	29,930,160	0	217,259,520	456, 138, 400	297,378,400	0
O Green	7 695 000	3 130 920	1 625 670	3 492 180	2 974 374	3 275 494	1 854 468	2 986 416	4 359 204	2 528 820	2 865 996	1 685 880
AT OSI DA	000,000,1	0,1001,0	1,040,0	001,101,00	1011010	Far(0)a(0)	1,001,100	011:000.7	F07:000'F	e.040.040.4	000.000.1	1,000,000
uman care	30,922,500	13, 299, 000	13,299,000	13, 299, 000	13, 299, 000	13, 299, 000	13, 299, 000	13, 299, 000	13, 299, 000	13,299,000	13, 299, 000	13,299,000
ttermediate casure	311,822	283,102	288,744	278,903	38, 249	214,200	67,078	0	21,973	234,200	51,671	0
ivision 1		101 000 010 0			000 000 01			c	07 1 00 1 10	010 000 110	c	000 1 10 100
Vage	5,157,263,899 45 944 054	2,959,889,401 55 008 367	11 644 358	757,676,459 58 595 338	16,069,483 512 680	2,674,975,796 68 966 146	5,210,744 595 539		25,569,146 1 562 103	314,896,612 13 533 893		221,814,989 3 443 993
laterial	0	0	0	0	0	0	0	0	0	0	0	0
O Green	7.695.000	3.130.920	1.380.000	1.860.000	1.787.100	2.235.000	1.500.000	1.500.000	2.745.000	2.222.700	1.440.000	1.425.000
id ISO TS												
uman care	30,922,500	13, 299, 000	13, 299, 000	13, 299, 000	13,299,000	13, 299, 000	13,299,000	13, 299, 000	13,299,000	13,299,000	13,299,000	13, 299, 000
itermediate sasure	238,043	290,630	60,608	304,217	2,655	356,861	3,076	0	8,086	69,873	0	17,847
vivision 2												
Vage	12,195,077,064	4,860,293,986	339,536,988	2,057,636,404	43,640,202	6,774,778,648	11,910,272	0 (59,442,535	811,466,305	0 0	515,670,149
nergy !aterial	3.697.858.942	5.307.762.992	150,309,134 659.249.920	2.876.448.080	0,202,002	1,100,405,339 3.303.074.160	9,926,800 956,800		24,993,040 549.291.520	2.10, 041, 171 3.303.074.160		2.579.068.752
O Green	10 960 000	174 660	1 840 000	9 180 000	000 606 6	000 080 6	000 000 6	000 000 6	3 660 000	9 063 600	000 000 1	000 000 1
vd ISO TS	000°007'01	T, 1 (T, 000	000,010,1	000°00±'*	*,000,400,4	000,000,4	000°000°*	000°000°*	000,000,0	*,*00,000	000°070'T	т,200,000
uman care	30,922,500	13,299,000	13,299,000	13,299,000	13,299,000	13, 299, 000	13, 299, 000	13,299,000	13, 299, 000	13,299,000	13,299,000	13,299,000
ttermediate	237,924	290,510	60,547	304,044	2,653	356,790	3,075	0	8,081	69,849	0	17,834
amena												
vivision 3								1				
Vage	6,391,967,963	3,293,293,714	199,591,411	985,739,607	20,906,452	3,394,239,454	6,386,100	0	31,511,846	402,014,102	0	273,368,526
nergy 'aterial	137,832,103 321.552,951	167,995,101 461.544.608	57.326.080	175,786,014 250,125,920	1,538,040 0	200,898,439 287.223.840	1,780,018 83.200		4,080,308 47.764.480	40,601,470 287.223.840		10,329,670 224.266.848
O Green	000 000	000 000 0	1 200 000	1 860 000	1001	0.005 000	1 500 000	1 600 000	0.111.000	001 000 0	1 110 000	1 105 000
AT OSI DA	000,680,7	3,130,920	1,380,000	1,860,000	1,787,100	2,235,000	1,500,000	1,500,000	2,145,000	2,222,700	1,440,000	1,425,000
uman care	30,922,500	13,299,000	13,299,000	13, 299, 000	13, 299, 000	13, 299, 000	13, 299, 000	13,299,000	13, 299, 000	13, 299, 000	13,299,000	13,299,000
ttermediate	236,764	288,577	60,007	301,960	2,642	355,404	3,069	0	8,050	69,744	0	17,744
costs, ener	ev costs, mater	rial costs, ISO	Green and I	SO TS investi	ments, and 1	human care co	osts are in In	ranian Rial.				
	uman care urnan care termediate essure large o Green o Green uman care termediate essure ivision 3 large uman care termediate essure essure termediate essure termediate essure termediate essure termediate essure termediate essure termediate essure termediate essure es	at D. 15 $30,922,500$ termediate $313,507$ essure $16,271,138,033$ tage $16,271,138,033$ tage $16,271,138,033$ tage $16,271,138,033$ tage $16,271,138,033$ tage $5,149,377,165$ of Green $10,260,000$ at ISO TS $30,922,500$ termediate $313,350$ essure $30,922,500$ essure $313,350$ essure $30,922,500$ energy $145,5771,010$ of Green $7,695,000$ utaterial $447,772,03499$ attorial $30,922,500$ attorial $0,922,500$ attorial $0,922,500$ attorial $30,922,500$ attorial $0,052,500$ attorial $5,194,67$ of Green $7,695,000$ attorial $30,922,500$ attorial $30,922,500$ attorial $30,922,500$ attorial<	uman care $30,922,500$ $13,299,000$ twision 2 $313,507$ $285,116$ essure $313,507$ $285,116$ essure $16,271,138,033$ $2.266,595,454$ Age $778,307,712$ $706,622,592$ Age $16,271,138,033$ $2.266,595,454$ Age $16,271,138,033$ $2.266,595,454$ Age $10,260,000$ $4,174,560$ uman care $30,922,500$ $13,299,000$ ensure $313,350$ $284,999$ ensure $313,350$ $313,9020$ ensure $313,350$ $313,9020$ ensure $7,695,000$ $3,130,920$ ensure $7,695,000$ $3,130,920$ ensure $311,822$ $283,102$ ivision 1 $5,197,723,990$ $60,600$ <	at DO LS 30.922,500 13.290,000 13.290,000 13.290,000 ensure 313.507 285,116 291,634 every 16.271,138,033 2.356,505,444 1892,993,463 revery 778,307,712 753,305,476 5,051,756,034 Age 16.271,138,033 2.356,505,404 1892,993,463 Assoch 10.260,000 4,174,560 2.167,560 at Size 30.922,500 13,290,000 13,290,000 at Size 30.922,500 13,290,000 21,67,560 at Size 30.922,500 13,290,000 13,290,000 at Size 30.922,500 3,13,30,920 291,343 at Size 10.30,023,733 1,139,004,541 at Size 1,320,920 1,025,670 at Size 1,320,920 1,323,491 at Size 3,0323,500 3,13,320,920 1,325,670 at Size 1,320,920 1,325,670 1,325,670 at Size 1,44,47,721,011 441,735 1,325,670 at Size 3,3	mum curve 30.322.500 13.207 285.110 29.1634 280.008 tentime 313.607 285.110 29.1634 280.008 13.390.00 tentime 313.507 285.110 29.1634 280.00 13.390.00 tentime 16.371.138.033 2.265.505.414 1.802.903.402 2.111.794.280 tenetim 5.149.377.123 700.622.502 2.107.765.264 4.943.909.600 of SO TS 0.0226.000 13.299.000 13.2390.00 13.2390.00 of SO TS 0.0225.000 13.299.000 13.2390.00 13.2390.00 tentim 31.3.350 284.900 2.167.66.40 1.366.240 umma curve 31.3.350 31.3.290.000 13.299.000 13.299.000 terrind 447.772.101 481.300.32.503 11.66.43.55 429.210.400 terrind 447.772.101 481.300.32.503 132.290.000 13.299.000 terrind 311.522 283.102 132.500.000 13.299.000 terrind 311.522 283.102 <td< th=""><th>Link and the constant of the constant o</th><th>Multication in the state of the s</th><th>Matrix 30.32.5(0) 13.290.000<</th><th>mannesses 0.022.500 13.200.00</th><th>mannesses 30,923,00 13,290,00</th><th>Mathematication Constrained Constraine Constrained <thconstrained< th=""></thconstrained<></th><th>matrix matrix matrix<</th></td<>	Link and the constant of the constant o	Multication in the state of the s	Matrix 30.32.5(0) 13.290.000<	mannesses 0.022.500 13.200.00	mannesses 30,923,00 13,290,00	Mathematication Constrained Constraine Constrained <thconstrained< th=""></thconstrained<>	matrix matrix<

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							Suppliers	(DMUs)					
		TECH. A. T.	STEEL P.	D. L. KARAN	PARS HAM.	FARAZAN	SIRIN S. N.	PIROOZ	ALSAN	KARIN	TIR	BARAN	HAMRAH
	Division 1					c					c		c
	Wage Energy	3,275,020,758 53,264,009	3,146,751,467 $52,245,805$	1,110,990,248 105,019,056	267, 122, 183 14, 524, 504	0 0	23,835,939,828 139,024,956	26,711,219 2,928,176	1,481,194,491 25,372,465	201,268,145 8,052,337	0 0	368,487,488 $19,571,934$	0 0
	Material	0	0	0	0	0	0	0	0	0	0	0	0
	ISO Green and ISO TS	21,300,000	8,492,760	4, 140, 000	5,580,000	3,300,000	6,705,000	4,500,000	6,000,000	8,235,000	4,500,000	5,100,000	3,000,000
	Human care	40,500,000	18, 113, 333	18, 113, 333	18, 113, 333	18, 113, 333	18, 113, 333	18,113,333	18, 113, 333	18, 113, 333	18, 113, 333	18, 113, 333	18, 113, 333
	Intermediate measure	271,195	266,410	536,839	74,200	0	708,341	14,893	129, 206	40,975	0	99,651	0
	Division 2												
	Wage	11,276,994,552	5,252,131,945	2,627,092,963	725, 428, 804	0	50,094,716,775	77,889,017	3,502,493,051	518, 653, 781	0	886,335,543	0
	Energy Material	852,224,148 8 801 797 363	835,932,876 8 314 573 462	1,680,304,896 12.775.635.200	232,392,060 1 420 234 820	0 0	2,224,399,296 6 676 079 388	46,850,820 576 254 507	405,959,436 5 707 256 101	128,837,388 16-191-565-760	0 853-733-283	313,150,944 19-170-076-800	0 5.112.952.072
Ŧ	ISO Green	28,400,000	11,323,680	5,520,000	7,440,000	4,400,000	8,940,000	6,000,000	8,000,000	10,980,000	6,000,000	6,800,000	4,000,000
107	and ISO TS Human care	40.500.000	18.113.333	18.113.333	18.113.333	18.113.333	18.113.333	18.113.333	18.113.333	18.113.333	18,113,333	18.113.333	18.113.333
:	Intermediate measure	271,059	266,301	536,303	74,158	0	708,199	14,888	129,133	40,950	0	99,641	0
	Division 3												
	Wage	4,678,875,809	3,516,116,463	1,376,973,181	347, 526, 853	0	28,442,742,801	35,689,780	1,835,808,273	256,949,836	0	459, 338, 024	0
	Energy Material	159,792,028 765 373 684	156,737,414 723 006 388	315,057,168 1 110 024 800	43,573,511 193 408 680	0 0	417,074,868 580 528 642	8,784,529 50 100 088	76,117,394 406 283 130	24,157,010 1 407 962 240	0 74 237 677	58,715,802 1 666 963 200	0 444 604 528
	ISO Green	21 300 000	8 492 760	4 140 000	5 580 000	3 300 000	6 705 000	4 500 000	6 000 000	1,101,302,210 8 235 000	4 500 000	5 100 000	3 000 000
	and ISO TS												
	human care Intermediate	40,000,000	18,113,333	18,113,333	16,113,333	18,113,333	16,113,333	18,113,333	18,113,333	18,113,333	18,113,333	16,113,333	18,113,333
	measure	270,033	264, 871	532,416	73,635	0	704,816	14,845	128,631	40,823	0	99,224	0
	Division 1						; 1						
	Wage	2,526,389,793	742, 376, 500	2,558,045,226	505,069,803	0	5,289,447,136	54,653,665	1,346,095	96,673,773	793,398,567	0	162, 175, 771
	Energy	46,889,535	14,375,361	202, 227, 564	31,925,817	0 0	75,431,664	6,692,070	267,960	4,296,138	30,029,076	0 0	7,968,114
	ISO Green	0 550 000	9 240 000	0	9 510 000	0 010 000	0 000 000 6	000 000 5	0 2 2 0 000	0 4 560 000	9 750 000	0 300.000	3 150 000
	and ISO TS	0,000,000	0,440,000	T,900,000	000,010,0	2,910,000	000,000,0	2,100,000	0,040,000	±,000,000	0,100,000	000,000,0	0,100,000
	Human care	35,166,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667
	Intermediate measure	203,696	62,568	881,577	139,115	0	327,916	29,037	1,164	18,665	130, 302	0	34,657
	Division 2												
	Wage	8,535,839,392	1,239,074,445	5,030,739,984	1,371,627,693	0	10,064,771,753	151,067,056	3,076,790	240,651,103	2,193,016,435	0	396, 824, 952
	Energy Material	750, 232, 560 8.533.341.330	230,005,776 1.222.869.566	3,235,641,024 33.992.653.440	510,813,072 $4.126.165.358$	00	1,206,906,624 1.818.728.514	107,073,120 639,516.531	4,287,360 3.150.328.860	68,738,208 1.966.827.520	480,465,216 653,907.940	0 0	127,489,824 3.454.931.200
ç	ISO Green	11,400,000	4, 320, 000	2,600,000	4,680,000	3,880,000	5,280,000	3,600,000	5,120,000	6,080,000	5,000,000	4,400,000	4,200,000
107	and ISU TS Human care	35,166,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667	14,776,667
:	Intermediate	203,594	62, 542	880,697	139,036	0	327,850	29,028	1,163	18,654	130, 256	0	34,632
	Division 3 Wage	3.580.679.196	829.516.490	2.991.851.324	657.097.503	0	6.127.223.384	71.568.295	1.649.726	121.932.954	1.038.945.562	c	203.342.294
	Energy	140,668,605	43,126,083	606,682,692	95,777,451	0	226,294,992	20,076,210	803,880	12,888,414	90,087,228	0	23,904,342
	Material	742,029,681	106, 336, 484	2,955,882,908	358,796,988	0	158, 150, 306	55,610,133	273,941,640	171,028,480	56,861,560	0	300, 428, 800
	ISO Green and ISO TS	8,550,000	3,240,000	1,950,000	3,510,000	2,910,000	3,960,000	2,700,000	3,840,000	4,560,000	3,750,000	3,300,000	3,150,000
	Human care	35,166,667	14,776,667	14,776,667	14, 776, 667	14,776,667	14, 776, 667	14,776,667	14,776,667	14,776,667	14, 776, 667	14,776,667	14,776,667
	Intermediate	202,985	62, 231	875,444	138,207	0	326,544	28,970	1,160	18,598	129,996	0	34,494
*: All *	wage costs, en	erev costs, mat	erial costs. IS	O Green and	ISO TS invest	ments and	human care c	osts are in I	ranian Rial.				



Figure 6. Structure of each supplier of NMI.

 $\sum_{i}^{n} l_{wj(k-h)}^{t} \lambda_{jk}^{t} = \sum_{i}^{n} l_{wj(k-h)}^{t} \lambda_{jh}^{t},$

 $t = 1, \cdots, T - 1, \qquad \forall K,$

 $\forall K, T,$

 $1, \cdots, U,$

 $\sum_{i}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} = c_{uok}^{t,t+1} + \Delta c_{uok}^{t,t+1}, \qquad u = 1, \cdots, U,$

 $w = 1, \cdots, W,$

Table 7 demonstrates each division's efficiency and efficiency of terms for each supplier of NMI. As is observed in Table 7, DMU D has an increasing trend, while DMU F has a decreasing trend. DMUs A, I, and L are only overall efficient DMUs.

To determine changes of inputs and outputs, the following model is utilized:

min
$$\Delta x_{iok}^t$$
,

s.t.:

$$\sum_{j}^{n} x_{ijk}^{t} \lambda_{jk}^{t} + s_{iok}^{x^{t^{*}}} = x_{iok}^{t} + \Delta x_{iok}^{t}, \qquad \qquad \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t} = \sum_{j}^{n} c_{ujk}^{t,t+1} \lambda_{jk}^{t+1}, \qquad u = x_{iok}^{t}, \qquad \qquad x_{iok}^{t} = 1, \cdots, m, \qquad \forall K,$$

\mathbf{DMUs}	Overall			Term ef	fficiency			Divisi	onal effic	ciency
$(\mathbf{suppliers})$	efficiency	2010	2011	2012	2013	2014	2015	Div. 1	Div. 2	Div. 3
TECH. A. T. (A)	1	1	1	1	1	1	1	1	1	1
STEEL P. (B)	0.9974	1	1	0.9846	1	1	1	1	0.9923	1
D. L. KARAN (C)	0.5032	0.5441	0.4403	0.3861	0.9004	0.5501	0.1984	0.5672	0.4716	0.4709
PARS HAM. (D)	0.7047	0.8819	0.5157	0.4542	0.5069	0.9941	0.8758	0.7080	0.7022	0.7040
FARAZAN (E)	0.9999	1	1	0.9999	1	1	1	0.9999	1	1
SIRIN S. N. (F)	0.5396	0.9795	0.5931	0.6245	0.2901	0.2812	0.4691	0.4608	0.5778	0.5802
PIROOZ (G)	0.9999	1	1	1	1	1	0.9999	0.9999	1	1
ALSAN (H)	0.9702	0.8215	1	1	1	1	1	0.9817	0.9648	0.9641
KARIN (I)	1	1	1	1	1	1	1	1	1	1
TIR(J)	0.9206	0.9985	0.7178	0.8746	0.9331	1	1	0.9228	0.9261	0.9130
BARAN (K)	0.8907	0.9459	0.7120	0.7766	1	0.9096	1	0.9555	0.8583	0.8582
HAMRAH (L)	1	1	1	1	1	1	1	1	1	1

Table 7. Efficiency scores.

$$\sum_{j}^{n} \lambda_{jk}^{t} = 1, \qquad \forall K, T,$$
$$\Delta x_{iok}^{t}, \lambda_{jk}^{t} \ge 0, \qquad \Delta c_{uok}^{t,t+1} : \text{free}, \quad \forall i, j, r, t. \quad (31)$$

Results of Model (31) are shown in Table 4. Some points can be derived from the results:

- Inputs experience very low changes (Δx_{ijk}^t) . Structure of Model (31) addresses this result;
- Manufacturers D. L. KARAN, PARS HAM, SIRIN S. N., and TIR have bigger changes in carry-overs $(\Delta e_{uok}^{t,t+1});$
- Given DMU TIR, it can be found that DMUs with higher efficiency score may have more changes;
- Carry-overs have large changes. Positive changes of carry-overs imply DMUs' shortfall in investments in green programs, ISO TS programs, and human care programs. Conversely, negative changes imply excess investments.

5. Managerial implications

Key factors of sustainability of supply chains are economic, environmental, and social factors. Though the amount of investment in sustainability factors demonstrates management attention to sustainability of supply chains, investment in each sustainability factor should be proportionate. For instance, in Table 8, given results of PARS HAM, we conclude disproportionate investment.

Amount of investment in green programs and ISO TS is more than that of investment in human care programs. Negative carry-over changes indicate excess amounts of investment in green programs and ISO TS. Furthermore, PARS HAM has unbalanced investment in green programs during 6 years. On the other hand, positive changes of carry-over (human care programs) imply shortfall of investment in human care programs. Accordingly, the main finding of the case study is to know whether or not the investment of an organization is proportionate.

6. Conclusions

As Seuring and Muller [65] addressed, sustainable supply chain is a growing topic. Carbone et al. [66] argued that a couple of factors triggered companies to apply sustainability principles. Those factors included regulations, scandals, competitors' moves, and customer expectations. Wittstruck and Teuteberg [67] introduced House of Sustainable Supply Chain that had three pillars including environmental performance, economic performance, and social performance. Li [68] claimed that benefits of sustainability, including economic, environmental, and social benefits, should be achieved, simultaneously.

In this paper, a model was proposed to assess sustainability of supply chains. For the first time, we introduced inverse network and dynamic model based upon input-oriented RAM model. As mentioned earlier, RAM model is a unit and translation invariant DEA model. We discussed that the classical inverse DEA models could only determine input or output changes. For the first time, two approaches were proposed to determine input and output changes. The first approach was used to determine which inputs and carryovers, as well as to what extent, should be changed. In the second approach, inputs can be reduced to their

		ΔX^* and ΔC^*	TECH. A.T.	STEEL P.	D.L. KARAN	PARS HAM.	FARAZAN	Supplier SIRIN S. N.	s (DMUs) PIROOZ	ALSAN	KARIN	TIR	BARAN	HAMRAH
		DW ¹	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DEN ¹	-0.745E-8	0.0	0.0	0.0	0.0	1.970156	0.0	0.0084704	0.0	0.0	1.160656	0.0
	Div. 1	DCARGE-TS ²	-0.186E-8	0.0	-4407 17	-1004242	-0.433E-7	105469.2	0.0	-0.181928	-0.222E-6	187368.8	-103 3697	0.0
		DCARHC ³	0.745E-8	0.0	0.475E-8	0.104E-8	0.305874	00.02440	0.0	0.0	0.526E 7	0.186E.8	0.0	0.0
		DOAMIC	-0.74015-8	0.0	-0.47515-8	-0.10415-8	0.303874	55.02445	0.0	0.0	0.52015-7	0.10015-0	0.0	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DEN	0.10217 7	0.0	0.0	0.0	0.0	0.0	0.0	26 1752	0.0	0.0	10 7 2 7 0 8	0.0
0	Div 2	DEN DM4	-0.10315-7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	15.12150	0.0
201	2.11. 2	DM-	0.0	0.0	3781.88	0.0	0.0	26.13003	0.0	0.0	0.0	0.0	264.9410	0.0
		DCARGR-TS	0.332E-8	0.0	-3.0411	-88519.5	0.0	145506.2	0.0	-0.116260	0.521E-7	-2.026985	-0.873759	0.0
		DCARHC	-0.213E-8	0.0	0.37488	167730.6	0.0	0.0	0.0	-0.364701	-0.141E-8	-0.555666	0.0091881	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	D: 0	DEN	0.0	0.0	0.0	0.0	0.0	0.483685	-0.288E-7	3.04067	0.0	0.0	0.0	0.0
	Div. 3	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	16.20219	0.0
		DCARGR-TS	-0.171E-8	0.0	-22.523	-67875.2	0.0	109051.2	0.0	-0.080657	-0.791E-8	0.411475	0.0516349	0.0
		DCARHC	-0.325E-8	0.0	0.141E-8	167600.4	0.0	8.871403	0.0	-0.016989	-0.707E-7	1.382778	0.262E-8	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	Div. 1	DEN	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	5.39747	0.0	0.0
		DCARGR-TS	0.0	0.0	968808.1	-2660908	-0.795 E - 7	80279.25	0.0	-0.214151	-0.932E-6	2077114.	300000	0.0
		DCARHC	0.0	0.0	0.137 E - 8	0.0	0.108 E - 6	2264.724	0.0	0.141E-8	-0.109 E - 5	$0.345 \mathrm{E}$ -8	0.0	0.0
		DW	0.0	0.0	0.0	0.0	0.0	392.8517	0.0	0.0	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	0.0	0.0	0.0	186.9409	0.0	0.0039664	0.0	0.0	0.0	0.0
111	Div. 2	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2(DCARGR-TS	0.0	0.0	1314663.0	-260899.8	0.0	120860.2	0.0	-0.299907	0.0	1720426.	399993.9	0.0
		DCARHC	0.0	0.0	8.57366	3836057.0	0.186E-8	-0.186E-8	0.0	-0.492839	0.0	-12.7082	0.210135	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	114.9616	0.0
		DEN	0.0	0.0	30.8368	0.0	0.0	0.0	0.0	0.0	0.0	4.033516	6.212341	0.0
	Div. 3	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DCARGR-TS	0.0	0.0	985936.7	-200734.2	0.0	90172.23	0.0	-0.177334	0.186E-8	1575897.	299999.8	0.0
		DCARHC	0.0	0.0	0.321E-7	3833079.0	0.175E-8	202.8921	0.0	-0.388562	-0.170E-5	31.62460	0.0139E-8	0.0
		DW	0.0	0.0	77.5122	0.0	0.0	0.0	0.0	0.0	0.0	0.0	28.28630	0.0
		DEN	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.937587	0.0
	Div. 1	DCARGR-TS	0.0	0.0	388879.6	-1068089	-0.313E-7	32224.09	0.0	-0.085960	-0.373E-6	833753.7	120420.0	0.0
		DCARHC	0.0	0.0	0.0	-0.372E-8	0.512E-8	110.0272	0.0	0.0	-0.886E-6	0.0	0.0	0.0
		DW	0.0	141.0	0.0	0.0	0.0	249.0799	0.0	-0.302E-7	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	24.7075	0.0	0.0	0.0	0.0	-0.302E-7	0.0	0.0	0.0	0.0
2	Div. 2	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	-0.302E-7	0.0	0.0	433.8932	0.0
201		DCARGR-TS	0.0	0.0	527413 5	-1051538	0.0	48003 31	0.0	-0 120356	0.0	691015.0	159997 6	0.0
		DCARHC	0.0	0.0	0 41653	186367-3	0.0	0.0	0.0	-0 402053	0.0	-0 617406	0.010209	0.0
		DW	0.0	0.0	519.468	0.0	0.0	0.0	-0.298E-7	-0.238E-7	0.0	0.0	58.75217	0.0
		DEN	0.0	0.0	17.9930	0.0	0.0	0.0	0.0	-0.238E-7	0.0	0.0	5.812746	0.0
	Div. 3	DM	0.0	0.0	0.0	0.0	0.0	0.0	-0.372E-8	-0.238E-7	0.0	0.0	3 681721	0.0
		DCARGR-TS	0.0	0.0	395664 7	-80762.99	0.0	36253 35	0.0	-0.071172	0.0	632986 4	120999 9	0.0
		DCABHC	0.0	-0 158E-8	0.242E-7	186222.6	0.0	9 857115	0.0	-0 316984	0.208E-8	1 536419	0.0	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	Div. 1	DCARGR-TS	0.0	0.185E-8	121642.0	-281791.8	-202600.0	-418299.0	0.0	0.0428301	-0.212E-6	0.0077834	60000.0	0.0
		DCABHC	0.0	-0.276E-8	-0.110E-8	-0.372E-8	0.558E-8	110 0272	0.0	0.0	-0.886E-6	0 149E-8	0.0	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0 2491E-4	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0 1992E-4	0.0	0.0	0.0	0.0
ņ	Div. 2	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0 1973 10 5	0.0	0.0	-0.023E 9	0.0
201		DCARGE TS	0.186E-8	0.341E.7	270268.8	106528-3	0.0	130917 9	0.0	0.604637	0.0	0.0679126	79998 78	0.0
		DCAREC	0.3795 0	0.60910-0	0.41652	186267.2	0.0	100911.9	0.0	0.402052	0.0	0.617406	0.010200	0.0
		DOANNO	-0.012E-8	0.000E-8	0.41000	100301.3	0.0	0.00	0.0	-0.402003	0.0	-0.017400	0.010209	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.68412.7	0.0	0.0	0.0	0.0
		- ·· DEN	0.0	0.0	0.0	14.005	0.0	0.0	0.0	0.00-10-1	0.0	8 883	0.0	0.0
	Div. 3	DM	0.0	0.0	0.0	14.000	0.0	0.0	0.0	0.0	0.0	0.000	0.0	0.0
		DCARCETS	0.0	0.0	0.0	78872 71	0.0	186621 4	0.0	0.0	0.0	0.0	50000.00	0.0
		DCARHC	-0.34010 7	_0.0 _0.186ឆ្ខ	0.0	186222.6	0.0	9.85711F	0.0	-0.316094	0.0	1 536/10	0.0	0.0
		2 Onitito	0.04010-1	0.1000-0	0.0	100444.0	0.0	0.001110	0.0	.0.010304	0.0	1.000419	0.0	0.0

 Table 8. Results of Model (31).

1. DW and DEN denote changes of wage and energy costs; 2. DCARGR-TS denotes changes of green programs and ISO TS investments;

3. DCARHC denotes changes of human care programs costs; 4. DM represents changes of material costs.

		ΔX^*	$\operatorname{Suppliers}(\operatorname{DMUs})$											
		and ΔC^*	TECH. A.T.	STEEL P.	D.L. KARAN	PARS HAM	FARAZAN	SIRIN S. N.	PIROOZ	ALSAN	KARIN	TIR	BARAN	HAMRAH
2014		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.172 E - 8	0.0	0.0
	Div. 1	DEN	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.172 E - 8	0.0	0.0
		DCARGR-TS	0.0	$-0.242 ext{E} - 7$	-29139.9	-845375.4	0.0	-2536489.	0.0	-0.107932	-0.613E-6	0.0151980	-284737.7	0.0
		DCARHC	0.0	0.288E-8	1.99375	-0.465E-8	-0.186E-8	139.7647	0.0	-0.022961	0.134E-6	0.0312679	0.012968	0.0
	Div. 2	DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	-0.464E-7	0.0	0.0
		DEN	0.0	0.0	395.657	0.0	-0.498E-8	0.0	0.0	0.0	0.0	-0.464 E - 7	0.0	0.0
		DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DCARGR-TS	0.0	0.271 E - 6	18142.27	-129411.1	0.0	-1002170.	0.0	-0.232607	0.135 E - 5	0.2455036	-1061060.	0.0
		DCARHC	0.0	0.623E-8	0.529113	236737.5	0.0	-0.815E-8	0.0	-0.510718	-0.171E-8	-0.840912	0.012968	0.0
	Div. 3	DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.115E-6	0.0	0.0
		DEN	0.0	0.0	100.307	0.0	0.0	0.0	0.0	0.0	0.0	0.115 E - 6	0.0	0.0
		DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DCARGR-TS	-0.674E-6	0.0	13628.13	-996953.6	0.0	-1471328.	0.0	-0.158647	0.119 E - 6	0.3812455	-795185.9	0.0
		DCARHC	0.0	-0.295 E - 8	0.0	236553.7	0.0	12.52123	0.0	-0.431735	0.0	2.092614	-0.186 E - 8	0.0
	Div. 1	DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	41.1759	0.0	0.0	0.0	0.0	0.5732829	0.0	0.0	0.0	0.0
		DCARGR-TS	0.0	-0.390E-8	1135687.0	-284467.6	0.0	-973915.	458334.1	-0.068623	-0.232E-6	0.0024823	-61693.16	-0.201 E - 7
2015		DCARHC	0.0	0.401E-6	1.81593	0.0	0.0	127.2990	0.209 E - 4	-0.209136	0.121E-6	0.0284792	0.0105793	0.0
		DW	0.0	0.0	19.8118	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DEN	0.0	0.0	43.5999	0.0	0.0	0.0	0.0	9.190957	0.0	0.0	0.0	0.0
	Div. 2	DM	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		DCARGR-TS	0.0	-0.114E-6	1526598.0	-127922.6	0.0	-217139.3	0.0	-0.151619	0.121E-6	-0.164971	-229896.4	-0.201 E - 7
		DCARHC	0.0	0.0	0.43164	215622.9	0.0	-0.279E-8	0.0	-0.416618	0.291E-8	-0.630291	0.0105793	0.0
		DW	0.0	0.0	0.0	0.0	0.0	0.0	0.0	8.543818	0.0	0.0	0.0	0.00
		DEN	0.0	0.0	21.5113	0.0	0.0	0.0	0.0	1.723376	0.0	0.0	0.0	0.0
	Div. 3	DM	0.0	0.0	101.675	0.0	0.0	0.0	0.0	0.0	0.0	$0.447 \mathrm{E}$ -7	0.0	0.0
		DCARGR-TS	0.170E-8	0.0	1144953.0	-70833.57	0.0	-632645.1	0.0	-0.101078	0.551E-7	0.336189	-172290.3	0.0
		DCARHC	0.568E-8	-0.327E-8	-0.407E-8	215455.5	0.0	11.40446	0.0	-0.352205	0.188E-8	1.707133	0.0	0.0

Table 8. Results of Model (31) (continued).

1. DW and DEN denote changes of wage and energy costs; 2. DCARGR-TS denotes changes of green programs and ISO TS investments;

3. DCARHC denotes changes of human care programs costs; 4. DM represents changes of material costs.

lower bounds and be increased to their upper bounds. In the first approach, inputs cannot decrease to less than their current values. Negative or positive changes in inputs/outputs demonstrate the direction of future investments. This paper assessed sustainability of supply chains. For prospective researchers, we suggest running our model in fields of assessing production lines, assessing electricity transfer lines, etc.

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